

微晶尺寸的计算

假设某一微晶的(hkl)面共有N层，面间距为d，光程差为 Δl 。

$$\Delta l = 2d \sin \theta = \lambda$$

$$\Delta l = 2d \sin(\theta + \varepsilon) = \lambda + 2\varepsilon d \cos \theta$$

相位差: $\Delta \phi = \frac{2\pi \Delta l}{\lambda} = 2\pi + \frac{4\pi \varepsilon d \cos \theta}{\lambda} = \frac{4\pi \varepsilon d \cos \theta}{\lambda}$

N层(hkl)面总的散射振幅为: $E = E_0 \sum_{k=0}^{N-1} e^{ik\Delta \phi}$

$$I = I_0 \frac{\sin^2 \frac{N}{2} \Delta \phi}{\sin^2 \frac{1}{2} \Delta \phi} = I_0 \frac{N^2 \sin^2 \frac{N}{2} \Delta \phi}{(\frac{N}{2} \Delta \phi)^2}$$

当 $\varepsilon = 0$ 时, $I_{\max} = I_0 N^2$

当 $\varepsilon = \varepsilon_{1/2}$ 时, $I_{1/2} = \frac{1}{2} I_{\max}$

$$\frac{I_{1/2}}{I_{\max}} = \frac{1}{2} = \frac{\sin^2 \frac{\alpha}{2}}{(\frac{\alpha}{2})^2}$$

其中 $\alpha = 4\pi N \varepsilon_{1/2} d \cos \theta / \lambda$

以 $\frac{\sin^2 \frac{\alpha}{2}}{(\frac{\alpha}{2})^2}$ 对 $\frac{\alpha}{2}$ 作图, 当 $\frac{\alpha}{2} = 1.40$ 时, $\varepsilon_{1/2} = \frac{1.40 \lambda}{2\pi N d \cos \theta}$

$$\beta_{hkl} = 4\varepsilon_{1/2} \quad \therefore \beta_{hkl} = \frac{0.89 \lambda}{N d \cos \theta} = \frac{0.89 \lambda}{D_{hkl} \cos \theta}$$

$D_{hkl} = \frac{0.89 \lambda}{\beta_{hkl} \cos \theta}$ — Scherrer公式, 表示垂直(hkl)面的平均尺度。

倒空间的描述:

$\Delta g \propto \frac{g}{d_0}$, 倒空间的倒易矢量的变化量与面间距成反比。

在某应力作用下, 该晶粒的衍射线位移与衍射线的级数有关。

微观应力的计算:

平均微观应变: $\varepsilon_{\text{平}} = \left(\frac{\Delta d}{d} \right)_{\text{平}}$, $\Delta 2\theta_2 = 2\theta_2 - 2\theta_0 = 2\theta_0 - 2\theta_1$

$\beta = 4\Delta\theta$, $\frac{\Delta d}{d} = -\cot \theta \Delta\theta$, $\therefore \left(\frac{\Delta d}{d} \right)_{\text{平}} = \frac{\beta}{4} \cot \theta$