

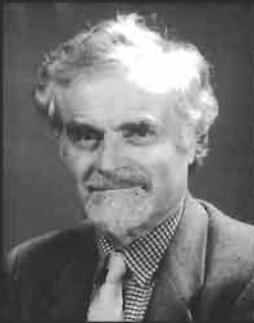
# Physical Metallurgy

Robert W. Cahn and Peter Haasen (†), editors

FOURTH, REVISED AND ENHANCED EDITION



NORTH-HOLLAND



*Prof. Robert W. Cahn, editor*





# **PHYSICAL METALLURGY**

**VOLUME I**

# LIST OF CONTRIBUTORS

A. S. Argon	C. Laird
E. Arzt	P. Lejček
H. K. D. H. Bhadeshia	W. C. Leslie
H. Biloni	Y. Limoge
J. L. Bocquet	J. D. Livingston
W. J. Boettinger	F. E. Luborsky
G. Brebec	T. B. Massalski
R. W. Cahn	J. R. Nicholls
G. Y. Chin†	A. D. Pelton
T. W. Clyne	D. G. Pettifor
R. D. Doherty	D. P. Pope
H. E. Exner	M. Rühle
R. Ferro	A. Saccone
D. R. Gaskell	S. R. J. Saunders
H. Gleiter	M. P. Seah
A. L. Greer	W. Steurer
P. Haasen†	J.-L. Strudel
J. P. Hirth	R. M. Thomson
S. Hofmann	C. M. Wayman
E. D. Hondros	M. Wilkens
E. Hornbogen	A. H. Windle
G. Kostorz	H. J. Wollenberger

# PHYSICAL METALLURGY

Fourth, revised and enhanced edition

*Edited by*

**Robert W. CAHN**

*University of Cambridge*

**Peter HAASEN†**

*University of Göttingen*

VOLUME I



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**Regretfully unnoticed, in the final printing process a layout error has occurred on the original page v, due to which the authors' names of chapters 15-19 are not correctly aligned with their chapter titles. Please use this corrected page instead.**

## SYNOPSIS OF CONTENTS

### Volume 1

1. Crystal structure of the metallic elements	<i>Steurer</i>
2. Electron theory of metals	<i>Pettifor</i>
3. Structure and stability of alloys	<i>Massalski</i>
4. Structure of intermetallic compounds and phases	<i>Ferro, Saccone</i>
<i>Appendix: Quasicrystals</i>	<i>Steurer</i>
5. Metallurgical thermodynamics	<i>Gaskell</i>
6. Phase diagrams	<i>Pelton</i>
7. Diffusion in metals and alloys	<i>Bocquet, Limoge, Brebec</i>
8. Solidification	<i>Biloni, Boettinger</i>
9. Microstructure	<i>Gleiter</i>

### Volume 2

10. Surface microscopy, qualitative and quantitative	<i>Exner</i>
11. Transmission electron microscopy	<i>Rühle, Wilkens</i>
12. X-ray and neutron scattering	<i>Kostorz</i>
13. Interfacial and surface microchemistry	<i>Hondros, Seah, Hofmann, Lejček</i>
14. Oxidation, hot corrosion and protection of metallic materials	<i>Saunders, Nicholls</i>
15. Diffusive phase transformations in the solid state	<i>Doherty</i>
16. Nondiffusive phase transformations	<i>Wayman, Bhadeshia</i>
17. Physical metallurgy of steels	<i>Leslie, Hornbogen</i>
18. Point defects	<i>Wollenberger</i>
19. Metastable states of alloys	<i>Cahn, Greer</i>

### Volume 3

20. Dislocations	<i>Hirth</i>
21. Mechanical properties of single-phase crystalline media: deformation at low temperatures	<i>Argon</i>
22. Mechanical properties of single-phase crystalline media: deformation in the presence of diffusion	<i>Argon</i>
23. Mechanical properties of solid solutions	<i>Haasen†</i>
24. Mechanical properties of intermetallic compounds	<i>Pope</i>
25. Mechanical properties of multiphase alloys	<i>Strudel</i>
26. Fracture	<i>Thomson</i>
27. Fatigue	<i>Laird</i>
28. Recovery and recrystallization	<i>Cahn</i>
29. Magnetic properties of metals and alloys	<i>Livingston, Luborsky, Chint</i>
30. Metallic composite materials	<i>Clyne</i>
31. Sintering processes	<i>Exner, Arzt</i>
32. A metallurgist's guide to polymers	<i>Windle</i>



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## PREFACE TO THE FOURTH EDITION

The first, single-volume edition of this Work was published in 1965 and the second in 1970; continued demand prompted a third edition in two volumes which appeared in 1983. The first two editions were edited by myself alone, but in preparing the third, which was much longer and more complex, I had the crucial help of Peter Haasen as co-editor. The third edition came out in 1983, and sold steadily, so that the publishers were motivated to propose the preparation of yet another version of the Work; we began the joint planning for this in early 1992. We agreed on the changes and additions we wished to make: the responsibility for commissioning chapters was divided equally between us, but the many policy decisions, made during a series of face-to-face discussions, were very much a joint enterprise. Peter Haasen was able to commission all the chapters which he had agreed to handle, and this task (which involved detailed discussions with a number of authors) was completed in early 1993. Thereupon, in May 1993, my friend of many years was suddenly taken ill; the illness worsened rapidly, and in October of the same year he died, at the early age of 66. When he was already suffering the ravages of his fatal illness, he yet found the resolve and energy to revise his own chapter and to send it to me for comments, and to modify it further in the light of those comments. He was also able to examine, edit and approve the revised chapter on dislocations, which came in early. These were the very last professional tasks he performed. Peter Haasen was in every sense co-editor of this new edition, even though fate decreed that I had to complete the editing and approval of most of the chapters. I am proud to share the title-page with such an eminent physicist.

The first edition had 22 chapters and the second, 23. There were 31 chapters in the third edition and the present edition has 32. The first two editions were single volumes, the third had to be divided into two volumes, and now the further expansion of the text has made it necessary to go to three volumes. This fourth edition is nearly three times the size of the first edition thirty years ago; this is due not only to the addition of new topics, but also to the fact that the treatment of existing topics has become much more substantial than it was in 1965. There are those who express the conviction that physical metallurgy has passed its apogee and is in steady decline; the experience of editing this edition, and the problems I have encountered in holding enthusiastic authors back from even more lengthy treatments (to avoid exceeding the agreed page limits by a wholly unacceptable margin), have shown me

how mistaken this pessimistic assessment is! Physical metallurgy, the parent discipline of materials science, has maintained its central status undiminished.

The first three editions each opened with a historical overview. We decided to omit this in the fourth edition, for two main reasons: the original author had died and it would have fallen to others to revise his work, never an entirely satisfactory proceeding; it had also become plain (especially from the reaction of the translators of the earlier editions into Russian) that the overview was not well balanced between different parts of the world. I am engaged in writing a history of materials science, as a separate venture, and this will incorporate proper attention to the history of physical metallurgy as a principal constituent. — It also proved necessary to leave out the chapter on superconducting alloys: the ceramic superconductor revolution has virtually removed this whole field from the purview of physical metallurgy. — Three entirely new topics are treated in this edition: one is oxidation, hot (dry) corrosion and protection of metallic materials, another is the dislocation theory of the mechanical behavior of intermetallic compounds. The third new topic is a leap into very unfamiliar territory: it is entitled “A Metallurgist’s Guide to Polymers”. Many metallurgists — including Alan Windle, the author of this chapter — have converted in the course of their careers to the study of the more physical aspects of polymers (regarded by many materials scientists as *the* “materials of the future”), and have had to come to terms with novel concepts (such as “semicrystallinity”) which they had not encountered in metals: Windle’s chapter is devoted to analysing in some depth the conceptual differences between metallurgy and polymer science, for instance, the quite different principles which govern alloy formation in the two classes of materials. I believe that this is the first treatment of this kind.

Six of the existing chapters (now numbered 1, 4, 21, 22, 27, 30) have been entrusted to new authors, while another five chapters have been revised by the previous authors with the collaboration of additional authors (8, 13, 16, 17, 19). Chapter 19, originally entitled “Alloys rapidly quenched from the melt” has been broadened and retitled “Metastable states of alloys”. A treatment of quasicrystals has been introduced in the form of an appendix to chapter 4, which is devoted to the solid-state chemistry of intermetallic compounds; this seemed appropriate since quasicrystallinity is generally found in such compounds. — Only three chapters still have the same authors they had in the first edition, written some 32 years ago.

27 of the 29 new versions of existing chapters have been substantially revised, and many have been entirely recast. Two chapters (11 and 25) have been reprinted as they were in the third edition, except for corrected cross-references to other chapters, but revision has been incorporated in the form of an Addendum to each of these chapters; this procedure was necessary on grounds of timing.

This edition has been written by a total of 44 authors, working in nine countries. It is a truly international effort.

I have prepared the subject index and am thus responsible for any inadequacies that may be found in it. I have also inserted some cross-references between chapters (internal cross-references within chapters are the responsibility of the various authors), but the function of such cross-references is better achieved by liberal use of the subject index.

As always, the editors have been well served by the exceedingly competent staff of North-Holland Physics Publishing (which is now an imprint of Elsevier Science B.V. in

Amsterdam; at the time of the first two editions, North-Holland was still an independent company). My particular thanks go to Nanning van der Hoop and Michiel Born on the administrative side, to Ruud de Boer who is responsible for production and to Chris Ryan and Maurine Alma who are charged with marketing. Mr. de Boer's care and devotion in getting the proofs just right have been extremely impressive. My special thanks also go to Professor Colin Humphreys, head of the department of materials science and metallurgy in Cambridge University, whose warm welcome and support for me in my retirement made the creation of this edition feasible. Finally, my thanks go to all the authors, who put up with good grace with the numerous forceful, sometimes impatient, messages which I was obliged to send in order to "get the show on the road", and produced such outstanding chapters under pressure of time.

I am grateful to Dr. W.J. Boettinger, one of the authors, and his colleague Dr. James A. Warren, for kindly providing the computer-generated dendrite microstructure that features on the dust-cover.

The third edition was dedicated to the memory of Robert Franklin Mehl, the author of the historical chapter and a famed innovator in the early days of physical metallurgy in America. I would like to dedicate this fourth edition to the memory of two people: my late father-in-law, *Daniel Hanson* (1892–1953), professor of metallurgy at Birmingham University for many years, who did more than any other academic in Britain to foster the development and teaching of modern physical metallurgy; and the physical metallurgist and scientific publisher — and effective founder of Pergamon Press — *Paul Rosbaud* (1896–1963), who was retained by the then proprietor of the North-Holland Publishing Company as an adviser and in 1960, in the presence of the proprietor, eloquently urged upon me the need for a new, advanced, multiauthor text on physical metallurgy.

November 1995  
Cambridge

Robert W. CAHN



## PREFACE TO THE THIRD EDITION

The first edition of this book was published in 1965 and the second in 1970. The book continued to sell well during the 1970s and, once it was out of print, pressure developed for a new edition to be prepared. The subject had grown greatly during the 1970s and R. W. C. hesitated to undertake the task alone. He is immensely grateful to P. H. for converting into a pleasure what would otherwise have been an intolerable burden!

The second edition contained twenty-two chapters. In the present edition, eight of these twenty-two have been thoroughly revised by the same authors as before, while the others have been entrusted to new contributors, some being divided into pairs of chapters. In addition, seven chapters have been commissioned on new themes. The difficult decision was taken to leave out the chapter on superpure metals and to replace it by one focused on solute segregation to interfaces and surfaces — a topic which has made major strides during the past decade and which is of great practical significance. A name index has also been added.

Research in physical metallurgy has become worldwide and this is reflected in the fact that the contributors to this edition live in no fewer than seven countries. We are proud to have been able to edit a truly international text, both of us having worked in several countries ourselves. We would like here to express our thanks to all our contributors for their hard and effective work, their promptness and their angelic patience with editorial pressures!

The length of the book has inevitably increased, by 50% over the second edition, which was itself 20% longer than the first edition. Even to contain the increase within these numbers has entailed draconian limitations and difficult choices; these were unavoidable if the book was not to be priced out of its market. Everything possible has been done by the editors and the publisher to keep the price to a minimum (to enable readers to take the advice of G. CHR. LICHTENBERG [1775]: “He who has two pairs of trousers should pawn one and buy this book”).

Two kinds of chapters have been allowed priority in allocating space: those covering very active fields and those concerned with the most basic topics such as phase transformations, including solidification (a central theme of physical metallurgy), defects and diffusion. Also, this time we have devoted more space to experimental methods and their underlying principles, microscopy in particular. Since there is a plethora of texts available on the standard aspects of X-ray diffraction, the chapter on X-ray and neutron scattering has been

designed to emphasize less familiar aspects. Because of space limitations, we regretfully decided that we could not include a chapter on corrosion.

This revised and enlarged edition can properly be regarded as to all intents and purposes a new book.

Sometimes it was difficult to draw a sharp dividing line between physical metallurgy and process metallurgy, but we have done our best to observe the distinction and to restrict the book to its intended theme. Again, reference is inevitably made occasionally to nonmetallics, especially when they serve as model materials for metallic systems.

As before, the book is designed primarily for graduate students beginning research or undertaking advanced courses, and as a basis for more experienced research workers who require an overview of fields comparatively new to them, or with which they wish to renew contact after a gap of some years.

We should like to thank Ir. J. Soutberg and Drs. A.P. de Ruiter of the North-Holland Publishing Company for their major editorial and administrative contributions to the production of this edition, and in particular we acknowledge the good-humoured resolve of Drs. W.H. Wimmers, former managing director of the Company, to bring this third edition to fruition. We are grateful to Dr. Bormann for preparing the subject index. We thank the hundreds of research workers who kindly gave permission for reproduction of their published illustrations: all are acknowledged in the figure captions.

Of the authors who contributed to the first edition, one is no longer alive: Robert Franklin Mehl, who wrote the introductory historical chapter. What he wrote has been left untouched in the present edition, but one of us has written a short supplement to bring the treatment up to date, and has updated the bibliography. Robert Mehl was one of the founders of the modern science of physical metallurgy, both through his direct scientific contributions and through his leadership and encouragement of many eminent metallurgists who at one time worked with him. We dedicate this third edition to his memory.

April 1983

Robert W. CAHN, Paris  
Peter HAASEN, Göttingen

## PREFACE TO THE FIRST AND SECOND EDITIONS

This book sets forth in detail the present state of physical metallurgy, which is the root from which the modern science of materials has principally sprung. That science has burgeoned to such a degree that no one author can do justice to it at an advanced level; accordingly, a number of well-known specialists have consented to write on the various principal branches, and the editor has been responsible for preserving a basic unity among the expert contributions. This book is the first general text, as distinct from research symposium, which has been conceived in this manner. While principally directed at senior undergraduates at universities and colleges of technology, the book is therefore also appropriate for postgraduates and particularly as a base for experienced research workers entering fields of physical metallurgy new to them.

Certain topics have been left to one side or treated at modest length, so as to limit the size of the book, but special stress has been placed on others which have rarely been accorded much space. For instance, a good deal of space is devoted to the history of physical metallurgy, and to point defects, structure and mechanical properties of solid solutions, theory of phase transformations, recrystallization, superpure metals, ferromagnetic properties, and mechanical properties of two-phase alloys. These are all active fields of research. Experimental techniques, in particular diffraction methods, have been omitted for lack of space; these have been ably surveyed in a number of recent texts. An exception has however been made in favour of metallographic techniques since, electron microscopy apart, recent innovations have not been sufficiently treated in texts.

Each chapter is provided with a select list of books and reviews which will enable readers to delve further into a particular subject. Internal cross-references and the general index will help to tie the various contributions together.

I should like here to acknowledge the sustained helpfulness and courtesy of the publisher's staff, and in particular of Mr. A. T. G. van der Leij, and also the help provided by Professor P. Haasen and Dr. T. B. Massalski in harmonising several contributions.

*Brighton, June 1965 (and again 1970) R. W. CAHN*



## CONTENTS

<i>List of contributors</i> .....	ii
<i>Synopsis of contents</i> .....	v
<i>Preface to the fourth edition</i> .....	vii
<i>Preface to the third edition</i> .....	xii
<i>Preface to the first and second editions</i> .....	xiii

## VOLUME I

<i>Chapter 1. Crystal structure of the metallic elements, by W. Steurer</i> .....	1
1. Introduction .....	2
2. Factors governing a crystal structure .....	2
2.1. Chemical bond factor .....	3
2.1.1. The covalent bond .....	3
2.1.2. The metallic bond .....	4
2.2. Geometrical factors .....	5
2.2.1. Coordination .....	7
2.2.2. Space filling .....	7
2.2.3. Layer stackings, polytypism .....	7
2.2.4. Polymorphism .....	10
3. Crystal structure of metallic elements .....	12
3.1. Nomenclature .....	13
3.2. Group 1 and 2, alkali and alkaline earth metals .....	15
3.3. Groups 3 to 10, transition metals .....	18
3.4. Groups 11 and 12, copper and zinc group metals .....	21
3.5. Groups 13 to 16, metallic and semi-metallic elements .....	22
3.6. Lanthanides and actinides .....	28
References .....	45
Further reading .....	46

<i>Chapter 2. Electron theory of metals, by D. G. Pettifor . . . . .</i>	47
1. Introduction . . . . .	48
2. Band formation . . . . .	50
2.1. The constituent atoms . . . . .	50
2.2. Bond formation . . . . .	59
2.3. Band formation . . . . .	63
3. Simple-metal bands . . . . .	64
3.1. The free-electron approximation . . . . .	64
3.2. Nearly-free-electron approximation . . . . .	67
3.3. Volume dependence . . . . .	72
4. Transition-metal bands . . . . .	77
4.1. Tight-binding approximation . . . . .	77
4.2. Hybrid NFE-TB bands . . . . .	82
4.3. Volume dependence . . . . .	84
5. Bulk properties . . . . .	87
5.1. Simple metals . . . . .	87
5.2. Transition metals . . . . .	90
6. Structural stability . . . . .	95
6.1. Elemental metals . . . . .	95
6.2. Binary intermetallic phases . . . . .	102
7. Heat of formation . . . . .	111
8. Band theory of magnetism . . . . .	123
References . . . . .	129
Further reading . . . . .	133
<i>Chapter 3. Structure and stability of alloys, by T. B. Massalski . . . . .</i>	135
1. Solid solubility . . . . .	136
2. Terminology (types of solid solutions) . . . . .	138
3. Energy of solid solutions and phase stability considerations . . . . .	140
4. Factors governing solid solubility (Hume-Rothery rules for primary solid solutions) . . . . .	144
5. The meaning of "electron concentration" . . . . .	147
5.1. Progress in the electronic theories of metals and alloys . . . . .	149
6. Termination of primary solid solubility . . . . .	150
6.1. Electronic theories of primary solid solutions based on noble metals . . . . .	150
6.2. Primary solid solubility in transition metal alloys . . . . .	154
7. The atomic size in solid solutions . . . . .	154
7.1. The size factor . . . . .	157
7.2. The measurement of atomic size in terms of volume . . . . .	159
7.3. Combined effects of size and electronegativity . . . . .	161
7.4. Strain in solid solutions . . . . .	161
7.5. Deviation from Vegard's law . . . . .	164
7.6. Measurement of actual atomic sizes in solid solutions . . . . .	165
8. Intermediate phases with wide solid solubility . . . . .	166
8.1. The electron phases . . . . .	166
8.2. Electron phases with cubic symmetry . . . . .	168

8.3. Electron phases with hexagonal symmetry . . . . .	170
8.4. Laves phases . . . . .	176
8.5. Phases with wide solubility formed by the transition elements . . . . .	178
9. Lattice spacings in solid solutions . . . . .	180
9.1. Lattice spacings in primary solid solutions . . . . .	180
9.2. The relationship between lattice spacings and magnetic properties . . . . .	184
10. Defect structures . . . . .	186
10.1. Vacancies and vacant sites in structures of alloys . . . . .	186
10.2. Stacking faults . . . . .	189
10.3. Metastable structures . . . . .	192
11. Order in solid solutions . . . . .	193
11.1. Types of superlattices . . . . .	194
11.2. Long-period superlattices . . . . .	195
11.3. Long-range order and short-range order . . . . .	198
References . . . . .	199
Further reading . . . . .	203

<i>Chapter 4. Structure of intermetallic compounds and phases, by R. Ferro and A. Saccone</i>	205
1. Introduction . . . . .	206
1.1. Preliminary remarks and definition of an intermetallic phase . . . . .	206
1.2. Identification of the intermetallic phases . . . . .	209
2. Chemical composition of the intermetallic phase and its compositional formula . . . . .	210
3. Crystal structure of the intermetallic phase and its representation . . . . .	214
3.1. Unit cell description (general remarks, lattice complexes) . . . . .	214
3.2. Structural types . . . . .	220
3.3. Unit cell Pearson symbol . . . . .	223
3.4. Structure trivial names and symbols . . . . .	224
3.5. Rational crystal structure formulae . . . . .	227
3.5.1. Coordination and dimensionality symbols in the crystal coordination formula . . . . .	228
3.5.2. Layer stacking sequence representation . . . . .	231
3.5.3. Assembly of polyhedra . . . . .	237
3.5.4. Modular aspect of crystal structure . . . . .	240
3.5.5. An exercise on the use of alternative structural notations ( $\text{AuCu}_3$ type as an example) . . . . .	241
4. Relationships between structures and structure “families” . . . . .	247
4.1. Degenerate and derivative structures, superstructures (defect, filled-up, derivative structures)	247
4.1.1. Ordering-disordering transformation . . . . .	251
4.2. Antiphase domain structures . . . . .	256
4.3. Homeotect structure types (polytypic structures) . . . . .	256
4.4. Chimney-ladder structures (structure commensurability, structure modulation) . . . . .	258
4.5. Recombination structures, intergrowth structure series . . . . .	260
4.6. Group-subgroup relations for the representation of crystal-chemical relationships . . . . .	263
5. Elements of systematic description of structure types. General remarks and references . . . . .	264
6. Description of a few selected structural types . . . . .	267
6.1. bcc W-type structure and derivative structures . . . . .	268
6.1.1. Structural type: $\text{cI}2-\text{W}$ . . . . .	268

6.1.2.	Structural type: cP2–CsCl .....	268
6.1.3.	Structural type: cF16–MnCu <sub>2</sub> Al .....	271
6.1.4.	Structural types: cF16–Li <sub>3</sub> Bi and cF16–NaTl .....	272
6.1.5.	Comments on the bcc derivative structures .....	273
6.2.	Close-packed structures and derivative structures .....	275
6.2.1.	Structural type: cF4–Cu .....	275
6.2.2.	Cu-derivative, substitutional and interstitial superstructures (tetrahedral and octahedral holes) .....	275
6.2.3.	Structural type: cP4–AuCu <sub>3</sub> .....	279
6.2.4.	Structural types: tP2–AuCu (I) and oI40–AuCu(II) .....	279
6.2.5.	Structural type: tP4–Ti <sub>3</sub> Cu .....	279
6.2.6.	Structural types: hP2–Mg, hP4–La and hR9–Sm .....	280
6.2.7.	Structural type: hP8–Ni <sub>3</sub> Sn .....	281
6.2.8.	Structural type: hP6–CaCu <sub>5</sub> .....	281
6.3.	Tetrahedral structures .....	283
6.3.1.	cF8–C (diamond) and tI4– $\beta$ Sn structural types .....	283
6.3.2.	Structural types: cF8–ZnS sphalerite and hP4–ZnO (ZnS wurtzite) .....	285
6.3.3.	General remarks on “tetrahedral structures” and polytypes. tI16–FeCuS <sub>2</sub> , hP4–C lonsdaleite, oP16–BeSiN <sub>2</sub> types and polytypes .....	286
6.3.4.	An important non-tetrahedral C structure. The hP4–C graphite .....	288
6.4.	cF8–NaCl, cF12–CaF <sub>2</sub> , and cF12–AgMgAs types .....	288
6.4.1.	cF8–NaCl type structure and compounds .....	288
6.4.2.	cF12–CaF <sub>2</sub> type and antitype structures and compounds .....	291
6.4.3.	Structural type: cF12–AgMgAs .....	293
6.5.	hP4–NiAs, cP3–CdI <sub>2</sub> , hP6–Ni <sub>2</sub> In, oP12–Co <sub>2</sub> Si, oP12–TiNiSi types; hP2–WC, hP3–AlB <sub>2</sub> , hP6–CaIn <sub>2</sub> , hP9–Fe <sub>2</sub> P types, tI8–NbAs, tI8–AgTlTe <sub>2</sub> and tI10–BaAl <sub>4</sub> (ThCr <sub>2</sub> Si <sub>2</sub> ) types, tI12–ThSi <sub>2</sub> and tI12–LaPtSi types .....	293
6.5.1.	Structural type: hP4–NiAs .....	294
6.5.2.	Structural type: hP3–CdI <sub>2</sub> .....	294
6.5.3.	Structural type: hP6–Ni <sub>2</sub> In .....	294
6.5.4.	Structural types: oP12–Co <sub>2</sub> Si (PbCl <sub>2</sub> ) and oP12–TiNiSi .....	295
6.5.5.	Structural type: hP2–WC .....	295
6.5.6.	Structural types: hP3–AlB <sub>2</sub> and hP3–BaPtSb; hP3– $\omega$ , Cr-Ti phase .....	296
6.5.7.	Structural type: hP6–CaIn <sub>2</sub> .....	297
6.5.8.	Structural type: hP9–Fe <sub>2</sub> P .....	299
6.5.9.	Structural types: tI8–NbAs, tI8–AgTlTe <sub>2</sub> and tI10–BaAl <sub>4</sub> (ThCr <sub>2</sub> Si <sub>2</sub> ) .....	299
6.5.10.	Structural types: tI12– $\alpha$ ThSi <sub>2</sub> and tI12–LaPtSi .....	304
6.6.	Tetrahedrally close-packed, Frank–Kasper structures, Laves phases, Samson phases .....	307
6.6.1.	General remarks .....	307
6.6.2.	cP8–Cr <sub>3</sub> Si type cP8–Cr <sub>3</sub> Si type structure .....	309
6.6.3.	$\sigma$ phase type structure, (tP30– $\sigma$ -Cr–Fe type) .....	309
6.6.4.	Laves phases: cF24–Cu <sub>2</sub> Mg (and cF24–Cu <sub>4</sub> MgSn and cF24–AuBe <sub>5</sub> ), hP12–MgZn <sub>2</sub> (and hP12–U <sub>2</sub> O <sub>3</sub> Al <sub>3</sub> ) and hP24–Ni <sub>2</sub> Mg types .....	311
6.6.5.	Structures based on frameworks of fused polyhedra, Samson phases .....	314
7.	On some regularities in the intermetallic compound formation and structures .....	315
7.1.	Preliminary remarks .....	315
7.2.	On some factors which control the structure of intermetallic phases .....	317
7.2.1.	Chemical bond factor and electrochemical factor .....	322
7.2.2.	Energy band factor, electron concentration .....	325
7.2.3.	Geometrical principles and factors, Laves' stability principles .....	326
7.2.4.	Atomic dimensions and structural characteristics of the phases .....	328
7.2.5.	Reduced dimensional parameters .....	334
7.2.6.	Alternative definitions of coordination numbers .....	338
7.2.7.	Atomic-environment classification of the structure types .....	342

8.	Semi-empirical approaches to the prediction of (intermetallic) compound formation . . . . .	345
8.1.	General remarks on procedures of prediction of compound and structure formation in alloy systems . . . . .	345
8.2.	Stability diagrams, structure maps . . . . .	345
8.3.	Savitskii–Gribulya–Kiselyova method (cybernetic computer-learning prediction system) .	346
8.4.	Villars, Villars and Grgis approaches (analysis of the dependence of the behaviour of alloy systems on the properties of the component elements) . . . . .	347
8.5.	Miedema's theory and structural information . . . . .	349
8.6.	Prediction of the properties of selected families of alloys: Gschneidner's relations as an example . . . . .	351
8.7.	Pettifor's chemical scale and structure maps . . . . .	352
Appendix 1.	Gazetteer, in alphabetic order, of intermetallic phases cited in this chapter. . . . .	355
References	. . . . .	363
 <i>Appendix to chapter 4. The structure of quasicrystals, by W. Steurer . . . . .</i>		371
1.	Introduction . . . . .	372
2.	Description of quasiperiodic structures . . . . .	374
2.1.	Decoration of quasiperiodic tilings . . . . .	374
2.2.	Higher-dimensional approach . . . . .	376
2.3.	Symmetry of quasicrystals . . . . .	378
3.	The structure of quasicrystals and approximants . . . . .	379
3.1.	One-dimensional quasicrystals . . . . .	380
3.2.	Two-dimensional quasicrystals . . . . .	381
3.2.1.	Octagonal phases . . . . .	381
3.2.2.	Decagonal phases . . . . .	382
3.2.3.	Dodecagonal phases . . . . .	391
3.3.	Icosahedral phases . . . . .	391
3.3.1.	Primitive hypercubic icosahedral phases . . . . .	395
3.3.2.	Face-centered hypercubic icosahedral phases . . . . .	401
References	. . . . .	408
Further reading	. . . . .	411
 <i>Chapter 5. Metallurgical thermodynamics, by D. R. Gaskell . . . . .</i>		413
1.	Introduction . . . . .	414
1.1.	The First and Second Laws of Thermodynamics . . . . .	414
1.2.	Auxiliary thermodynamic functions . . . . .	415
2.	Metallurgical thermochemistry . . . . .	417
2.1.	The measurement of changes in enthalpy . . . . .	417
2.2.	The measurement of entropy . . . . .	419
3.	Phase equilibrium in a one-component system . . . . .	422
4.	Chemical reaction equilibrium . . . . .	424
5.	Ellingham diagrams . . . . .	429
6.	The thermodynamic properties of solutions . . . . .	435
6.1.	Mixing processes . . . . .	435
6.2.	Regular solution behavior . . . . .	439
7.	The thermodynamic origin of phase diagrams . . . . .	443

8.	Reaction equilibrium involving solutions and the Gibbs phase rule . . . . .	447
8.1.	The dependence of the equilibrium state on activity . . . . .	447
8.2.	The Gibbs phase rule . . . . .	450
9.	The thermodynamics of surfaces and interfaces . . . . .	453
9.1.	The Gibbs adsorption isotherm . . . . .	453
9.2.	The Langmuir adsorption isotherm . . . . .	456
9.3.	Curved interfaces . . . . .	458
10.	The measurement of thermodynamic activity . . . . .	460
10.1.	Determination of activity by experimental measurement of vapor pressure . . . . .	461
10.2.	Determination of activity by establishing heterogeneous equilibrium . . . . .	464
10.3.	Electrochemical measurement of activity . . . . .	467
	Bibliography . . . . .	469
	<i>Chapter 6. Phase diagrams, by Arthur D. Pelton</i> . . . . .	471
1.	Introduction . . . . .	472
2.	Binary phase diagrams . . . . .	472
2.1.	The thermodynamic origin of phase diagrams . . . . .	474
2.2.	Minima and maxima in two-phase regions . . . . .	477
2.3.	Miscibility gaps . . . . .	478
2.4.	Simple eutectic systems . . . . .	480
2.5.	Binary phase diagrams with no intermediate phases . . . . .	481
2.5.1.	Thermodynamic origin illustrated by simple regular solution theory . . . . .	481
2.5.2.	Liquid–liquid immiscibility – monotectics . . . . .	483
2.5.3.	Peritectics . . . . .	483
2.5.4.	Syntactics . . . . .	485
2.6.	Limited mutual solid solubility . . . . .	485
2.7.	Calculation of limiting slopes of phase boundaries . . . . .	488
2.8.	Intermediate phases . . . . .	489
2.9.	Topology of binary phase diagrams . . . . .	492
2.9.1.	Order-disorder transformations . . . . .	494
2.10.	Application of thermodynamics to phase diagram analysis . . . . .	495
2.10.1.	Polynomial representation of excess properties . . . . .	496
2.10.2.	Least-squares optimization . . . . .	496
2.10.3.	Calculation of metastable phase boundaries . . . . .	500
2.11.	Solution models . . . . .	500
2.12.	Binary phase diagrams involving a gaseous phase . . . . .	502
3.	Ternary phase diagrams . . . . .	503
3.1.	The ternary composition triangle . . . . .	503
3.2.	Ternary space model . . . . .	504
3.3.	Polythermal projections of liquidus surfaces . . . . .	506
3.4.	Ternary isothermal sections . . . . .	509
3.4.1.	Topology of ternary isothermal sections . . . . .	511
3.5.	Ternary isopleths (constant composition sections) . . . . .	512
4.	Multicomponent phase diagrams . . . . .	514
4.1.	Zero phase fraction lines . . . . .	515
4.2.	Nomenclature for invariant reactions . . . . .	515
5.	Thermodynamic calculation of ternary and multicomponent phase diagrams . . . . .	516
6.	Phase diagrams with potentials as axes . . . . .	518
6.1.	Classification of phase diagrams . . . . .	524

7.	Experimental techniques of measuring phase diagrams .....	525
7.1.	Thermal analysis .....	526
7.2.	Sampling techniques and quenching techniques .....	528
7.3.	Other techniques .....	529
8.	Bibliography .....	530
8.1.	Compilations of phase diagrams .....	530
8.2.	Texts and review articles .....	530
9.	Acknowledgements .....	531
	References .....	531
	<i>Chapter 7. Diffusion in metals and alloys, by J. L Bocquet, G. Brebec and Y. Limoge . .</i>	535
1.	Macroscopic and microscopic theories of diffusion .....	536
1.1.	The mechanisms of diffusion .....	536
1.1.1.	Exchange mechanisms .....	536
1.1.2.	Mechanisms involving point defects .....	536
1.1.2.1.	Interstitial mechanisms .....	537
1.1.2.2.	Vacancy mechanisms .....	538
1.1.2.3.	Mixed mechanisms .....	538
1.1.2.4.	Short-lived Frenkel pairs .....	539
1.1.3.	Mechanisms involving extended defects .....	539
1.2.	The macroscopic theory of diffusion .....	539
1.2.1.	Generalities .....	539
1.2.2.	Binary alloys and the vacancy mechanism .....	539
1.2.3.	Some special cases .....	541
1.2.3.1.	Chemical diffusion .....	541
1.2.3.2.	Dilute systems .....	542
1.2.4.	The various diffusion coefficients .....	543
1.2.5.	Fick's second Law .....	545
1.3.	The random walk theory of diffusion .....	546
1.3.1.	Einstein relation and flux expression .....	546
1.3.2.	Calculation of $\bar{X}$ and $\bar{X}^2$ in terms of jump frequencies .....	547
1.3.2.1.	Expression for $\bar{X}^2$ .....	548
1.3.2.2.	Expression for $\bar{X}$ .....	548
1.3.3.	Binary alloys and vacancy mechanism .....	550
1.3.4.	Correlation effects .....	550
1.3.5.	The limitation of Fick's Law .....	552
1.4.	Jump frequency and diffusion coefficient calculation .....	553
1.4.1.	Vacancy concentration .....	553
1.4.2.	Vacancy jump .....	554
1.4.2.1.	Rate theory of jumps .....	554
1.4.2.2.	Dynamic theory of jumps .....	555
1.4.3.	Macroscopic parameters of diffusion .....	557
1.4.3.1.	Variation with temperature .....	557
1.4.3.2.	Variation with pressure .....	558
1.4.3.3.	Variation with atomic mass .....	558
1.5.	Numerical simulation approaches .....	559
1.5.1.	Molecular Dynamics method .....	560
1.5.2.	Monte Carlo method .....	561
2.	Experimental methods .....	562
2.1.	Macroscopic methods .....	563
2.1.1.	D from the $C(x)$ curve .....	563

2.1.1.1. C(x) by sample sectioning .....	563
2.1.1.2. Non-destructive techniques .....	563
2.1.2. Other macroscopic methods .....	564
2.2. Microscopic (or local) methods .....	564
2.2.1. Relaxation methods .....	565
2.2.1.1. Thermodynamic aspects of relaxation .....	565
2.2.1.2. Anelasticity .....	566
2.2.1.3. Snoek relaxation .....	567
2.2.1.4. Zener relaxation .....	567
2.2.1.5. Gorsky effect .....	568
2.2.1.6. Magnetic relaxation in ferromagnetic alloys .....	569
2.2.1.7. Kinetics of short-range ordering .....	570
2.2.2. Spectroscopic methods .....	570
2.2.2.1. Nuclear magnetic resonance .....	570
2.2.2.2. Mössbauer effect .....	571
2.2.2.3. Quasi-elastic neutron scattering .....	572
3. Self-diffusion in pure metals .....	572
3.1. Self-diffusion in fcc and hcp metals .....	574
3.2. Diffusion in bcc metals .....	580
3.3. Prediction of the self-diffusion coefficients .....	581
3.3.1. Theoretical calculations of D .....	581
3.3.2. Empirical relations .....	582
4. Self- and solute-diffusion in dilute alloys .....	582
4.1. Vacancy diffusion in dilute A-B alloys .....	583
4.1.1. Standard models for bcc and fcc alloys .....	583
4.1.2. Kinetic expressions of the phenomenological coefficients $L_{AA}$ , $L_{AB}$ , $L_{BA}$ and $L_{BB}$ .....	584
4.1.2.1. Kinetic theory .....	584
4.1.2.2. Linear response method .....	586
4.1.3. Experimentally accessible quantities .....	588
4.1.4. Determination of vacancy jump frequencies .....	589
4.1.5. Determination of the solute–vacancy binding energy .....	592
4.2. Dumb-bell interstitial diffusion in dilute A-B alloys .....	592
4.3. A-B alloys with a high solute diffusivity .....	593
4.3.1. Purely interstitial solutes .....	593
4.3.2. Complex diffusion mechanisms .....	594
5. Diffusion in concentrated alloys .....	595
5.1. Diffusion of A* and B* tracers in homogeneous disordered alloys .....	595
5.1.1. Experimental results .....	595
5.1.2. Manning's random alloy model .....	596
5.1.3. Atomic models for diffusion in non-random disordered alloy .....	598
5.2. Diffusion of A* and B* tracers in ordered binary alloys .....	599
5.2.1. Ordered alloys with B <sub>2</sub> structure .....	602
5.2.1.1. Experimental results .....	603
5.2.1.2. Atomic mechanisms for diffusion in ordered B <sub>2</sub> alloys .....	604
5.2.2. Ordered alloys with L1 <sub>2</sub> structure .....	604
5.2.3. Ordered alloys with L1 <sub>0</sub> structure .....	606
5.2.4. Ordered alloys with DO <sub>3</sub> structure .....	606
5.2.5. Ordered alloys with B8 structure .....	606
5.2.6. Ordered alloys with B3 <sub>2</sub> structure .....	607
5.2.7. Ordered alloys with A15 structure .....	607
5.3. Chemical diffusion .....	607
5.3.1. Chemical diffusion in binary systems and Kirkendall effect .....	608
5.3.1.1. Description and interpretation of a typical experiment .....	608

5.3.1.2. Vacancy wind effect — Manning's approximation .....	609
5.3.1.3. Experimental check of vacancy wind effect .....	611
5.3.2. Ternary alloys .....	611
6. Electro- and thermomigration .....	612
6.1. Thermodynamic aspects .....	612
6.2. Microscopic analysis .....	613
6.3. Experimental methods .....	614
6.4. Experimental results and discussion .....	615
6.4.1. Thermomigration .....	615
6.4.2. Electromigration .....	616
6.5. Electromigration in short-circuits .....	617
6.6. Electromigration as a purification process .....	618
7. Diffusion along short-circuits .....	619
7.1. Phenomenological approach .....	619
7.1.1. Semi-infinite bicrystal .....	621
7.1.2. Semi-infinite crystal with an isolated dislocation .....	621
7.1.3. Short-circuit networks .....	622
7.1.4. Experimental results .....	623
7.2. New advances in grain-boundary diffusion .....	623
7.2.1. Impurity effects .....	623
7.2.2. Diffusion-induced grain-boundary migration (DIGM) .....	623
7.3. Atomistic approach to diffusion in short-circuits .....	624
7.3.1. Atomic model for grain-boundary diffusion .....	624
7.4. Surface diffusion .....	626
7.4.1. Atomic structure and point defects .....	626
7.4.2. Experimental results .....	630
7.4.2.1. Microscopic data .....	630
7.4.2.2. Macroscopic data .....	631
8. Diffusion under non-equilibrium defect concentrations .....	633
8.1. Quenched-in vacancies .....	633
8.2. Cold-work-induced defects .....	634
8.3. Irradiation-induced defects .....	635
8.3.1. Irradiation-enhanced diffusion .....	635
8.3.1.1. Defect creation .....	636
8.3.1.2. Collisional diffusion .....	637
8.3.1.3. Diffusion by thermally activated jumps .....	638
8.3.2. Irradiation-induced segregation and precipitation .....	640
8.3.3. Irradiation-induced phase transformations .....	643
9. Diffusion in amorphous metallic alloys .....	643
9.1. A primer of metallic glasses .....	644
9.1.1. Experimental portrait of the diffusion behaviour .....	645
9.1.2. Mechanism proposals .....	648
9.2. Simulation approach of the self-diffusion process .....	648
9.3. Random walk on a random array .....	649
References .....	651
Further reading .....	666
<i>Chapter 8. Solidification, by H. Biloni and W. J. Boettinger</i> .....	669
1. Introduction .....	670
2. Heat flow in solidification .....	670

2.1.	Heat transfer within the solid/liquid metal system . . . . .	670
2.2.	Heat transfer at the metal-mould interface . . . . .	673
2.3.	Heat flow in one dimensional solidification geometries . . . . .	675
2.3.1.	Freezing at mould wall . . . . .	676
2.3.2.	Rapid freezing in contact with a cold substrate with initial melt supercooling . . . . .	677
2.4.	Heat flow in more complex solidification geometries . . . . .	679
2.4.1.	Heat flow in controlled directional solidification of metals . . . . .	679
2.4.2.	Powder solidification . . . . .	679
2.5.	Software packages . . . . .	680
2.6.	Experimental methods involving controlled solidification . . . . .	681
3.	Thermodynamics of solidification . . . . .	682
3.1.	Hierarchy of equilibrium . . . . .	682
3.2.	$T_0$ curves . . . . .	686
4.	Nucleation . . . . .	687
4.1.	Nucleation in pure liquids . . . . .	687
4.1.1.	Calculation of the critical radius and energy barrier . . . . .	688
4.1.2.	Nucleation rate . . . . .	691
4.2.	Effect of melt subdivision . . . . .	693
4.3.	Experiments on nucleation in pure metals . . . . .	693
4.4.	Alloy nucleation . . . . .	695
4.5.	Experiments on heterogeneous nucleation . . . . .	697
4.6.	Formation of metastable phases by supercooling . . . . .	699
4.7.	Grain size predictions in castings . . . . .	700
5.	Interface kinetics . . . . .	700
5.1.	Pure materials . . . . .	700
5.1.1.	Interface structure . . . . .	702
5.1.2.	Continuous growth . . . . .	704
5.1.3.	Growth of a diffuse interface . . . . .	707
5.1.4.	Two dimensional nucleation controlled growth . . . . .	707
5.1.5.	Growth by screw dislocations . . . . .	708
5.1.6.	Transition between continuous growth and faceted growth . . . . .	708
5.2.	Binary alloys . . . . .	709
6.	Solidification of alloys with planar and nearly planar S-L interfaces . . . . .	714
6.1.	General formulation of diffusion controlled growth . . . . .	714
6.2.	Solute redistribution during one dimensional solidification . . . . .	714
6.2.1.	Equilibrium freezing . . . . .	714
6.2.2.	Complete liquid mixing, with no solid diffusion . . . . .	715
6.2.3.	Solid diffusion during solidification . . . . .	716
6.2.4.	Steady-state diffusion controlled freezing . . . . .	717
6.2.5.	Convection effects. Freezing with partial mixing in the liquid (Boundary Layer Approach) . . . . .	718
6.2.6.	Zone melting . . . . .	719
6.3.	Lateral segregation . . . . .	720
6.4.	Morphological stability of a planar interface . . . . .	720
6.4.1.	Theory . . . . .	721
6.4.2.	Relationship to constitutional supercooling . . . . .	724
6.4.3.	Experiments . . . . .	725
6.4.4.	Further theoretical developments . . . . .	726
6.5.	Coupled interface and fluid flow instabilities . . . . .	729
7.	Cellular and dendritic solidification . . . . .	731
7.1.	Alloy dendritic growth . . . . .	732
7.1.1.	Theory of the tip region . . . . .	732

7.1.2. Anisotropy . . . . .	737
7.1.3. Approximate theory for low supercooling . . . . .	739
7.1.4. Experiments on dendritic growth . . . . .	739
7.2. Cell and dendrite spacings . . . . .	741
7.2.1. Numerical calculations of arrayed cell and dendrite primary spacings . . . . .	741
7.2.2. Analytical expressions for primary spacings . . . . .	743
7.2.3. Secondary dendrite arm spacing . . . . .	746
7.2.4. Cell to dendrite transition . . . . .	748
7.3. Microsegregation . . . . .	749
7.4. Solidification of ternary alloys . . . . .	752
7.5. New approaches to modeling dendritic growth . . . . .	755
8. Polyphase solidification . . . . .	755
8.1. Eutectic solidification . . . . .	756
8.1.1. Eutectic classification . . . . .	757
8.1.2. Non-facetted–Non-facetted eutectics . . . . .	757
8.1.3. Non-facetted–facetted eutectics . . . . .	763
8.1.4. Eutectic cells and dendrites . . . . .	765
8.1.5. Competitive growth – coupled zone . . . . .	765
8.1.6. Divorced eutectics . . . . .	767
8.1.7. Rapid solidification of eutectic alloys . . . . .	768
8.2. Monotectic solidification . . . . .	771
8.2.1. Directional solidification of monotectic alloys . . . . .	773
8.2.2. Rapid solidification of monotectic alloys . . . . .	775
8.3. Peritectic solidification . . . . .	775
8.3.1. Peritectic solidification during dendritic growth . . . . .	776
8.3.2. Aligned peritectic growth . . . . .	778
8.3.3. Rapid solidification of peritectic systems . . . . .	779
9. Fluid flow and casting structure . . . . .	780
9.1. Transport processes and fluid flow in casting . . . . .	780
9.2. Ingot structure . . . . .	781
9.2.1. Chill zone . . . . .	781
9.2.2. Columnar zone . . . . .	782
9.2.3. Equiaxed zone . . . . .	785
9.2.3.1. Origin of the equiaxed nuclei . . . . .	785
9.2.3.2. Columnar to equiaxed transition (CET) . . . . .	786
9.3. Macrosegregation . . . . .	789
9.3.1. Gravity segregation . . . . .	789
9.3.2. Interdendritic fluid flow and macrosegregation . . . . .	789
9.3.3. Further theoretical developments for flow in the mushy zone . . . . .	792
9.4. Porosity and inclusions . . . . .	792
9.4.1. Porosity . . . . .	793
9.4.2. Inclusions . . . . .	794
9.5. Fluidity . . . . .	795
9.5.1. Maximum fluidity . . . . .	796
9.5.2. Combined effects of surface tension and fluidity . . . . .	797
9.5.3. Continuous fluidity length . . . . .	797
10. Solidification processes . . . . .	797
10.1. Continuous casting . . . . .	797
10.1.1. Continuous casting of steels . . . . .	799
10.1.2. Continuous casting of light alloys . . . . .	801
10.2. Fusion welding structures . . . . .	803
10.2.1. Weld pool geometry . . . . .	806
10.2.2. Macro- and microstructures of welds . . . . .	807
11. Structure manipulation and new processes . . . . .	809

11.1. Single crystal growth from the melt . . . . .	809
11.2. Grain refinement . . . . .	810
11.2.1. Thermal methods . . . . .	810
11.2.2. Innoculation methods . . . . .	812
11.2.3. Energy-induced methods . . . . .	814
11.3. Eutectic modification . . . . .	815
11.3.1. Aluminum–silicon alloys . . . . .	815
11.3.2. Cast iron . . . . .	816
11.3.3. Cast iron eutectic morphology . . . . .	817
11.4. Influence of rapid solidification processes (RSP) . . . . .	820
11.4.1. Experimental and production methods . . . . .	820
11.4.2. Relationships between RSP and solidification structures . . . . .	821
11.5. Low gravity effects during solidification . . . . .	821
11.6. Solidification processing of metal matrix composites . . . . .	824
11.7. Semisolid metal forming processes . . . . .	826
References . . . . .	830
Further reading . . . . .	842
 <i>Chapter 9. Microstructure, by H. Gleiter . . . . .</i>	843
1. Definition and outline . . . . .	844
2. Elements of microstructure . . . . .	844
2.1. Point defects, dislocations and stacking faults . . . . .	844
2.2. Grain boundaries . . . . .	844
2.2.1. Crystallography . . . . .	844
2.2.1.1. Coincidence site lattice . . . . .	844
2.2.1.2. O-lattice . . . . .	845
2.2.1.3. DSC lattice . . . . .	847
2.2.2. Coincidence models . . . . .	847
2.2.3. Structural unit models . . . . .	848
2.2.4. Broken bond model . . . . .	850
2.2.5. Dislocation models . . . . .	853
2.2.6. Polyhedral unit models . . . . .	855
2.2.7. Limitations of existing models . . . . .	856
2.3. Interphase boundaries . . . . .	859
2.3.1. Bonding at interphase boundaries . . . . .	859
2.3.2. Chemistry of interphase boundaries . . . . .	862
2.3.2.1. Interfaces without reaction layers . . . . .	862
2.3.2.2. Interfaces with reaction layers . . . . .	862
2.3.3. Crystallographic structure: “lock-in” model . . . . .	864
3. Characterization of microstructure . . . . .	865
4. Development of microstructure . . . . .	870
4.1. Basic aspects . . . . .	870
4.2. Microstructural changes stimulated by interfacial-energy reduction . . . . .	870
4.2.1. Microstructural changes in single-phase materials, stimulated by interfacial energy: domain and grain growth . . . . .	870
4.2.2. Microstructural changes in polyphase materials with a dispersion structure, stimulated by interfacial energy: Ostwald ripening . . . . .	873
4.2.2.1. Stability against coarsening . . . . .	877
4.2.2.2. Technological applications of coarsening theory . . . . .	878
4.2.3. Microstructural changes in polyphase materials with a duplex structure stimulated by interfacial energy . . . . .	878

4.2.4. Coarsening by Brownian motion . . . . .	882
4.2.5. Microstructural changes stimulated by interfacial energy in the presence of external potential fields . . . . .	883
4.2.5.1. Temperature gradients . . . . .	883
4.2.5.2. Temperature cycling . . . . .	884
4.2.5.3. Magnetic fields . . . . .	885
4.2.5.4. Stress field . . . . .	885
4.2.5.5. Electric fields . . . . .	886
4.3. Deformation . . . . .	886
4.4. Multiphase microstructures generated by migrating lattice defects . . . . .	887
4.4.1. Moving grain boundaries . . . . .	887
4.4.2. Moving dislocations . . . . .	889
4.5. Periodic microstructures in open, dissipative systems ("self-organization") . . . . .	890
4.5.1. Periodic structures due to long-range interaction forces . . . . .	892
4.5.1.1. Precipitate lattices . . . . .	892
4.5.1.2. Void lattices . . . . .	892
4.5.1.3. Dislocation-loop lattices . . . . .	893
4.5.1.4. Point-defect lattices . . . . .	894
4.5.1.5. Long-period antiphase boundary structures . . . . .	894
4.6. Microstructure in the vicinity of point defect sources and/or sinks . . . . .	894
4.6.1. Enhanced precipitation and precipitate-free zones . . . . .	894
4.6.2. Irradiation-induced precipitation . . . . .	896
4.6.3. Point-defect condensation . . . . .	896
4.7. Microstructure due to lattice defects formed by migrating grain boundaries . . . . .	896
4.8. Microstructure of glasses . . . . .	897
4.8.1. Microstructure of amorphously phase-separated glasses . . . . .	898
4.8.2. Microstructure of partially crystallized glasses . . . . .	899
5. Nanostructured materials . . . . .	900
5.1. Materials with reduced dimensionality, reduced dimensions and/or high densities of defect cores . . . . .	901
5.2. Man-made superlattices and quantum-well structures . . . . .	902
5.3. Semicrystalline polymers . . . . .	903
5.4. Nanocrystalline and nanoglassy materials . . . . .	908
5.4.1. Basic concepts . . . . .	908
5.4.2. Generation of nanocrystalline materials . . . . .	914
5.4.3. Atomic structure . . . . .	916
5.5. Nanoglasses . . . . .	921
5.6. Nanocomposites . . . . .	923
5.6.1. Nanocomposites made up of crystallites with different chemical compositions . . . . .	925
5.6.2. Nanocomposites made up of crystallites and glassy components with different chemical compositions . . . . .	925
5.6.3. Nanocomposites with intercalated (doped) grain boundaries . . . . .	925
5.7. Technological applications . . . . .	928
5.7.1. Hard, wear-resistant nanocrystalline WC-Co materials . . . . .	928
5.7.2. Near net shape forming of nanocrystalline ceramics/intermetallics . . . . .	928
5.7.3. Soft ferromagnetic nanostructured materials ("Finemet") . . . . .	930
5.7.4. Magneto-caloric cooling with nanostructured materials . . . . .	931
5.7.5. Nanocrystalline magnetic recording materials . . . . .	932
5.7.6. Giant magnetoresistance in nanostructured materials . . . . .	932
5.7.7. Luminescence from porous Si . . . . .	933
5.7.8. Catalytic materials . . . . .	935
References . . . . .	935
Further reading . . . . .	942

**VOLUME II**

<i>Chapter 10. Qualitative and quantitative surface microscopy, by H. E. Exner .....</i>	943
1. Introduction .....	944
2. Optical microscopy .....	945
2.1. Metallographic specimen preparation .....	945
2.1.1. Sampling .....	945
2.1.2. Mounting .....	947
2.1.3. Grinding .....	947
2.1.4. Polishing .....	948
2.1.5. Replica techniques .....	950
2.2. Etching and other contrasting techniques .....	950
2.2.1. Chemical and electrolytic etching .....	950
2.2.2. Thermal etching .....	951
2.2.3. Ion-etching .....	951
2.2.4. Staining (tinting) and anodic oxidation .....	952
2.2.5. Interference-layer contrast .....	953
2.3. Principles of light microscopy and optical contrast enhancement .....	954
2.3.1. Resolution and depth of focus .....	955
2.3.2. Bright-field illumination .....	955
2.3.3. Oblique illumination, dark field and stop contrast .....	955
2.3.4. Polarized-light microscopy .....	956
2.3.5. Phase contrast and interference contrast .....	957
2.3.6. Filters .....	958
2.4. Special optical devices and accessories .....	958
2.4.1. Stereomicroscopy .....	958
2.4.2. Laser scanning and confocal microscopy .....	958
2.4.3. Scanning near-field optical microscopy .....	959
2.4.4. High-temperature microscopy .....	959
2.4.5. Television cameras .....	960
2.4.6. Microphotometry and ellipsometry .....	960
2.4.7. Interferometry .....	960
2.4.8. Microhardness .....	961
3. Scanning electron microscopy .....	961
3.1. Basic features of scanning electron microscopy .....	961
3.2. Specimen preparation .....	966
3.3. Typical forms of contrast .....	967
3.3.1. Topographic contrast .....	967
3.3.2. Material (atomic number) contrast .....	968
3.3.3. Electron channelling contrast, electron channelling and Kossel patterns .....	969
3.3.4. Magnetic contrast .....	970
3.3.5. Charge collection microscopy and electron-beam-induced current measurements .....	970
3.3.6. X-ray mapping .....	970
3.3.7. Cathodoluminescence .....	971
3.4. Accessory equipment .....	971
3.4.1. Stereomicroscopy .....	971
3.4.2. Dynamic and non-ambient-temperature SEM .....	972
4. Scanning tunneling, atomic force and related microscopies .....	972
4.1. Basic principles and capabilities .....	974
4.2. Atomic force microscopy .....	974
4.3. Tunneling spectroscopy .....	976

4.4. Related scanning techniques . . . . .	976
4.5. Applications . . . . .	977
5. Other special techniques of surface microscopy . . . . .	979
5.1. Scanning acoustic and thermal wave microscopy . . . . .	979
5.1.1. Scanning laser acoustic microscopy . . . . .	980
5.1.2. Thermal-wave microscopy . . . . .	981
5.2. Field-ion and field-electron microscopy . . . . .	981
5.2.1. Field-ion microscopy . . . . .	981
5.2.2. Atom-probe field-ion microscopy . . . . .	982
5.2.3. Field-electron microscopy . . . . .	983
5.2.4. Applications of field-ion microscopy . . . . .	983
5.3. Photo-electron emission microscopy . . . . .	985
5.4. Scanning Auger-electron microscopy . . . . .	986
5.5. X-ray microscopy, topography and fluorescence . . . . .	987
5.6. Imaging by other types of spectroscopic information . . . . .	988
6. Topochemical techniques and surface spectroscopy . . . . .	988
7. Quantitative interpretation of microstructural geometry . . . . .	996
7.1. Image analysis . . . . .	996
7.2. Planar characteristics and stereology . . . . .	1001
7.2.1. Volume-fraction analysis . . . . .	1001
7.2.2. Interface density . . . . .	1004
7.2.3. Size and distance . . . . .	1005
7.2.4. Orientation, contiguity, shape and other complex parameters . . . . .	1010
7.3. Mathematical morphology . . . . .	1014
7.4. Further aspects . . . . .	1016
References . . . . .	1016
Further reading . . . . .	1030
<i>Chapter 11. Transmission electron microscopy, by M. Rühle and M. Wilkens . . . . .</i>	1033
1. Introductory remarks . . . . .	1034
2. The instrument . . . . .	1034
3. Information from the diffraction pattern . . . . .	1038
3.1. Diffraction spot pattern . . . . .	1038
3.1.1. Double diffraction . . . . .	1038
3.1.2. Patterns from ordered crystals . . . . .	1039
3.2. Kikuchi lines . . . . .	1040
3.3. Convergent-beam diffraction . . . . .	1040
3.4. Moiré pattern . . . . .	1042
4. Theory of diffraction contrast . . . . .	1042
4.1. Introduction . . . . .	1042
4.2. Specimen, reciprocal lattice and excitation error . . . . .	1043
4.3. Outline of the dynamical diffraction theory . . . . .	1044
4.4. Normal and anomalous absorption . . . . .	1046
4.5. Dynamical bright-field and dark-field intensities . . . . .	1047
4.6. The column approximation . . . . .	1050
4.7. Diffraction at imperfect crystals . . . . .	1050
4.7.1. The displacement field . . . . .	1050
4.7.2. The kinematical approach . . . . .	1051
4.7.3. Dynamical diffraction theory in terms of plane waves . . . . .	1052

4.7.4. Dynamical diffraction theory in terms of Bloch waves . . . . .	1053
4.7.5. Properties of strain contrast in strong-beam images . . . . .	1054
4.7.6. Structure-factor contrast . . . . .	1056
4.8. Practical applications of the differential equations . . . . .	1056
5. Dislocations . . . . .	1056
5.1. Introduction . . . . .	1056
5.2. The displacement field . . . . .	1057
5.3. Contrast profiles of single perfect dislocations . . . . .	1057
5.3.1. The $\mathbf{g} \cdot \mathbf{b} \neq 0$ contrast . . . . .	1057
5.3.2. The $\mathbf{g} \cdot \mathbf{b} = 0$ contrast . . . . .	1058
5.4. Contrast of dislocation pairs . . . . .	1059
5.5. Determination of the dislocation Burgers vectors and the dislocation densities . . . . .	1061
5.6. Elastic anisotropy . . . . .	1062
6. Point-defect agglomerates, radiation damage . . . . .	1063
6.1. Introduction . . . . .	1063
6.2. Dislocation loops . . . . .	1063
6.2.1. Formation of loops . . . . .	1063
6.2.2. Analysis of large dislocation loops . . . . .	1064
6.2.3. Small dislocation loops . . . . .	1064
6.3. Stacking-fault tetrahedra . . . . .	1066
6.4. Cavities . . . . .	1066
6.5. Displacement cascades and disordered zones . . . . .	1067
7. Precipitates . . . . .	1067
8. Structure of grain boundaries and interfaces . . . . .	1069
8.1. Transmission electron microscopy of pure translation interfaces . . . . .	1072
8.2. Transmission electron microscopy of grain boundaries . . . . .	1075
8.3. Diffraction studies on the structure of grain boundaries . . . . .	1077
8.4. Direct imaging of grain boundaries . . . . .	1077
8.5. TEM contrast of heterophase boundaries . . . . .	1078
9. High-resolution TEM . . . . .	1079
9.1. Introduction . . . . .	1079
9.2. The optical transfer function . . . . .	1081
9.3. Consequences of the wave aberration . . . . .	1082
9.4. The weak-phase object approximation . . . . .	1083
9.5. Some remarks to the high-resolution images of crystalline specimens . . . . .	1085
10. Analytical electron microscopy . . . . .	1086
10.1. Basic considerations . . . . .	1086
10.2. Quantitative analytical electron microscopy of thin foils: analysis of X-rays . . . . .	1088
10.2.1. Cross-section for inner-shell ionization . . . . .	1089
10.2.2. Thin-film approximation . . . . .	1089
10.2.3. Beam-spreading in the specimen . . . . .	1090
10.2.4. Errors limiting the data of X-ray analysis . . . . .	1090
10.2.5. Examples . . . . .	1091
10.3. Quantitative analytical electron microscopy of thin foils — electron energy loss spectroscopy . . . . .	1091
10.3.1. Examples . . . . .	1093
Appendix. Elements of the kinematical diffraction theory . . . . .	1094
A.1. Introduction . . . . .	1094
A.2. Fundamental equations . . . . .	1095
A.3. Real space and reciprocal space, description of perfect crystal structures . . . . .	1097
A.4. The kinematical diffraction amplitude $F(\mathbf{K})$ of a perfect crystal . . . . .	1099
A.5. The Ewald sphere and Bragg's law . . . . .	1101
A.6. The atomic scattering amplitudes and the Debye–Waller factor . . . . .	1102

A.7. Imperfect crystals .....	1104
References .....	1105
General bibliography for transmission electron microscopy .....	1108
Addendum .....	1109
B.1. Instrumentation .....	1110
B.2. Conventional transmission electron microscopy including weak beam .....	1111
B.3. Analytical electron microscopy .....	1111
B.4. High-resolution transmission electron microscopy .....	1112
Addendum References .....	1112
 <i>Chapter 12. X-ray and neutron scattering, by G. Kostorz</i> .....	1115
1. Introduction .....	1116
2. Scattering from real crystals .....	1117
2.1. General predictions of the kinematical theory .....	1117
2.2. X-rays and neutrons .....	1119
2.3. Magnetic scattering .....	1123
2.4. Inelastic and quasi-elastic scattering .....	1126
2.5. Some experimental considerations .....	1128
3. Bragg peaks and vicinity .....	1130
3.1. Peak shifts .....	1130
3.2. Peak broadening and intensity changes .....	1132
3.3. Diffuse scattering near Bragg peaks .....	1134
4. Between Bragg peaks .....	1139
4.1. Displacement scattering .....	1139
4.2. Short-range order .....	1144
5. Near the incident beam .....	1161
5.1. Small-angle scattering .....	1162
5.2. Alloys .....	1166
5.3. Defects .....	1179
5.4. Special topics .....	1181
6. Energy transfers .....	1183
6.1. Phonons in real crystals .....	1183
6.2. Diffuse motion .....	1187
References .....	1188
Further reading .....	1198
 <i>Chapter 13. Interfacial and surface microchemistry, by E. D. Hondros, M. P. Seah, S. Hofmann and P. Lejček</i> .....	1201
1. Introduction — The chemistry of interfaces and physical metallurgy .....	1202
2. Thermodynamic features of interfacial adsorption .....	1205
3. Methods of measuring the microchemistry of interfaces .....	1209
3.1. The interfacial energy or Gibbsian approach .....	1210
3.2. Modern surface analysis techniques .....	1211
3.3. Micrographic techniques .....	1216
4. Theory of segregation processes .....	1218

4.1.	Introduction: equilibrium and non-equilibrium segregation .....	1218
4.2.	The Langmuir–McLean theory .....	1219
4.2.1.	Prediction of the free energy of segregation to grain boundaries .....	1221
4.2.2.	Prediction of the free energy of segregation to surfaces .....	1225
4.2.3.	Segregation with adsorbate–adsorbate interactions .....	1229
4.2.4.	Temperature dependence of the free energies of segregation .....	1230
4.3.	Segregation in simple ternary systems: site competition .....	1232
4.4.	Segregation in complex metallurgical systems .....	1233
4.5.	Anisotropy of segregation .....	1234
4.5.1.	Segregation at symmetrical grain boundaries .....	1235
4.5.2.	Segregation at asymmetrical grain boundaries .....	1237
4.5.3.	Computer simulation of grain-boundary segregation .....	1238
4.5.4.	Correlation between grain-boundary and free-surface segregation .....	1240
4.6.	The kinetics of segregation .....	1242
4.7.	Non-equilibrium segregation .....	1244
4.7.1.	Solute pile-up at growing precipitates .....	1244
4.7.2.	Quench-induced segregation .....	1245
4.7.3.	Stress-induced segregation .....	1248
4.7.4.	Segregation at moving grain boundaries .....	1248
4.7.5.	Radiation-induced segregation .....	1249
5.	Segregation-related physicochemical properties .....	1249
5.1.	Interfacial energetics .....	1249
5.2.	Surface and grain-boundary kinetics .....	1254
5.3.	Grain-boundary cohesion .....	1258
6.	Metallurgical phenomena affected by segregation .....	1263
6.1.	Surface free energy change: role in creep cavitation .....	1263
6.2.	Grain-boundary diffusivity: role in diffusion creep .....	1268
6.3.	Interfacial cohesion: role in temper-brittleness .....	1270
6.4.	Further examples of metallurgical phenomena influenced by microchemical processes .....	1274
6.4.1.	Microchemical barrier layers .....	1274
6.4.2.	Creep-embrittlement .....	1275
6.4.3.	Intergranular stress-corrosion cracking .....	1276
6.4.4.	Intergranular hydrogen-embrittlement .....	1279
6.4.5.	Inhibition of surface oxidation on alloys .....	1279
7.	Interfacial microchemistry and materials design theory .....	1280
	References .....	1284
	Further reading .....	1288
	<i>Chapter 14. Oxidation, hot corrosion and protection of metallic materials, by S. R. J. Saunders and J. R. Nicholls</i> .....	1291
1.	Introduction .....	1292
1.1.	Definitions .....	1292
1.2.	General .....	1292
1.3.	Outline .....	1293
2.	Fundamentals of oxidation .....	1293
2.1.	Thermodynamics .....	1293
2.2.	Oxide structure .....	1296
2.2.1.	Amorphous oxides .....	1296
2.2.2.	Crystalline oxides .....	1296
2.3.	Kinetics .....	1297
2.3.1.	Thin film region .....	1298

2.3.2. Thick film region .....	1299
2.4. Properties of oxide layers .....	1303
2.4.1. Electrical properties (diffusion) .....	1303
2.4.2. Mechanical properties (stress generation and relief) .....	1304
3. Oxidation of alloys .....	1306
3.1. Selective oxidation .....	1306
3.2. Internal oxidation .....	1309
3.3. Intermetallic alloys .....	1309
3.4. Scale adhesion .....	1309
4. Multi-component atmospheres .....	1311
4.1. Phenomenology .....	1311
4.2. Prediction of reaction products .....	1312
4.3. Reaction path .....	1315
5. Hot-salt corrosion .....	1317
5.1. The environment .....	1317
5.2. Phenomenology of hot-salt corrosion .....	1319
5.3. Mechanism of attack .....	1319
5.3.1. $\text{Na}_2\text{SO}_4$ -induced attack .....	1319
5.3.2. Vanadate-induced attack .....	1323
5.4. Coal-fired gas turbines .....	1325
6. Test and measurement methods .....	1326
6.1. Monitoring oxidation processes .....	1326
6.1.1. Isothermal testing .....	1326
6.1.2. Cyclic oxidation .....	1328
6.1.3. Mechanistic studies .....	1328
6.2. Mechanical failure of oxide scales .....	1330
6.2.1. Internal stress measurements .....	1330
6.2.2. Detection of scale failure .....	1333
6.2.3. Measurement of the macro defects (cracks, voids and pores) present in an oxide scale .....	1334
6.3. Mixed oxidant tests .....	1335
6.3.1. Control of gas composition .....	1336
6.3.2. Experimental procedures .....	1337
6.4. Attack by molten salts .....	1337
6.5. Attack by solid deposits .....	1338
7. Life prediction modelling .....	1338
7.1. Oxidation models .....	1338
7.2. A probabilistic model of corrosion loss .....	1339
7.3. Modelling extreme corrosion .....	1340
7.4. Development of a life prediction model .....	1341
8. Developments in coating technology .....	1343
8.1. Diffusion-coating processes .....	1345
8.2. Modified aluminide coatings .....	1347
8.3. Overlay coatings processes .....	1348
8.3.1. Physical vapor deposition .....	1349
8.3.2. Spraying processes .....	1350
8.3.3. Laser processes .....	1351
8.4. Oxidation and hot-salt corrosion resistance of diffusion and overlay coatings .....	1351
8.5. Thermal stability of diffusion and overlay coatings .....	1352
8.6. Mechanical properties of diffusion and overlay coatings .....	1353
8.7. Future trends in overlay coating design .....	1354

References .....	1357
Further reading .....	1361
<i>Chapter 15. Diffusive phase transformations in the solid state, by R. D. Doherty .....</i>	1363
1. General considerations .....	1364
1.1. Introduction .....	1364
1.2. Driving forces — free energy changes .....	1365
1.3. Stable and unstable free-energy curves .....	1368
1.4. Gibbs's two types of transformation .....	1369
1.5. First order and higher order transformations .....	1371
1.6. Short-range and long-range diffusion .....	1371
1.7. Techniques for studying phase transformations .....	1372
2. Nucleation-and-growth transformations .....	1374
2.1. Theory of nucleation .....	1374
2.1.1. Interfacial structure and energy .....	1378
2.1.2. Equilibrium shape .....	1380
2.1.3. Strain energy .....	1383
2.1.4. Heterogeneous nucleation .....	1385
2.1.5. Experimental studies of nucleation .....	1389
2.2. Growth processes .....	1395
2.2.1. Growth without change of composition .....	1396
2.2.2. Transformations involving long-range diffusion .....	1400
2.2.3. Role of interface structure in growth processes .....	1405
2.2.4. Growth of ledged interfaces .....	1409
2.2.5. Quantitative experimental observations of growth rates .....	1415
2.2.5.1. Interface-controlled growth rates, without change of composition	1415
2.2.5.2. Reactions involving long-range solute diffusion	1418
2.2.6. Growth instabilities .....	1421
2.2.6.1. Initial instability .....	1421
2.2.6.2. Linear growth models .....	1427
2.3. Precipitate dissolution .....	1431
2.4. Competitive growth .....	1434
2.4.1. Growth from a supersaturated matrix after "soft" impingement .....	1435
2.4.2. Competitive coarsening: Ostwald ripening .....	1437
2.4.3. During initial nucleation and growth .....	1443
2.4.4. Coarsening of Widmanstätten precipitates .....	1448
2.5. Discontinuous reactions: moving two-phase boundary MTPB reactions .....	1451
2.5.1. Eutectoidal decomposition .....	1451
2.5.2. Discontinuous precipitation — MTPB precipitation .....	1456
2.5.3. Discontinuous (MTPB) coarsening .....	1458
2.5.4. Determination of lamellar spacing in discontinuous (MTB) reactions .....	1460
2.5.5. Diffusion-induced grain-boundary migration (DIGM) .....	1461
2.5.6. Experimental results on discontinuous eutectoidal reactions .....	1468
2.6. Bainitic transformations .....	1468
3. Continuous transformations .....	1480
3.1. Spinodal decomposition .....	1480
3.2. Continuous ordering .....	1490
4. Application of phase transformation theory to specific alloy systems .....	1494
5. Problems in phase transformations .....	1495
References .....	1497
Further reading .....	1505

<i>Chapter 16. Phase transformations, nondiffusive, by C. M. Wayman and H. K. D. H. Bhadeshia . . . . .</i>	1507
1. Overview . . . . .	1508
2. Martensitic transformations . . . . .	1508
2.1. Introduction and general characteristics . . . . .	1508
2.2. Experimental observations of crystallographic features . . . . .	1510
2.3. The phenomenological crystallographic theory of martensitic transformations . . . . .	1514
2.3.1. Summary of Crystallographic Theory . . . . .	1515
2.3.2. The inhomogeneous shear and martensite substructure . . . . .	1517
2.3.3. Mathematical description of the phenomenological crystallographic theory . . . . .	1518
2.3.4. Some other crystallographic observations . . . . .	1521
2.3.5. Further observations on the martensite morphology and substructure . . . . .	1522
2.4. Martensite-parent interfaces . . . . .	1524
2.5. Energetics of martensitic transformations . . . . .	1527
2.5.1. Transformation hysteresis and the reverse transformation . . . . .	1527
2.6. Thermoelastic and non-thermoelastic martensitic transformations . . . . .	1528
2.6.1. Free energy change due to martensitic transformation . . . . .	1529
2.6.2. Nucleation of martensite . . . . .	1530
2.7. Mechanical effects in martensitic transformations . . . . .	1531
2.7.1. Introductory comments . . . . .	1531
2.7.2. Chemical and mechanical driving forces . . . . .	1532
2.7.3. Critical stress to induce martensitic transformation . . . . .	1535
2.7.4. Transformation-induced plasticity (TRIP) . . . . .	1536
2.8. Mechanical effects specific to thermoelastic martensitic transformations . . . . .	1538
2.8.1. General . . . . .	1538
2.8.2. The shape memory effect (SME) . . . . .	1538
2.8.3. The two-way shape memory effect . . . . .	1540
2.8.4. The engine effect in shape memory alloys . . . . .	1541
2.8.5. Pseudoelastic effects . . . . .	1541
2.8.6. Pseudoelastic effects: superelasticity . . . . .	1541
2.8.7. Pseudoelastic effects: rubber-like behavior . . . . .	1542
2.8.8. Martensite-to-martensite transformations . . . . .	1543
3. Crystallographically similar transformations . . . . .	1544
3.1. The bainite transformation in steels . . . . .	1544
3.2. Oxides and hydrides . . . . .	1544
3.3. The CuAu II ordering reaction . . . . .	1544
4. Omega phase formation . . . . .	1546
5. Phase changes and charge density waves . . . . .	1548
References . . . . .	1552
General bibliography . . . . .	1553
<i>Chapter 17. Physical metallurgy of steels, by W. C. Leslie and E. Hornbogen . . . . .</i>	1555
1. Iron and steel . . . . .	1556
1.1. Introduction . . . . .	1556
1.2. Some properties of pure iron . . . . .	1557
2. Alloys of iron . . . . .	1561
2.1. Interstitial alloys . . . . .	1561
2.2. Substitutional alloys . . . . .	1566
2.3. Interstitial plus substitutional alloys . . . . .	1568

3. Transformation reactions . . . . .	1570
3.1. Pearlite . . . . .	1570
3.2. Martensite . . . . .	1572
3.3. Bainite . . . . .	1576
3.4. Transformation diagrams and hardenability . . . . .	1577
3.5. Tempering of martensite . . . . .	1579
4. Deformation and recrystallization . . . . .	1583
4.1. Microstructure of deformed steel . . . . .	1583
4.2. Recovery and recrystallization . . . . .	1587
5. Mechanical properties . . . . .	1589
5.1. Strength of ferrite . . . . .	1589
5.2. Properties of structural steels . . . . .	1594
5.2.1. High-strength low-alloy steels . . . . .	1600
5.3. Strength of martensite . . . . .	1602
5.4. Strength and ductility of tempered martensite . . . . .	1604
5.5. Ultra-high-strength steels . . . . .	1607
5.5.1. Maraging steels . . . . .	1607
5.5.2. Modified standard steels . . . . .	1608
5.5.3. Thermomechanically-treated steels . . . . .	1609
5.6. Tool steels . . . . .	1610
5.7. Austenitic steels . . . . .	1610
5.8. Steels for low-temperature applications . . . . .	1611
5.9. Segregation of solutes and steel purity . . . . .	1612
6. Other physical properties . . . . .	1613
6.1. Steels for nuclear applications . . . . .	1613
6.2. Steels for electrical applications . . . . .	1614
7. Solidification . . . . .	1615
7.1. Rimming steel, killed steel . . . . .	1615
7.2. Cast irons . . . . .	1616
References . . . . .	1618
Further reading . . . . .	1620
<i>Chapter 18. Point defects, by H. J. Wollenberger</i> . . . . .	1621
1. Introduction . . . . .	1622
2. Vacancy properties . . . . .	1623
2.1. Theoretical background . . . . .	1623
2.2. Experimental methods and results . . . . .	1625
2.2.1. Introductory remarks . . . . .	1625
2.2.2. Enthalpy and entropy of formation . . . . .	1626
2.2.2.1. Single vacancies and di-vacancies . . . . .	1626
2.2.2.2. Differential dilatometry . . . . .	1627
2.2.2.3. Positron-annihilation spectroscopy . . . . .	1633
2.2.2.4. Resistivity measurements after quenching . . . . .	1634
2.2.3. Activation enthalpy of migration . . . . .	1635
2.2.3.1. Problems of methods of determination . . . . .	1635
2.2.3.2. Two selected pieces of evidence for vacancy migration in stage III . . . . .	1636
2.2.3.3. Experimental determination of $\Delta H_v^m$ . . . . .	1639
2.2.4. Agglomeration . . . . .	1642
2.2.5. Interaction with solutes . . . . .	1644
2.3. Vacancies in ordered alloys . . . . .	1646

3. Self-interstitials .....	1647
3.1. Production of interstitial atoms .....	1647
3.1.1. Introduction .....	1647
3.1.2. Atomic displacement cross-section for electron irradiation and the production of stable Frenkel defects .....	1648
3.2. Determination of Frenkel defect concentrations .....	1654
3.3. Interstitial properties .....	1654
3.3.1. Results of model calculations .....	1654
3.3.1.1. Activation enthalpies of formation in equilibrium and saddle-point configurations .....	1656
3.3.1.2. Dynamic properties .....	1658
3.3.1.3. Arrhenius behavior of diffusion .....	1661
3.3.1.4. Multiple interstitials .....	1662
3.3.2. Experimental methods and results .....	1663
3.3.2.1. Relaxation volume .....	1663
3.3.2.2. Configuration .....	1663
3.3.2.3. Formation enthalpy .....	1665
3.3.2.4. Activation enthalpy of migration .....	1666
3.3.2.5. The controversy on the interpretation of the recovery-stage III .....	1670
3.3.2.6. Dynamic properties .....	1672
3.3.2.7. Interstitial agglomeration .....	1673
3.3.2.8. Interstitial-solute interaction .....	1676
4. Miscellaneous radiation effects .....	1682
4.1. Introductory remarks .....	1682
4.2. Frenkel defect production by neutrons and ions .....	1683
4.2.1. Atomic displacement cross-section and cascade formation .....	1683
4.2.2. Intra-cascade defect reactions .....	1688
4.3. Fast heavy-ion irradiation .....	1690
4.4. Swelling .....	1695
4.5. Radiation-induced creep .....	1700
4.6. Self-organization of point defect agglomerates .....	1701
4.7. Radiation-induced solute segregation .....	1708
References .....	1710
Further reading .....	1720
<i>Chapter 19. Metastable states of alloys, by R. W. Cahn and A. L. Greer . . . . .</i>	1723
1. Introduction .....	1724
1.1. General features .....	1724
1.2. Methods for achieving metastability .....	1725
1.3. The nature of metastability .....	1726
2. Formation of metallic glasses (amorphous alloys) .....	1728
2.1. Formation and thermodynamics .....	1728
2.2. Compositions of amorphous alloys .....	1736
2.3. Criteria for formation of amorphous phases .....	1739
2.3.1. Criteria for amorphization by irradiation, and mechanically aided and induced amorphization .....	1747
3. Practical methods of creating metastable phases and microstructures .....	1748
3.1. Rapid quenching from the melt .....	1748
3.1.1. Cooling rates in rapid solidification processing .....	1752
3.2. Solidification of highly undercooled liquids .....	1756
3.3. Deposition by evaporation or sputtering .....	1758

3.4.	Amorphization by irradiation .....	1758
3.5.	Rapid solidification processing of surfaces .....	1759
3.6.	Electrochemical, electroless and sonochemical deposition of amorphous phases .....	1762
3.7.	Solid-state amorphization reactions (SSAR) .....	1764
3.8.	Amorphization by mechanical processing .....	1766
3.9.	Pressure effects .....	1767
4.	Metallic glasses: structure and properties .....	1769
4.1.	Structure .....	1769
4.2.	Relaxation .....	1778
4.3.	Crystallization .....	1784
4.4.	Plastic deformation and fracture .....	1796
4.4.1.	Partially devitrified (nanostructured) metallic glasses .....	1800
4.4.2.	Thermal embrittlement .....	1801
4.5.	Other properties of metallic glasses .....	1804
5.	Rapid-solidification-processed (RSP) and other metastable crystalline alloys .....	1805
5.1.	Age-hardening of light alloys .....	1805
5.2.	General characteristics of rapid-solidification-processed (RSP) crystalline alloys .....	1809
5.3.	RSP light alloys .....	1812
5.4.	Steels .....	1814
5.5.	Superalloys .....	1817
	References .....	1818
	Further reading .....	1829

### VOLUME III

	<i>Chapter 20. Dislocations, by J. P. Hirth</i> .....	1831
1.	Elementary geometrical properties .....	1832
2.	Elastic fields of dislocations .....	1834
2.1.	Displacements and stresses .....	1834
2.2.	Peach-Koehler force .....	1836
2.3.	Dislocation interactions .....	1837
2.4.	Surface effects .....	1839
2.5.	Line tension .....	1841
3.	Crystal lattice effects .....	1843
3.1.	Peierls barrier .....	1843
3.2.	Core structure and energy .....	1844
3.3.	Stacking faults and partial dislocations .....	1846
3.4.	Ordered alloys .....	1850
3.5.	Slip systems .....	1852
3.6.	Jogs .....	1853
4.	Dislocation behavior at low homologous temperatures .....	1854
4.1.	Kink motion .....	1854
4.2.	Poincaré forces and bowout .....	1855
4.3.	Granato-Lücke internal friction theory .....	1856
4.4.	Dislocation sources .....	1857
4.5.	Dislocation pile-ups .....	1858
4.6.	Pinning in alloys .....	1860
4.7.	Work-hardening .....	1862

5.	Dislocation behavior at high homologous temperatures .....	1863
5.1.	Osmotic climb forces .....	1863
5.2.	Jog drag .....	1865
5.3.	Climb .....	1866
5.4.	Solute drag .....	1866
6.	Grain boundaries .....	1869
	References .....	1872
 <i>Chapter 21. Mechanical properties of single-phase crystalline media: deformation at low temperatures, by A. S. Argon .....</i>		1877
1.	Overview .....	1878
2.	Kinematics of deformation .....	1879
2.1.	Elasticity as an affine transformation .....	1879
2.2.	Kinematics of inelastic deformation .....	1880
2.2.1.	Plasticity resulting from transformations .....	1880
2.2.2.	Plasticity resulting from dislocation glide .....	1881
2.3.	Lattice rotations accompanying slip .....	1884
3.	The mechanical threshold of deformation .....	1885
3.1.	The critical resolved shear stress for glide .....	1885
4.	Elements of thermally activated deformation .....	1887
4.1.	General principles .....	1887
4.2.	Principal activation parameters for plasticity .....	1891
4.3.	Flow stress mechanisms .....	1894
4.3.1.	Intrinsic mechanisms .....	1894
4.3.1.1.	The lattice resistance .....	1894
4.3.1.2.	The dislocation resistance .....	1895
4.3.2.	Extrinsic mechanisms .....	1896
4.3.2.1.	The solute resistance .....	1896
4.3.2.2.	Particle resistances .....	1897
4.3.2.3.	Cutting of forest dislocations .....	1903
4.4.	Superposition of resistances .....	1905
5.	Selection of slip systems in specific crystal structures .....	1906
6.	Plastic deformation by shear transformations .....	1907
6.1.	Types of transformations .....	1907
6.2.	Deformation twinning .....	1907
6.3.	Stress-induced martensitic transformations .....	1912
6.4.	Kinking .....	1912
7.	Evolution of plastic resistance with strain: strain hardening .....	1913
7.1.	General overview .....	1913
7.2.	Deformation features .....	1915
7.2.1.	The stress-strain curves .....	1915
7.2.2.	Slip distribution and dislocation microstructures .....	1918
7.2.3.	Lattice elastic strains developing during deformation .....	1923
7.2.4.	Dynamic recovery in Stage III .....	1924
7.3.	Theoretical models of strain hardening .....	1924
7.3.1.	The initial yield stress and strength differential effects .....	1924
7.3.2.	Strain hardening rate in Stage I .....	1926
7.3.3.	Strain hardening rate in Stage II .....	1926
7.3.4.	Strain hardening rate in Stage III and dynamic recovery .....	1929

7.3.5.	Strain hardening rate in stage IV .....	1930
7.3.6.	Latent hardening .....	1932
7.3.7.	Transient creep at low temperatures .....	1933
7.3.7.1.	Logarithmic creep .....	1934
7.3.7.2.	Andrade creep .....	1935
7.3.8.	Bauschinger effect .....	1935
7.3.9.	Balance between the inter-plane and intra-plane resistances and the mobile dislocation density .....	1937
7.3.10.	Yield phenomena .....	1938
8.	Deformation of polycrystalline solids .....	1940
8.1.	Plastic resistance of polycrystals .....	1940
8.2.	Evolution of deformation textures .....	1943
9.	Phenomenological continuum plasticity .....	1946
9.1.	Conditions of plastic flow in the mathematical theory of plasticity .....	1946
9.2.	Transition from dislocation mechanics to continuum mechanics .....	1947
10.	Deformation instabilities and strain localization .....	1949
11.	Contrasting crystal plasticity with that in amorphous media .....	1950
References .....		1951
Further reading .....		1954

<i>Chapter 22. Mechanical properties of single-phase crystalline media: Deformation in the presence of diffusion, by A. S. Argon .....</i>	1957
1. Overview .....	1958
2. Phenomenology of power-law creep .....	1960
2.1. Measurement of creep strain .....	1960
2.2. The functional forms of the creep relation .....	1961
3. Creep in solid-solution alloys .....	1969
4. Harper-Dorn creep .....	1973
5. Static thermal recovery .....	1973
6. Processes in steady-state creep in pure metals and class II solid-solution alloys .....	1977
6.1. Overview .....	1977
6.2. Slip distribution and dislocation clustering into sub-boundaries .....	1978
6.3. Dynamic internal stresses .....	1984
6.4. Effect of stacking-fault energy .....	1986
7. Diffusional flow .....	1988
8. Grain-boundary sliding during creep .....	1993
9. Superplasticity .....	1997
10. Other creep related phenomena .....	1999
11. Isomechanical scaling laws of inelastic behavior .....	1999
12. Phenomenological descriptions of homogenized continuum deformation behavior .....	2001
12.1. The representative volume element .....	2001
12.2. Evolution of deformation resistance .....	2002
12.3. Three-dimensional constitutive material response to deformation .....	2003
References .....	2004
Further reading .....	2006

<i>Chapter 23. Mechanical properties of solid solutions, by P. Haasen†</i> .....	2009
1. Introduction .....	2010
2. Solid-solution hardening .....	2011
2.1. Survey of stress-strain curves of fcc alloy single crystals .....	2011
2.2. Slip lines, etch pits, and electron transmission observations .....	2013
2.2.1. Slip lines and etch pits .....	2013
2.2.2. Electron transmission pictures of fcc alloys .....	2014
2.3. Theories of solid-solution hardening .....	2016
2.3.1. Dislocation locking mechanisms .....	2016
2.3.2. Summation of solute forces acting on moving dislocations .....	2018
2.4. Solid-solution effect on fcc stress-strain curves .....	2023
2.4.1. Critical shear stress $\tau_0$ of fcc solid solutions .....	2024
2.4.2. The yield phenomenon in fcc alloys .....	2028
2.4.3. Easy glide and overshoot in fcc alloys .....	2029
2.4.4. Linear hardening .....	2029
2.4.5. Dynamic recovery .....	2030
2.4.6. Deformation twinning in fcc alloys .....	2031
2.5. Solid-solution hardening in hcp crystals .....	2032
2.6. Solid-solution hardening in the bcc structure .....	2034
2.7. Hardening in the NaCl and diamond structures .....	2038
2.8. Creep of solid solutions .....	2039
2.8.1. Steady-state creep through dislocation climb .....	2040
2.8.2. Creep limited by dislocation drag (class I) and the Portevin–Le Chatelier effect .....	2041
2.8.3. Steady-state creep controlled by cross-slip .....	2042
2.9. Fatigue of solid solutions .....	2043
3. Precipitation-hardening .....	2043
3.1. Interactions between dislocations and precipitate particles .....	2044
3.2. Direct observation of precipitate-dislocation interactions .....	2047
3.3. Mechanical properties of precipitation-hardened Al alloys .....	2049
3.3.1. Overaged alloys .....	2050
3.3.2. Zone-hardened alloys .....	2051
3.4. Precipitation-hardening in other alloy systems .....	2051
3.4.1. Copper–cobalt .....	2051
3.4.2. Iron–carbon .....	2052
3.4.3. Spinodally decomposed Cu–Ti alloys .....	2055
4. Order-hardening .....	2055
4.1. The superdislocation .....	2056
4.2. Theoretical dependence of the yield stress on the degree of order .....	2059
4.2.1. Distortion of a partially ordered structure .....	2060
4.2.2. Change of lattice parameter with order .....	2060
4.2.3. Anti-phase domains of finite size .....	2061
4.2.4. Thickness of anti-phase boundary .....	2061
4.2.5. Cross-slip and climb of superdislocations .....	2061
4.2.6. Short-range order hardening .....	2061
4.2.7. Quench-hardening .....	2062
4.3. Temperature dependence of the flow stress of ordered alloys .....	2063
4.4. Creep in ordered alloys .....	2064
4.5. Twinning of ordered alloys .....	2065
References .....	2066
Further reading .....	2072

<i>Chapter 24. Mechanical properties of intermetallic compounds, by David P. Pope .....</i>	2075
1. Introduction .....	2076
2. The superdislocation and planar faults .....	2081
3. Plastic deformation of L <sub>1</sub> <sub>2</sub> materials: Ni <sub>3</sub> Al .....	2085
3.1. APBs, faults and dislocation cores in L <sub>1</sub> <sub>2</sub> materials .....	2086
4. The yield anomaly: models .....	2089
5. Plasticity of NiAl .....	2091
6. TiAl .....	2093
6.1. Two-phase L <sub>1</sub> <sub>0</sub> /DO <sub>19</sub> material: Ti-rich TiAl .....	2094
6.2. Crystal structure and phase equilibria .....	2095
6.3. Ti-rich single crystals .....	2096
7. Atomistic studies of dislocation cores in TiAl .....	2099
8. Closing remarks .....	2101
References .....	2102
Further reading .....	2104
<i>Chapter 25. Mechanical properties of multiphase alloys, by Jean-Loup Strudel .....</i>	2105
1. Introduction .....	2106
2. Description and microstructure of dispersed-phase alloys .....	2107
3. Tensile properties of two-phase alloys .....	2111
3.1. Experimental results in macroscopic tests .....	2111
3.1.1. Initial yield stress .....	2111
3.1.2. Stress-strain curves .....	2113
3.1.3. Bauschinger effect .....	2113
3.2. Microscopic mechanisms and models .....	2114
3.2.1. Initial yield stress .....	2114
3.2.2. Work-hardening at low temperature in alloys with small particles .....	2115
3.2.3. Heterogeneous deformation of alloys containing large particles .....	2124
3.3. Stress relaxation and recovery effects .....	2126
3.4. A continuum-mechanics approach to the internal stress .....	2128
4. High-temperature behavior of dispersed-phase alloys .....	2133
4.1. High-temperature subgrains in polycrystalline oxide-dispersion-strengthened alloys .....	2134
4.2. Apparent and effective creep parameters .....	2135
4.3. Average internal stresses in dispersed-phase alloys .....	2138
5. Composition and microstructure of precipitation-hardened alloys .....	2141
6. Tensile properties of precipitation-hardened alloys — behavior under high stress .....	2144
6.1. Macroscopic properties .....	2145
6.2. Deformation modes and hardening mechanisms .....	2147
6.2.1. Superlattice stacking faults .....	2149
6.2.2. Mechanical twinning of the ordered phase .....	2151
7. High-temperature creep of precipitation-hardened alloys .....	2152
7.1. Creep curves .....	2154
7.2. Deformation modes .....	2155
7.3. Internal stress .....	2155
7.4. Oriented coalescence of the hardening phase under strain .....	2157

8. Recrystallization . . . . .	2158
8.1. Particle size and amount of strain . . . . .	2159
8.2. Interparticle spacing . . . . .	2161
8.3. Effect of temperature . . . . .	2162
8.4. Micromechanisms . . . . .	2163
9. Duplex structures and multiphase alloys . . . . .	2165
9.1. Duplex structures . . . . .	2165
9.2. Multiphase precipitation-hardening . . . . .	2165
9.3. Mechanical alloying of complex alloys . . . . .	2167
9.4. Grain-size effects in multiphase alloys . . . . .	2168
References . . . . .	2174
Further reading . . . . .	2178
<i>Addendum</i> . . . . .	2179
A.1. Introduction . . . . .	2179
A.2. Stress relaxation and the measurement of activation parameters . . . . .	2179
A.3. Continuum mechanics approach to multiphase materials . . . . .	2182
A.3.1. Local micromechanical models . . . . .	2182
A.3.2. Macroscopic behavior of particle-hardened materials . . . . .	2182
A.3.3. Phenomenological approach . . . . .	2183
A.4. Oxide-dispersion-strengthened (ODS) materials and their resistance to high-temperature viscoplastic flow . . . . .	2184
A.4.1. The threshold stress . . . . .	2185
A.4.2. Dislocation climb models . . . . .	2186
A.4.3. High-temperature fatigue properties of ODS alloys . . . . .	2189
A.5. Micromechanisms of plasticity in nickel-base alloys . . . . .	2190
A.5.1. Single crystals hardened by a shearable phase . . . . .	2194
A.5.1.1. Plasticity of the $\gamma'$ phase . . . . .	2195
A.5.1.2. Plasticity of the $\gamma$ matrix . . . . .	2196
A.5.1.3. Plasticity of oriented nickel-base single crystals at intermediate temperatures . . . . .	2198
A.5.1.4. Rafting phenomena at high temperature . . . . .	2201
A.5.6. Recrystallization of ODS alloys . . . . .	2203
<i>Addendum References</i> . . . . .	2204
<i>Addendum Further reading</i> . . . . .	2206
<i>Chapter 26. Fracture, by R. M. Thomson</i> . . . . .	2207
1. Introduction and fracture overview . . . . .	2208
2. Qualitative and observational aspects of fracture . . . . .	2212
2.1. Fracture modes . . . . .	2212
2.2. Fractographic observations . . . . .	2213
2.3. The basis for fracture science . . . . .	2219
3. Elastic analysis of cracks . . . . .	2220
3.1. Stress analysis . . . . .	2220
3.2. Eshelby's theorem and the J-integral . . . . .	2225
4. Elastic dislocation-crack interactions . . . . .	2231
5. Equilibrium configurations . . . . .	2235
5.1. The Griffith crack . . . . .	2236
5.2. Shielding by one dislocation . . . . .	2237

5.3. General shielding and the extrinsic toughness of materials .....	2238
5.4. The HRR crack tip field .....	2242
5.5. Summary .....	2243
6. Atomic structure of cracks: theory .....	2245
6.1. Methodology .....	2245
6.2. Lattice trapping and slow crack growth .....	2248
6.3. The Griffith condition .....	2252
7. Atomic structure of cracks: dislocation emission .....	2254
7.1. Dislocation emission criteria .....	2255
7.2. Summary of ductility criteria .....	2260
7.3. Crack stability and mixed mode effects .....	2262
8. Interfacial cracks and chemical effects .....	2265
8.1. Elasticity of interfacial cracks .....	2265
8.2. Lattice description of the interfacial crack .....	2268
8.3. Ductility at interfaces .....	2269
9. Summary of basic ideas .....	2272
10. Some practical implications and problems .....	2274
10.1. Implications for final materials reliability .....	2275
10.2. Brittle crack initiation .....	2277
10.3. Ductile fracture, hole growth and the R curve .....	2277
10.4. Ductile-brittle transitions — temperature and rate effects .....	2280
10.5. Chemical effects — hydrogen embrittlement .....	2282
10.6. Temper embrittlement and intergranular segregation .....	2285
10.7. Liquid–metal embrittlement .....	2286
10.8. Transformation-toughening .....	2286
References .....	2287
Further reading .....	2290
 <i>Chapter 27. Fatigue, by Campbell Laird</i> .....	2293
1. Introduction — History, fatigue design and nomenclature .....	2294
2. Fatigue testing .....	2297
2.1. Constant amplitude stress tests .....	2297
2.2. Increasing stress amplitude tests .....	2298
2.3. Constant plastic strain amplitude tests .....	2298
2.4. Variable amplitude tests .....	2299
3. Performance parameters of fatigue .....	2300
3.1. Cyclic stress-strain behavior .....	2300
3.2. Fatigue life behavior .....	2303
4. Cyclic deformation .....	2304
4.1. Phenomenological behavior and dislocation structures .....	2305
4.2. Models of rapid hardening behavior: loop patches, persistent slip bands and channels .....	2313
4.3. Saturation behavior and strain localization .....	2321
4.4. Models of dislocation behavior in persistent slip bands .....	2326
4.5. Cyclic hardening in metals other than fcc .....	2333
4.6. Differences and similarities between monotonic and cyclic deformation .....	2336
4.7. Cyclic deformation of polycrystalline metals .....	2338
4.8. Cyclic deformation in alloys .....	2346
4.9. Dislocation patterning in cyclic deformation .....	2361

5. Fatigue crack initiation in ductile metals .....	2362
5.1. Fatigue crack initiation and surface roughness: the phenomena .....	2362
5.2. Fatigue crack initiation in persistent slip bands — mechanisms .....	2369
5.3. Grain-boundary crack initiation .....	2372
5.4. Environmental effects on crack initiation .....	2374
6. Fatigue crack propagation .....	2376
6.1. Macroscopic behavior of fatigue crack propagation .....	2376
6.2. Short crack growth — Stage I growth .....	2381
6.3. Long crack growth — Stage II .....	2385
References .....	2391
Further reading .....	2397
 <i>Chapter 28. Recovery and recrystallization, by R. W. Cahn</i> .....	2399
1. Classification of phenomena and terminology .....	2400
2. Recovery .....	2401
2.1. Recovery of electrical properties .....	2401
2.2. Recovery of stored internal energy .....	2401
2.3. Recovery of mechanical properties .....	2405
2.4. Recovery of microstructure .....	2410
2.4.1. Polygonization and subgrains .....	2410
2.4.2. Cell formation .....	2412
2.4.3. Quantitative theories of the recovery kinetics of yield strength .....	2417
2.4.4. Effect of prior recovery on textures .....	2418
3. Primary recrystallization .....	2419
3.1. Laws of recrystallization .....	2419
3.2. Kinetics of primary recrystallization .....	2421
3.3. Nucleation of primary grains .....	2425
3.4. Growth of primary grains and the role of impurities .....	2440
3.4.1. Impurity drag .....	2440
3.4.2. Special orientations .....	2448
3.4.3. Vacancies in grain boundaries .....	2450
3.5. Recrystallization during hot-working: dynamic recrystallization .....	2453
3.6. Annealing textures .....	2455
3.7. Mesotextures .....	2460
3.8. Primary recrystallization of two-phase alloys .....	2463
3.9. Recrystallization of ordered alloys (intermetallics) .....	2471
4. Grain growth and secondary recrystallization .....	2474
4.1. Mechanism and kinetics of grain growth .....	2474
4.2. Formation of annealing twins .....	2477
4.3. Grain growth in nanostructured materials .....	2479
4.4. Secondary recrystallization .....	2482
4.4.1. General features .....	2482
4.4.2. Surface-controlled secondary recrystallization .....	2487
4.4.3. Thin films .....	2489
4.4.4. Secondary recrystallization and sintering .....	2492
References .....	2492
Further reading .....	2500

<i>Chapter 29. Magnetic properties of metals and alloys, by F. E. Luborsky, J. D. Livingston and G. Y. Chin†</i> .....	2501
1. Origins of fundamental magnetic properties .....	2502
2. Magnetic measurements .....	2507
2.1. Magnetization .....	2507
2.2. Magnetic field .....	2508
2.3. Demagnetizing field .....	2509
2.4. Curie temperature .....	2509
2.5. Magnetic anisotropy .....	2509
2.6. Magnetostriction .....	2510
2.7. Core loss .....	2510
3. Permanent-magnet materials .....	2510
3.1. Reversal mechanisms and coercivity .....	2510
3.2. Microstructure and properties .....	2513
3.3. Shape-anisotropy materials .....	2515
3.3.1. ESD magnets .....	2516
3.3.2. Spinodal alloys .....	2516
3.4. Crystal-anisotropy materials .....	2519
3.4.1. Cobalt–rare earths .....	2519
3.4.2. Iron–rare earths .....	2521
3.4.3. Hard ferrites .....	2522
3.4.4. Mn–Al–C .....	2523
3.4.5. Co–Pt and related alloys .....	2523
4. Soft magnetic materials .....	2524
4.1. Iron and low-carbon steels .....	2525
4.2. Iron–silicon alloys .....	2526
4.2.1. Phase diagram and intrinsic magnetic properties .....	2526
4.2.2. Magnetic permeability .....	2527
4.2.3. Core loss .....	2528
4.2.3.1. Composition .....	2528
4.2.3.2. Impurities .....	2528
4.2.3.3. Grain orientation .....	2528
4.2.3.4. Stress .....	2528
4.2.3.5. Grain size .....	2530
4.2.3.6. Thickness .....	2531
4.2.3.7. Surface morphology .....	2531
4.2.4. Metallurgy of silicon steels .....	2531
4.3. Iron–aluminium and iron–aluminium–silicon alloys .....	2533
4.4. Nickel–iron alloys .....	2534
4.4.1. Phase diagrams and intrinsic magnetic properties .....	2534
4.4.2. Metallurgy of nickel–iron alloys .....	2536
4.4.2.1. High-permeability alloys .....	2536
4.4.2.2. Square-loop alloys .....	2539
4.4.2.3. Skewed-loop alloys .....	2540
4.4.2.4. Wear-resistant alloys .....	2540
4.4.2.5. Invar alloys .....	2540
4.5. Iron–cobalt alloys .....	2541
4.5.1. Metallurgy of equiatomic Fe–Co alloys .....	2541
4.6. Nanocrystalline alloys .....	2542
4.7. Materials for recording heads .....	2543
5. Amorphous magnetic materials .....	2543
5.1. Introduction .....	2543

5.2. Preparation . . . . .	2544
5.3. Properties . . . . .	2546
5.3.1. Curie temperature . . . . .	2546
5.3.2. Saturation magnetization . . . . .	2546
5.3.2.1. Dependence of magnetization on alloy composition . . . . .	2546
5.3.2.2. Temperature-dependence of magnetization and spin waves . . . . .	2549
5.3.3. Anisotropy . . . . .	2551
5.3.3.1. Structural and compositional anisotropy . . . . .	2553
5.3.3.2. Strain-magnetostriction anisotropy . . . . .	2553
5.3.3.3. Directional-order anisotropy . . . . .	2553
5.3.4. Magnetostriction . . . . .	2555
5.3.5. Low-field properties . . . . .	2555
6. Magnetic measurements in metallurgy . . . . .	2558
References . . . . .	2560
Further reading . . . . .	2564
 <i>Chapter 30. Metallic composite materials, by T. W. Clyne . . . . .</i>	2567
1. Introduction . . . . .	2568
2. Material production . . . . .	2569
2.1. Liquid-phase processing . . . . .	2569
2.1.1. Squeeze infiltration . . . . .	2569
2.1.2. Stir casting . . . . .	2571
2.1.3. Spray deposition . . . . .	2574
2.1.4. Reactive processing . . . . .	2576
2.2. Solid-state processing . . . . .	2577
2.2.1. Powder blending and consolidation . . . . .	2577
2.2.2. Diffusion bonding of foils . . . . .	2579
2.2.3. Physical vapour deposition (PVD) . . . . .	2581
3. Deformation behaviour . . . . .	2581
3.1. Elastic properties . . . . .	2581
3.2. Yielding and work hardening . . . . .	2584
3.2.1. Matrix flow . . . . .	2584
3.2.2. Thermal stresses . . . . .	2589
3.2.3. Work hardening and stress relaxation . . . . .	2592
3.3. Wear . . . . .	2595
4. Fracture . . . . .	2596
4.1. Damage development and ductility . . . . .	2598
4.1.1. Damage mechanisms . . . . .	2598
4.1.2. Ductility . . . . .	2601
4.2. Fracture toughness and fatigue . . . . .	2604
4.2.1. Fracture toughness . . . . .	2604
4.2.2. Fatigue of discontinuous composites . . . . .	2606
4.2.3. Fatigue of long fibre and layered composites . . . . .	2607
5. High temperature behaviour . . . . .	2609
5.1. Thermal expansion and thermal stresses . . . . .	2609
5.2. Creep and thermal cycling effects . . . . .	2611
References . . . . .	2616

<i>Chapter 31. Sintering processes, H. E. Exner and E. Arzt . . . . .</i>	2627
1. Solid-state sintering . . . . .	2628
1.1. Driving energy . . . . .	2630
1.2. Material sinks and sources . . . . .	2632
1.3. Neck growth and center approach in two-particle models . . . . .	2634
1.4. Shrinkage of particle arrays and powder compacts . . . . .	2637
1.5. Factors accelerating or retarding shrinkage . . . . .	2640
1.6. Development of microstructure and grain growth . . . . .	2643
2. Hot pressing (pressure-sintering) . . . . .	2645
2.1. Stresses and mechanisms . . . . .	2645
2.2. Densification models . . . . .	2646
2.3. HIP (hot isostatic pressing) maps . . . . .	2648
2.4. Technological considerations . . . . .	2649
3. Sintering with a liquid phase . . . . .	2651
4. Outlook . . . . .	2654
References . . . . .	2654
Further reading . . . . .	2660
<i>Chapter 32. A metallurgist's guide to polymers, by A. H. Windle . . . . .</i>	2663
Preface . . . . .	2664
1. Introduction to synthetic polymers . . . . .	2665
1.1. Thermosets (network polymers) . . . . .	2665
1.2. Thermoplastics: (a) Non-crystalline polymers . . . . .	2665
1.3. Thermoplastics: (b) Semi-crystalline polymers . . . . .	2666
1.4. Thermoplastics: (c) Liquid crystalline polymers . . . . .	2667
1.5. Naming of plastics . . . . .	2668
2. Crystal morphology of polymers and the concept of crystallinity . . . . .	2668
2.1. Crystalline or non-crystalline? . . . . .	2668
2.2. Crystallinity . . . . .	2670
2.3. Chain folding . . . . .	2670
2.4. Annealing . . . . .	2671
2.5. Special cases . . . . .	2672
2.6. Spherulites . . . . .	2673
3. Textures . . . . .	2675
3.1. Wire textures in metals — an overview . . . . .	2675
3.2. Fiber textures in polymers . . . . .	2676
3.3. Alignment of non-crystalline polymers . . . . .	2677
3.4. A parameter to describe the quality of fiber texture . . . . .	2679
3.5. Rolling textures . . . . .	2680
4. Polymer alloys: phase diagrams in macromolecular systems . . . . .	2682
4.1. General . . . . .	2682
4.2. Entropy and enthalpy of mixing . . . . .	2683
4.3. The Flory–Huggins equation . . . . .	2684
4.4. Polymer–polymer miscibility . . . . .	2684
4.5. Copolymers . . . . .	2689
5. Plastic deformation and yielding . . . . .	2692
5.1. Metals and polymers . . . . .	2692
5.2. True stress–strain relations . . . . .	2694

5.3. Considère's criterion .....	2694
5.4. Yield drops and Lüders bands .....	2695
5.5. Drawing of polymers .....	2697
5.6. Structural control of the natural draw ratio .....	2698
5.7. Yield criteria .....	2698
6. High-performance polymer fibers .....	2700
6.1. Diamond — the ultimate polymer? .....	2700
6.2. Theoretical axial modulus of polymer crystals .....	2700
6.3. Axial properties of conventionally drawn fibers .....	2703
6.4. Making high-performance fibers .....	2705
6.5. The Achilles' heel and the diamond challenge .....	2706
7. Crazing .....	2707
7.1. Introduction to a craze .....	2707
7.2. Craze criteria .....	2707
7.3. Materials factors .....	2710
7.4. Microstructure and micromechanisms .....	2710
7.5. Multiply induced crazing .....	2713
8. Electrically conducting polymers .....	2713
8.1. Conjugated polymers .....	2713
8.2. Band structure .....	2714
8.3. Solitons .....	2715
8.4. Polarons .....	2717
8.5. Materials .....	2718
8.6. Applications .....	2718
9. The glass transition: to melt and rubber .....	2720
9.1. Formation of a polymer glass .....	2720
9.2. Rate effects .....	2721
9.3. Observation of the glass transition using differential scanning calorimetry (DSC) .....	2722
9.4. Control of the glass transition temperature ( $T_g$ ) .....	2724
9.5. Melt or rubber? .....	2725
9.6. Viscoelasticity .....	2726
9.7. Model description of non-crystalline polymers .....	2729
10. Amorphous chain structures .....	2730
10.1. Simple statistical chains .....	2730
10.2. Real chains .....	2731
10.3. The Gaussian approximation .....	2732
10.4. The chain environment .....	2733
10.5. The condensed phase .....	2734
11. Rubber elasticity .....	2735
11.1. The network .....	2735
11.2. The entropy spring .....	2736
11.3. Thermodynamics .....	2736
11.4. Dependence of entropy on strain .....	2737
11.5. The stress-strain curve .....	2738
11.6. The high-strain discrepancy .....	2739
11.7. Summary .....	2740
References .....	2740
Author index .....	A1
Subject index .....	S1



## CHAPTER 1

# CRYSTAL STRUCTURE OF THE METALLIC ELEMENTS

W. STEURER

*Institute of Crystallography  
ETH-Zentrum  
CH-8092 Zürich, Switzerland*

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## 1. Introduction

In the very beginning of materials “science”, when men began to produce artificial materials, it was the time of trial and error, of pure empiricism. Today, we are a little closer to the realization of the old dream of designing any material with given properties owing to our improved understanding of the relationships between chemical composition, crystal structure and material properties. Though only a very few commercially and technologically important materials consist of metallic elements in their pure form (Si, Ge, Cu, Au, Ag, Pd, etc.), their crystal structures are of more than academic interest. Thus, to give an example, the crystal structure of a pure metal remains unchanged in the case of a solid solution, when one or several other components are added to tune the properties of a material. This technique has been used since time immemorial by alloying gold with copper or silver, for instance, to make jewelry or coins more resistant to wear. Especially the close packed structures and their derivatives, which are typical for pure metals, are also characteristic for numerous materials consisting of multi-component solid solutions or intermetallic alloys. Another reason for the study of “simple” element structures is that they are extremely helpful for the development and improvement of methods to understand why a given phase is adopting a particular crystal structure under certain conditions (temperature, pressure, etc.). The aim is, of course, to learn to predict the crystal structure of any given chemical compound under any ambient conditions and to model its possible phase transformations.

It is remarkable that even pure elements can have rather complicated crystal structures resulting from complex electronic interactions. Most elements are polymorphous, i.e., they occur in up to ten different crystal structures as a function of ambient conditions (temperature, pressure). The understanding of the phase transformations in these homatomic cases is also very helpful for understanding the more complicated phase transformations of complex intermetallic phases. Indeed, it is possible today to predict correctly most of the element structures and phase transformations by one-electron theory (SKRIVER [1985]).

## 2. Factors governing a crystal structure

Crystalline order, i.e., the three-dimensional (or in the case of quasicrystals or incommensurate phases, higher-dimensional) translationally periodic repetition of a particular atomic configuration, is the outstanding characteristic of condensed matter in thermodynamic equilibrium. Which crystal structure for a given chemical composition corresponds to the lowest Gibbs free energy,  $G = H - TS$ , depends on chemical bonding, electronic band structure and geometrical factors. Since it is not possible to solve the Schrödinger equation for a crystal and thus deduce the correct crystal structure, many approximations have been developed. Indeed, today there exist quite successful attempts to predict simpler crystal structures using one-electron approximations: the many-electron problem is reduced to a one-electron problem by the assumption that the electrons, surrounded by a mutual exclusion zone, are moving independently of each other in the

average field of all the others (local density functional theory).

 Beside this rather complicated and lengthy approach to understand and predict crystal structures, there exist a number of rules based on two factors: the chemical bond factor, which also takes into account the directionality of chemical bonds, and the geometrical factor, which considers optimum space filling, symmetry and connectivity. Especially in the case of the typical metallic elements, these structural principles work very well for predicting structures. (For electron theory of structural stability, see ch. 2, § 6.1).

## 2.1. Chemical bond factor

 The concept of chemical bonding was originally developed to understand the formation of molecules. In a crystal, a collective interaction of all atoms always exists which may approximately be considered as the sum of nearest-neighbor interactions. A further simplification comes in by the fact that only the electrons of the outer shells contribute to the chemical bonding. Traditionally, several limiting types of the chemical bond are defined: strong ionic (heteropolar), covalent (homopolar), metallic bonds, and weak van der Waals and hydrogen bonds. The strong bonds have in common that the outer atomic orbitals contribute to new collective electron states in the crystal, the electron bands. They differ mainly in the degree of localization of the valence electrons: when these are transferred from one atom to another atom, Coulomb attraction between the cation and the anion results and the bond is called *ionic*; when they remain localized between two atoms the so-called exchange interaction results from overlapping orbitals and *covalent* bonds are formed; when the valence electrons are delocalized over the whole crystal *metallic bonding* is obtained. Thus, contrary to the other bond types which also occur within molecules, the metallic bond can only exist in large arrays of atoms. Since the interaction of electron orbitals depends on their separation and mutual orientation, the bond type may change during phase transformations. Sometimes, a slight change in temperature can be sufficient, as in the transition from metallic white tin to non-metallic grey tin below 291K ("tin pest"); sometimes very high pressures are necessary, as for the transformation from molecular hydrogen to metallic hydrogen, for instance.

 The type of bonding occurring in crystals of the metallic elements ranges from pure metallic in the alkali metals to increasingly covalent for zinc or cadmium, for instance. The structural implications of these two bond types, which are just two contrary limiting manifestations of electronic interactions with a continuously changing degree of electron localization, will be characterized in the following in greater detail.

### 2.1.1. The covalent bond

 The covalent bond may be described in terms of the more qualitative VB (valence bond) theory by overlapping atomic orbitals occupied by unpaired valence electrons (fig. 1). Its strength depends on the degree of overlapping and is given by the exchange integral. In terms of the more quantitative LCAO-MO (linear combination of atomic orbitals – molecular orbitals) theory, molecular orbitals are constructed by linear combination of atomic orbitals (fig. 2). The resulting bonding, non-bonding and anti-

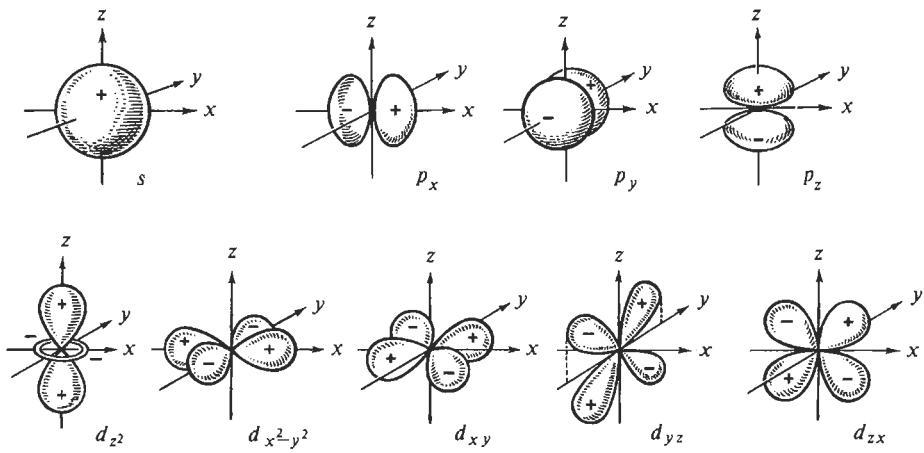


Fig. 1. Schematic structure of the atomic s-, p- and d-orbitals (from VAINSHTEIN *et al.* [1982]).

bonding molecular orbitals, filled up with valence electrons according to the Pauli exclusion principle, are localized between the bonding atoms with well defined geometry. Generally, covalent bonds can be characterized as strong, directional bonds. Increasing the number of atoms contributing to the bonds increases the number of molecular orbitals and their energy differences become smaller and smaller. Finally, the discrete energy levels of the molecular orbitals condense to quasicontinuous bands separated by energy gaps. Since in a covalent bond each atom reaches its particular stable noble gas configuration (filled shell) the energy bands are either completely filled or empty. Owing to the localization of the electrons, it needs much energy to lift them from the last filled valence band into the empty conduction band. The classic example of a crystal built from only covalently bonded atoms is diamond: all carbon atoms are bonded via tetrahedrally directed  $sp^3$  hybrid orbitals (fig. 3). Thus the crystal structure of diamond results as a framework of tetrahedrally coordinated carbon atoms (fig. 4).

### 2.1.2. The metallic bond

The metallic bond can be described in a similar way as the covalent bond. The main difference between these two bond types is that the ionization energy for electrons occupying the outer orbitals of the metallic elements is much smaller. In typical metals, like the alkali metals, these outer orbitals are spherical  $s$ -orbitals allowing overlapping with up to 12 further  $s$ -orbitals of the surrounding atoms. Thus, the well-defined electron localization in bonds connecting pairs of atoms with each other loses its meaning. Quantum-mechanical calculations show that in large agglomerations of metal atoms the delocalized bonding electrons occupy lower energy levels than in the free atoms; this would not be true for isolated "metal molecules". The metallic bond in typical metals is non-directional, favoring structures corresponding to closest packings of spheres. With increasing localization of valence electrons, covalent interactions cause deviations from spherically symmetric bonding, leading to more complicated structures.

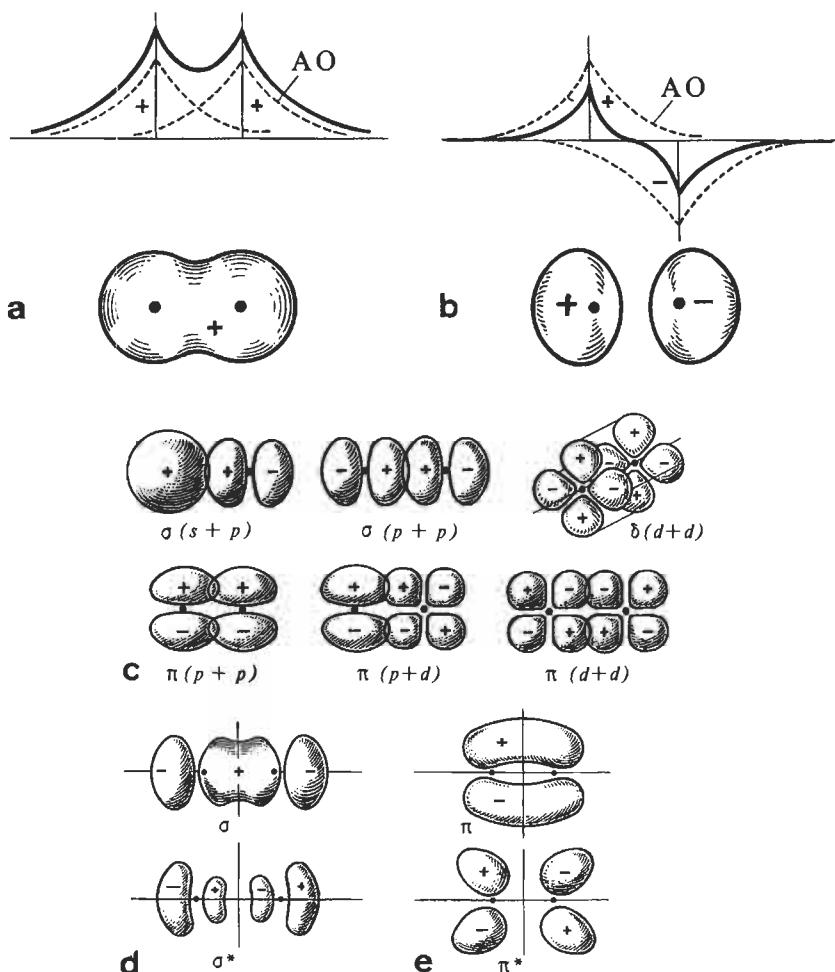


Fig. 2. (a) Bonding and (b) anti-bonding molecular orbitals of the  $\text{H}_2$  molecule. (c) Schematic drawing of the building of the most important molecular orbitals from atomic orbitals and (d), (e) examples of molecular orbitals (bonding:  $\sigma$ ,  $\pi$  and anti-bonding  $\sigma^*$ ,  $\pi^*$ ) (from VAINSHTEIN *et al.* [1982]).

## 2.2. Geometrical factors

 A crystal structure type is fully defined by its general chemical composition, its space group symmetry, the equipoint (Wyckoff) positions occupied by the atoms and the coordinates of the atoms in the unit cell (fig. 5). The metrics, i.e., the dimension of the unit cell (lattice parameters), in general differ for all chemical compounds or phases occurring in one particular crystal structure type. Also, for general Wyckoff positions, the numerical values of the coordinates may vary in a range not destroying the characteris-

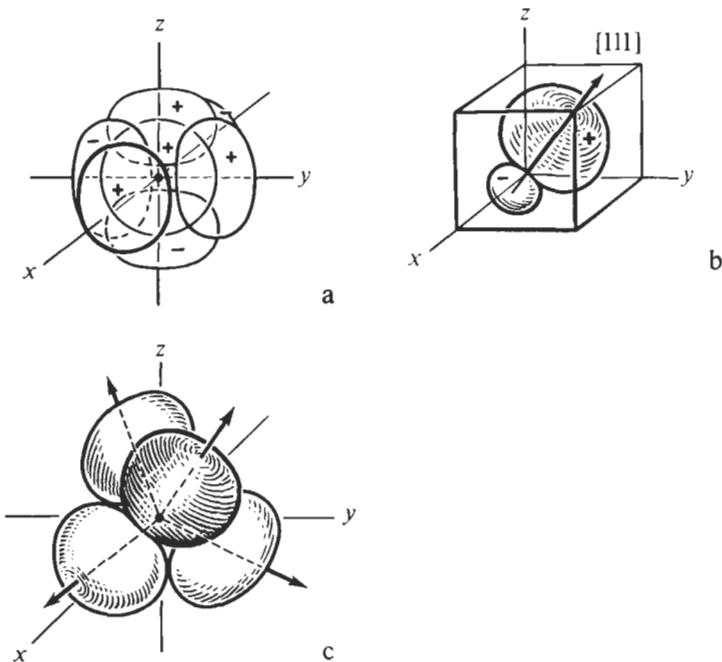


Fig. 3. Hybridization of (a) one s- and three p-orbitals to (b)  $sp^3$ -hybrid orbitals (c) which are directed along tetrahedron axes (from VAINSHTEIN *et al.* [1982]).

tics, i.e., coordination polyhedra and their linkings, of this crystal structure. With these data given it is easy to derive both the information about the global arrangement of structural units as well as the local environment of each atom (fig. 6). Besides this purely geometrical description of a structure, it is necessary to understand the characteristics of a crystal structure by identifying crystal-chemically meaningful structural units (coordination polyhedra) and their connecting principles (bonding).



For band-structure calculations, for instance, knowledge of the full crystal structure

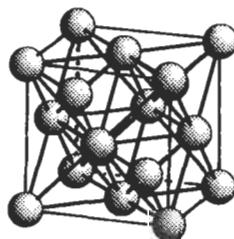


Fig. 4. The structure of diamond cF8-C, space group  $Fd\bar{3}m$ , No. 227, 8a: 0 0 0,  $\frac{1}{4} \frac{1}{4} \frac{1}{4}$ . All carbon atoms are tetrahedrally coordinated, they occupy the positions of a face-centered cubic lattice and one half of the centers of the eighth cubes.

is essential; for tensorial physical properties, however, the point symmetry group to which the space group belongs is the determining factor. Crystal-chemical properties are less sensitive to slight atomic shifts which may break the symmetry but do not change local environments of atoms. Thus the study of atomic coordinations may yield valuable tools in the analysis, description and comparison of crystal structures.

### 2.2.1. Coordination

 A general technique to derive useful coordination polyhedra was suggested by BRUNNER and SCHWARZENBACH [1971]: all interatomic distances around a particular atom are calculated up to a certain limit, and all atoms within a distance defined by the first maximum gap in a histogram of distances belong to the coordination polyhedron (fig. 6). If there is no clear maximum gap observable, a second criterion may be the maximum-convex-volume rule: all coordinating atoms lying at the intersections of at least three faces should form a convex polyhedron (DAAMS *et al.* [1992]).

### 2.2.2. Space filling

 Owing to the isotropic properties of the metallic bond the structure of typical metallic elements can often be described in terms of dense sphere packings. A sphere packing is an infinite set of non-interpenetrating spheres with the property that any pair of spheres is connected by a chain of spheres with mutual contact. A sphere packing is called homogenous if all spheres are symmetrically equivalent, otherwise it is called heterogenous (KOCH and FISCHER [1992]). In the last named case, the spheres of the different non-symmetrically equivalent subsets may have different radii and occupy the positions of different crystallographic orbits. The number of types of heterogenous sphere packings is infinite whereas it is finite for homogenous sphere packing types. There are, for instance, 199 different cubic and 394 different possible tetragonal homogenous sphere packings. The densities, i.e., the fractions of volumes occupied by the spheres, are with  $q=0.7405$  highest for the well-known hexagonal closest packing (hcp) and cubic closest packing (ccp) (figs. 7 and 8, respectively). In both cases the coordination numbers (CN) are twelve and the distances to the nearest neighbors the same. The number  $k$  of contacts per sphere amounts to  $3 \leq k \leq 12$ . Table 1 gives some examples for sphere packings with the highest and lowest densities and contact numbers, and table 2 space filling values for a number of structure types. Very low packing densities, such as that for the cF8–C type, for instance, indicate that a hard sphere packing is no longer an adequate description of such a structure.

 The crystal structures of the metallic elements adopt dense sphere packings as long as purely geometrical packing principles are dominant. Covalent bonding contributions and electronic effects give rise to more complicated structures.

### 2.2.3. Layer stackings, polytypism

 Many crystal structures can be considered to consist of successive stackings of atomic layers. The above mentioned hexagonal closest packing (hcp) refers to a stacking of dense packed layers with periodic sequence ..AB.., the cubic closest packing (ccp) to a sequence ..ABC.. (figs. 7 and 8). The atomic layers are denoted by A, B or C depending

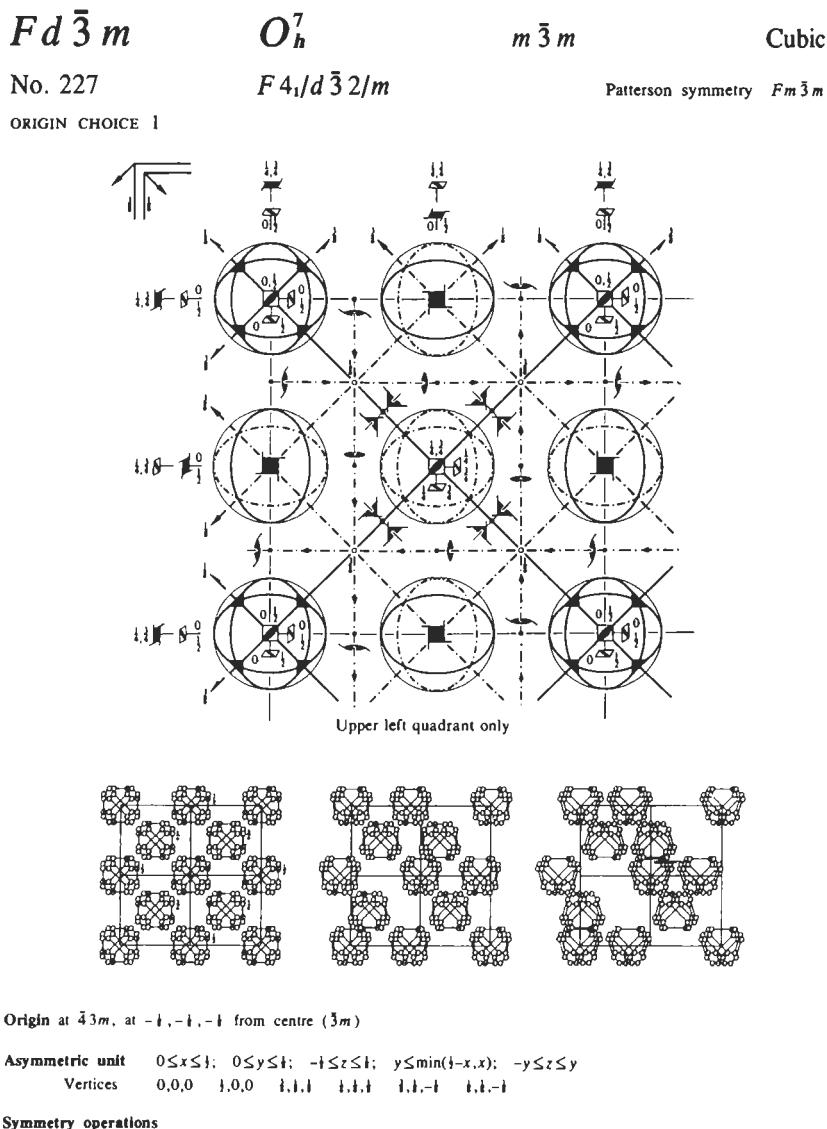


Fig. 5. Information given in the *International Tables for Crystallography* (HAHN [1992]) on the example of the space group  $Fd\bar{3}m$  of the diamond structure. Left side, top line: space group symbol in short Hermann-Mauguin and Schoenflies notation, point group (crystal class), crystal system. Second line: consecutive space group number, full space group symbol, Patterson symmetry, short space group symbol. Upper drawing: framework of symmetry elements in a unique part of one unit cell. Lower drawings: point complexes generated by the action of symmetry operations. Below: choice of origin, definition of the asymmetric unit. Right side: the Wyckoff letters a, b, c ... i denote the equipoint positions with multiplicities 8, 8, 16 ... 192. The positions of the carbon atoms in the diamond structure are given in Wyckoff position 8a.

No. 227

Fd $\bar{3}m$ 

**Generators selected** (1);  $t(1,0,0)$ ;  $t(0,1,0)$ ;  $t(0,0,1)$ ;  $t(0,\frac{1}{2},\frac{1}{2})$ ;  $t(\frac{1}{2},0,\frac{1}{2})$ ; (2); (3); (5); (13); (25)

**Positions**

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions		
	(0,0,0)+	(0,1,1)+	(1,0,1)+	(1,1,0)+	$h,k,l$ permutable General:		
192 $i$ . 1	(1) $x,y,z$ (5) $z,x,y$ (9) $y,z,x$ (13) $y-\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ (17) $x-\frac{1}{2},z+\frac{1}{2},y+\frac{1}{2}$ (21) $x+\frac{1}{2},y+\frac{1}{2},z+\frac{1}{2}$ (25) $x+\frac{1}{2},y+\frac{1}{2},z+\frac{1}{2}$ (29) $x+\frac{1}{2},x+\frac{1}{2},y+\frac{1}{2}$ (33) $y-\frac{1}{2},z+\frac{1}{2},x+\frac{1}{2}$ (37) $y-\frac{1}{2},x,z+\frac{1}{2}$ (41) $x-\frac{1}{2},z,y+\frac{1}{2}$ (45) $z+\frac{1}{2},y,x+\frac{1}{2}$	(2) $\bar{x},\bar{y}+\frac{1}{2},z+\frac{1}{2}$ (6) $z+\frac{1}{2},\bar{x},\bar{y}+\frac{1}{2}$ (10) $\bar{y}+\frac{1}{2},z+\frac{1}{2},x$ (14) $\bar{y}+\frac{1}{2},\bar{x}+\frac{1}{2},z+\frac{1}{2}$ (18) $\bar{x}+\frac{1}{2},z+\frac{1}{2},y+\frac{1}{2}$ (22) $z+\frac{1}{2},\bar{y}+\frac{1}{2},x+\frac{1}{2}$ (26) $x+\frac{1}{2},y+\frac{1}{2},z+\frac{1}{2}$ (30) $\bar{z}+\frac{1}{2},x+\frac{1}{2},y+\frac{1}{2}$ (34) $y+\frac{1}{2},z+\frac{1}{2},x+\frac{1}{2}$ (38) $y,x,z$ (42) $x+\frac{1}{2},z+\frac{1}{2},y$ (46) $\bar{z},y+\frac{1}{2},\bar{x}+\frac{1}{2}$	(3) $\bar{x}+\frac{1}{2},y+\frac{1}{2},z$ (7) $\bar{z},\bar{x}+\frac{1}{2},y+\frac{1}{2}$ (11) $y+\frac{1}{2},\bar{z},\bar{x}+\frac{1}{2}$ (15) $y+\frac{1}{2},z+\frac{1}{2},z+\frac{1}{2}$ (19) $\bar{x}+\frac{1}{2},z+\frac{1}{2},\bar{y}+\frac{1}{2}$ (23) $\bar{z}+\frac{1}{2},y+\frac{1}{2},x+\frac{1}{2}$ (27) $x+\frac{1}{2},\bar{y}+\frac{1}{2},z+\frac{1}{2}$ (31) $z+\frac{1}{2},x+\frac{1}{2},y+\frac{1}{2}$ (35) $\bar{y}+\frac{1}{2},z+\frac{1}{2},x+\frac{1}{2}$ (39) $\bar{y},x+\frac{1}{2},z+\frac{1}{2}$ (43) $x,z,y$ (47) $z+\frac{1}{2},\bar{y}+\frac{1}{2},\bar{x}$	(4) $x+\frac{1}{2},\bar{y},z+\frac{1}{2}$ (8) $\bar{z}+\frac{1}{2},x+\frac{1}{2},\bar{y}$ (12) $\bar{y},\bar{z}+\frac{1}{2},x+\frac{1}{2}$ (16) $\bar{y}+\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ (20) $x+\frac{1}{2},z+\frac{1}{2},y+\frac{1}{2}$ (24) $\bar{z}+\frac{1}{2},y+\frac{1}{2},\bar{x}+\frac{1}{2}$ (28) $\bar{x}+\frac{1}{2},y+\frac{1}{2},z+\frac{1}{2}$ (32) $z+\frac{1}{2},x+\frac{1}{2},y+\frac{1}{2}$ (36) $y+\frac{1}{2},z+\frac{1}{2},\bar{x}+\frac{1}{2}$ (40) $y+\frac{1}{2},x+\frac{1}{2},z$ (44) $\bar{x},z+\frac{1}{2},y+\frac{1}{2}$ (48) $z,y,x$	$hkl : h+k=2n$ and $h+l,k+l=2n$ $0kl : k+l=4n$ and $k,l=2n$ $hh\bar{l} : h+l=2n$ $h00 : h=4n$		
96 $h$ . . 2	$\frac{1}{2},y,\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{1}{2},y$ $y,\bar{y}+\frac{1}{2},\frac{1}{2}$ $\frac{1}{2},\bar{y}+\frac{1}{2},y$ $y,\frac{1}{2},\bar{y}+\frac{1}{2}$	$\frac{1}{2},y+\frac{1}{2},\bar{y}+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{1}{2},\bar{y}+\frac{1}{2}$ $y+\frac{1}{2},y+\frac{1}{2},\frac{1}{2}$ $\frac{1}{2},y+\frac{1}{2},y+\frac{1}{2}$ $y+\frac{1}{2},\frac{1}{2},y+\frac{1}{2}$	$\frac{1}{2},y+\frac{1}{2},y+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{1}{2},\bar{y}+\frac{1}{2}$ $y+\frac{1}{2},y+\frac{1}{2},\frac{1}{2}$ $\frac{1}{2},y+\frac{1}{2},y+\frac{1}{2}$ $y+\frac{1}{2},\frac{1}{2},y+\frac{1}{2}$	$\frac{1}{2},\bar{y},y+\frac{1}{2}$ $\bar{y}+\frac{1}{2},\frac{1}{2},\bar{y}$ $y+\frac{1}{2},\bar{y},\frac{1}{2}$ $\frac{1}{2},\bar{y},y+\frac{1}{2}$ $y+\frac{1}{2},\bar{y},\frac{1}{2}$	Special: as above, plus no extra conditions		
96 $g$ . . $m$	$x,x,z$ $z,x,x$ $x,z,x$ $x+\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ $x+\frac{1}{2},z+\frac{1}{2},x+\frac{1}{2}$ $z+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$	$\bar{x},\bar{x}+\frac{1}{2},z+\frac{1}{2}$ $\bar{z},\bar{x}+\frac{1}{2},x+\frac{1}{2}$ $x+\frac{1}{2},\bar{x},\bar{x}+\frac{1}{2}$ $\bar{x}+\frac{1}{2},\bar{x}+\frac{1}{2},z+\frac{1}{2}$ $\bar{x}+\frac{1}{2},z+\frac{1}{2},\bar{x}+\frac{1}{2}$ $z+\frac{1}{2},\bar{x}+\frac{1}{2},x+\frac{1}{2}$	$\bar{x}+\frac{1}{2},x+\frac{1}{2},\bar{z}$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$ $\bar{x},\bar{x}+\frac{1}{2},x+\frac{1}{2}$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ $\bar{x}+\frac{1}{2},z+\frac{1}{2},\bar{x}+\frac{1}{2}$ $z+\frac{1}{2},\bar{x}+\frac{1}{2},x+\frac{1}{2}$	$x+\frac{1}{2},\bar{x},\bar{z}+\frac{1}{2}$ $\bar{z}+\frac{1}{2},x+\frac{1}{2},\bar{x}$ $\bar{x},\bar{x}+\frac{1}{2},x+\frac{1}{2}$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},z+\frac{1}{2}$ $\bar{x}+\frac{1}{2},z+\frac{1}{2},x+\frac{1}{2}$ $z+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$	no extra conditions		
48 $f$ . $2mm$	$x,0,0$ $\frac{1}{2},x+\frac{1}{2},\frac{1}{2}$	$\bar{x},\frac{1}{2},\frac{1}{2}$ $\frac{1}{2},\bar{x}+\frac{1}{2},\frac{1}{2}$	$0,x,0$ $x+\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\bar{x},\frac{1}{2}$ $\bar{x}+\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$0,0,x$ $\frac{1}{2},\frac{1}{2},\bar{x}+\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\bar{x}$ $\frac{1}{2},\frac{1}{2},x+\frac{1}{2}$	$hkl : h=2n+1$ or $h+k+l=4n$
32 $e$ . $3m$	$x,x,x$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},x$ $x+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$ $x+\frac{1}{2},\bar{x}+\frac{1}{2},x+\frac{1}{2}$	$\bar{x},\bar{x}+\frac{1}{2},x+\frac{1}{2}$ $x+\frac{1}{2},\bar{x},\bar{x}+\frac{1}{2}$ $\bar{x}+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$ $x+\frac{1}{2},x+\frac{1}{2},x+\frac{1}{2}$				no extra conditions	
16 $d$ . $\bar{3}m$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$		$hkl : h=2n+1$ or $h,k,l=4n+2$	
16 $c$ . $\bar{3}m$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$		or $h,k,l=4n$	
8 $b$ . $\bar{3}m$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$				$hkl : h=2n+1$	
8 $a$ . $\bar{3}m$	0,0,0	$\frac{1}{2},\frac{1}{2},\frac{1}{2}$				or $h+k+l=4n$	

**Symmetry of special projections**

Along [001]  $p4mm$   
 $\mathbf{a}' = \frac{1}{2}(\mathbf{a}-\mathbf{b})$     $\mathbf{b}' = \frac{1}{2}(\mathbf{a}+\mathbf{b})$   
Origin at  $0,0,z$

Along [111]  $p6mm$   
 $\mathbf{a}' = \frac{1}{2}(2\mathbf{a}-\mathbf{b}-\mathbf{c})$     $\mathbf{b}' = \frac{1}{2}(-\mathbf{a}+2\mathbf{b}-\mathbf{c})$   
Origin at  $x,x,x$

Along [110]  $c2mm$   
 $\mathbf{a}' = \frac{1}{2}(-\mathbf{a}+\mathbf{b})$     $\mathbf{b}' = \mathbf{c}$   
Origin at  $x,x,\frac{1}{2}$

Table 1  
Examples of homogeneous sphere packings with distance  $d$  between neighboring spheres, highest and lowest contact numbers,  $k$ , and fractional packing densities,  $q$ .

$k$	Space Group Wyckoff position	Parameters	Distance $d$	Density $q$
12	P6 <sub>3</sub> /mmc 2c ½ ¾ ¼	$c/a = \frac{2}{3}\sqrt{6} = 1.633$	a	0.7405
12	Fm̄3m 4a 0 0 0		$\frac{1}{2}\sqrt{2}$ a	0.7405
11	C2/m 4i x 0 z	$x = \frac{1}{2}(\sqrt{2} - 1)$ $z = 3\sqrt{2} - 4b/a = \frac{1}{3}\sqrt{3}$ $c/a = \frac{1}{6}\sqrt{6} + \frac{1}{3}\sqrt{3} = 0.986$ $\cos \beta = \frac{1}{6}\sqrt{6} - \frac{1}{3}\sqrt{3}$	b	0.7187
10	I4/mmm 2a 0 0 0	$c/a = \frac{1}{3}\sqrt{6} = 0.8165$	c	0.6981
3	I4 <sub>1</sub> 32 24h ½ y ¼ y	$y = \frac{1}{4}\sqrt{3} - \frac{3}{8}$	$(\frac{1}{2}\sqrt{6} - \frac{3}{4}\sqrt{2})a$	0.0555

on their relative position against each other. The packing fractions as well as the coordination numbers ( $CN = 12$ ) are equal in both cases. The first shell atomic environment corresponds to a cuboctahedron for ccp and to a disheptahedron for hcp. The distribution of atomic distances becomes different not until the third and higher coordination shells (fig. 9).

 These two types of layer stackings are not the only possible ones, there exist infinitely many with exactly the same coordination numbers and packing fractions. They are called *polytypes*. Examples for such layer structures occurring for metallic elements are cobalt (..ABABABABCBCBC..), with one ccp sequence ABC statistically occurring among about ten hcp sequences, ordered hP4-La (..ACAB..) or hR3-Sm (..ABABCBCAC..) (fig. 10).

#### 2.2.4. Polymorphism

 Most of the elements adopt several different (allotropic) crystal structures at different pressures, temperatures or external fields. The transitions from one modification to the other are called polymorphous transformations or phase transitions.

 A phase transition is connected with a change in structural parameters and/or in the ordering of electron spins. There are two basically different types of phase transitions: first-order transitions which are correlated with a jumpwise change in the first-order

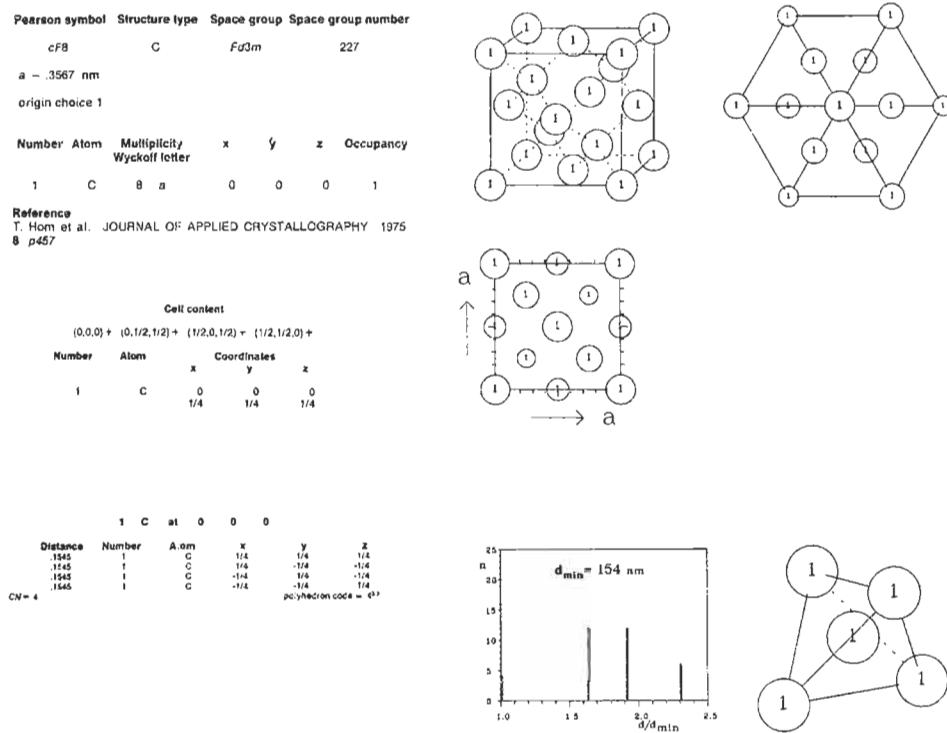


Fig. 6. Information given in the *Atlas of Crystal Structure Types for Intermetallic Phases* (DAAMS et al. [1991]) on the example of the diamond structure type. Beside numerical information and an atomic distances histogram, drawings of the crystal structure and characteristic coordination polyhedra in different projections are also shown.

derivatives of the Gibbs free energy  $G = H - TS$  (i.e., volume, entropy, ...), and second-order transitions which show a jump in the second derivatives of the Gibbs free energy (with respect to heat capacity, compressibility, etc.). In both types of phase transitions the crystal structure changes discontinuously at the transition point: in a first-order transition, in general no symmetry relationship exists between the two modifications; in a second-order transition, a group/subgroup relationship can always be found for the symmetry groups of the two polymorphous crystals structures.

With regard to structural changes resulting from a phase transformation of any order it is useful to distinguish between several different types: reconstructive phase transitions with essential changes in coordination numbers, atomic positions ( $\alpha$ -Fe and  $\gamma$ -Fe, for instance, with coordination numbers CN = 8 and CN = 12, respectively, fig. 11) and sometimes also in chemical bonding (grey  $\alpha$ -Sn and white  $\beta$ -Sn, for instance, with minimum distances changing from  $d_{\min}^{\alpha\text{-Sn}} = 1.54 \text{ \AA}$  to  $d_{\min}^{\beta\text{-Sn}} = 3.02 \text{ \AA}$ ). These transformations are always of first order. Displacive phase transitions with small atomic shifts not changing the first coordination shells may change the lattice by small atomic displacements (martensitic diffusionless lattice rearrangement). Order/disorder transitions are related to the long-range ordered or disordered arrangement of structure elements (copper-gold system, for instance).

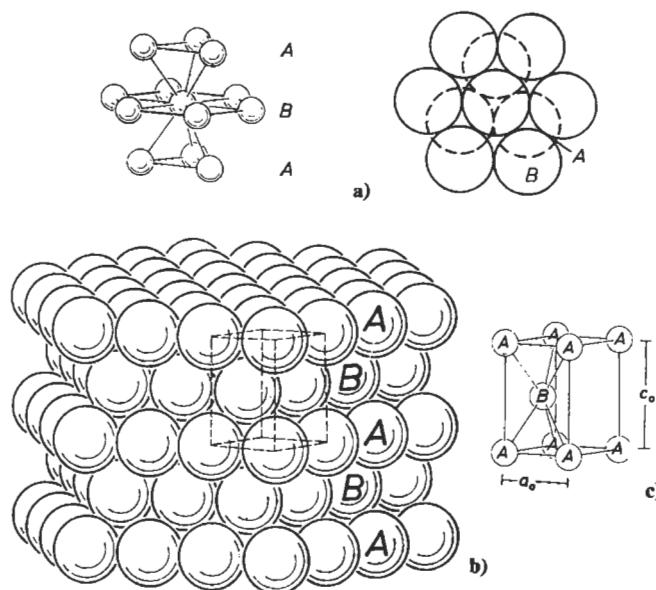


Fig. 7. Characteristics of the hexagonal closest-sphere packing. (a) The coordination polyhedron (disheptahedron) in perspective view and projected to show the packing principle, (b) the crystal structure and (c) one unit cell with atoms marked according to their belonging to layer A or B, are depicted (from BORCHARDT-OTT [1993]).

Table 2  
Fractional packing densities  $q$  of elemental structures (PEARSON [1972]).

Element	Structure Type, $c/a$	Space filling value $q$	Element	Structure Type, $c/a$	Space filling value $q$
Cu	cF4	0.740	Po	cP1	0.523
Mg	hP2, 1.63	0.740	Bi	hR2, 2.60	0.446
Zn	hP2, 1.86	0.650	Sb	hR2, 2.62	0.410
Pa	tI2	0.696	As	hR2, 2.80	0.385
In	tI2	0.686	Ga	oC8	0.391
W	cI2	0.680	Te	hP3	0.364
Hg	hR1	0.609	C (diamond)	cF8	0.340
Sn	tI4	0.535	P (black)	oC8	0.285
$\alpha$ -U	oC4	0.534			

### 3. Crystal structure of metallic elements

In the following, the crystal structures of all metallic and semi-metallic elements (table 3) will be discussed. If it is not indicated specifically, the crystal structure data

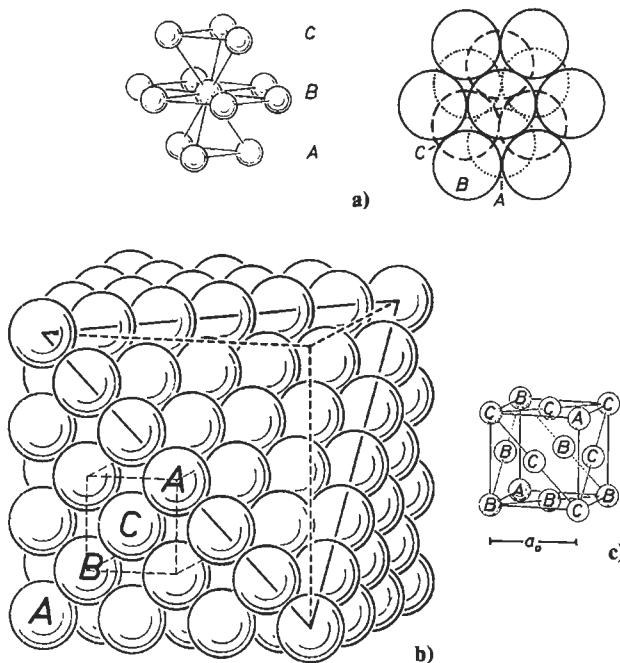


Fig. 8. Characteristics of the cubic closest-sphere packing. (a) The coordination polyhedron (cubooctahedron) in perspective view and projected to show the packing principle, (b) the crystal structure and (c) one unit cell with atoms marked according to their belonging to layer A, B or C, are depicted (from BORCHARDT-OTT [1993]).

have been taken from VILLARS and CALVERT [1991], YOUNG [1991] or MASSALSKI [1990]. In the (not so rare) cases of contradictory data, the most recent and reliable (?) ones have been used or the Pearson symbol has been replaced by a question mark. Particularly the structural information given for the high-pressure phases, which in most cases are derived from very small data sets, may be revised in future once better diffraction data become available.

### 3.1. Nomenclature

 For the short-hand characterization of crystal structures, the Pearson notation in combination with the prototype formula defining the structure type is used throughout the paper. In accordance with the IUPAC recommendations (LEIGH [1990]) the old *Strukturbericht* designation (A3 for hP2-Mg, for instance) should not be used any longer. A comparison of the Pearson notation, prototype formula, space group and Strukturbericht designation for a large number of crystal structure types is given in MASSALSKI [1990].

 The Pearson symbol consists of two letters and a number. The first (lower case letter) denotes the crystal family, the second (upper case) letter the Bravais lattice type (table 4). The symbol is completed by the number of atoms in the unit cell. The symbol cF4, for instance, classifies a structure type to be cubic (c), all-face centered (F), with 4 atoms per unit cell. In

Table 3

Periodic table of the elements. In accordance with the recommendations of the IUPAC 1988, the columns are numbered consecutively from 1 to 18. The elements whose structures are discussed in this chapter are shadowed.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18					
1 H																	2 He					
3 Li	4 Be																5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg																13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr					
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe					
55 Cs	56 Ba	57* La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn					
87 Fr	88 Ra	89+ Ac																				
<b>* Lanthanide metals</b>		58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu							
<b>+Actinide metals</b>		90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr							

the case of rhombohedral structures, like the hR3-Sm type, the number of atoms in the unit cell in the rhombohedral setting ( $a=b=c$ ,  $\alpha=\beta=\gamma \neq 90^\circ$ ) is given. The number of atoms in the corresponding hexagonal setting ( $a=b \neq c$ ,  $\alpha=\beta=90^\circ$ ,  $\gamma=120^\circ$ ) would be three times as much.

Table 4  
Meaning of the letters included in the Pearson Symbol.

Crystal family		Bravais lattice type					
a	triclinic (anorthic)	P	primitive				
m	monoclinic	I	body centered				
o	orthorhombic	F	all-face centered				
t	tetragonal	C	side- or base-face centered				
h	hexagonal, trigonal (rhombohedral)	R	rhombohedral				
c	cubic						

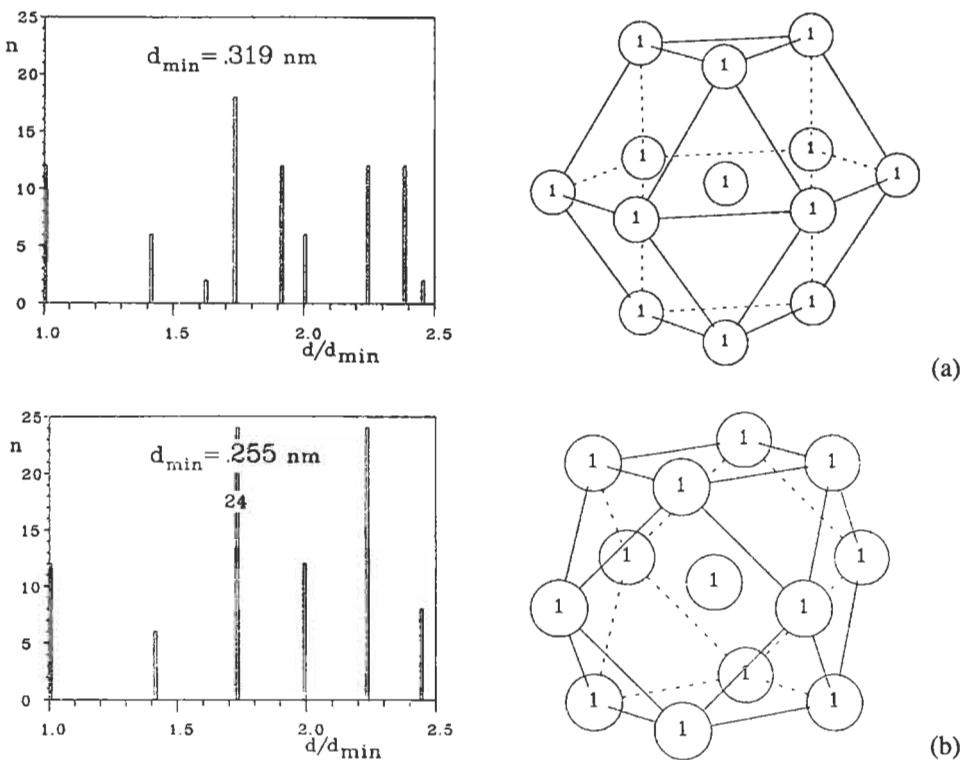


Fig. 9. Histograms of distances and coordination polyhedra of (a) hexagonal and (b) cubic closest packing (from DAAMS *et al.* [1991]).

### 3.2. Group 1 and 2, alkali and alkaline earth metals

The alkali and alkaline earth metals (table 5) belong to the typical metals. The outer electrons occupy the ns-orbitals, ionization removes the electrons of a whole shell, thus drastically reducing the atomic radius (Li: atomic radius 1.56 Å, ionic radius 0.60 Å, for instance). The absence of directional bonds forces close atomic (sphere) packings; the alkali metals conform most closely to the free electron gas model of metals. Under ambient conditions the alkali metals all crystallize in the simple body-centered cubic (bcc) structure cI2-W (fig. 12). The bcc structure is assumed to be more stable at higher temperature than the ccp or hcp one owing to its higher vibrational entropy. At lower temperature or higher pressure, the bcc structure is transformed martensitically to the closest-packed lattice types, hR3-Sm or cF4-Cu, respectively. Contrary to earlier studies, the hexagonal closest-packed phases are not of the hP2-Mg but of the hR3-Sm type (fig. 10) with stacking sequence ...ABABCBCAC... (YOUNG [1991]).

The extremely strong dependence of the atomic volume on pressure, which increases with increasing atomic number due to the shielding of the outer electrons by the

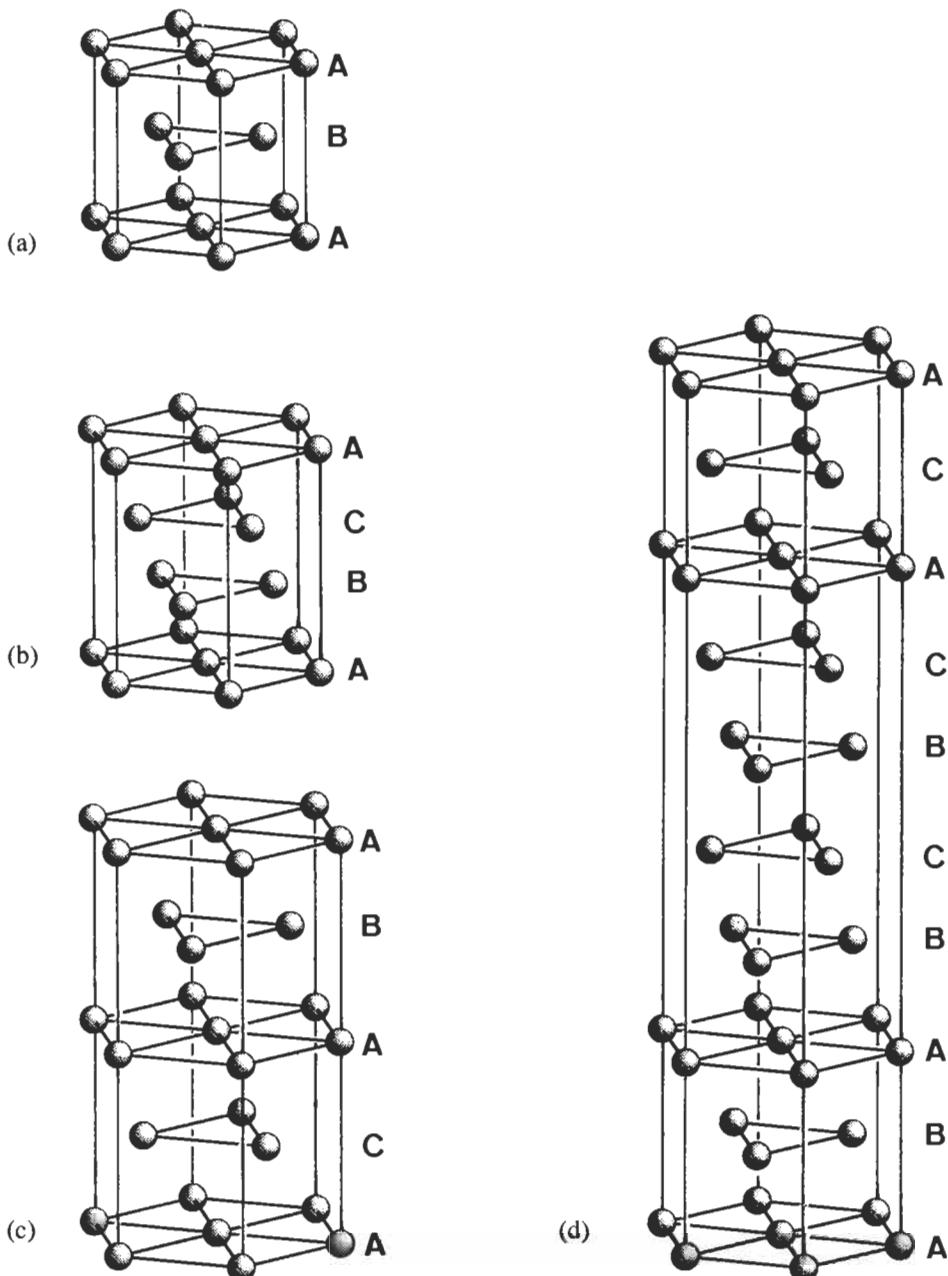


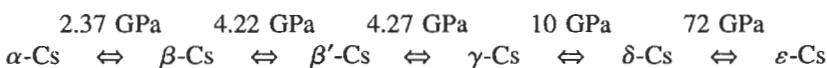
Fig. 10. Schematic representation of the stacking sequences of the closest-packed structures (a) hP2–Mg, (b) cF4–Cu, (c) hP4–La and (d) hR3–Sm.

Table 5

Structure information for the elements of group 1, alkali metals, and of group 2, alkaline earth metals. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$
Li 3 $1s^2 2s^1$	$V_{\text{at}} = 21.60 \text{ \AA}^3$				Be 4 $1s^2 2s^2$	$V_{\text{at}} = 8.11 \text{ \AA}^3$			
$\alpha < 70$		hR3	Sm		$\alpha$		hP2	Mg	1.568
$\beta$		cI2	W		$\beta > 1543$		cI2	W	
$\gamma > 6.9$		cF4	Cu		$\gamma > 28.3$		hP8?		0.789
Na 11 $1s^2 2s^2 p^6 3s^1$	$V_{\text{at}} = 39.50 \text{ \AA}^3$				Mg 12 $1s^2 2s^2 p^6 3s^2$	$V_{\text{at}} = 23.24 \text{ \AA}^3$			
$\alpha < 40$		hR3	Sm		$\alpha$		hP2	Mg	1.624
$\beta$		cI2	W		$\beta > 50$		cI2	W	
K 19 $1s^2 2s^2 p^6 3s^2 p^6 4s^1$	$V_{\text{at}} = 75.33 \text{ \AA}^3$				Ca 20 $1s^2 2s^2 p^6 3s^2 p^6 4s^2$	$V_{\text{at}} = 43.62 \text{ \AA}^3$			
$\alpha$		cI2	W		$\alpha$		cF4	Cu	
$\beta > 12$		cF4	Cu		$\beta > 728$ or $> 19.5$		cI2	W	
					$\gamma > 32$		cP1	$\alpha\text{-Po}$	
Rb 37 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 5s^1$	$V_{\text{at}} = 92.59 \text{ \AA}^3$				Sr 38 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 5s^2$	$V_{\text{at}} = 56.35 \text{ \AA}^3$			
$\alpha$		cI2	W		$\alpha$		cF4	Cu	
$\beta > 7.0$		cF4	Cu		$\beta > 504$		hP2	Mg	1.636
$\gamma > 14$					$\gamma > 896$ or $> 3.5$		cI2	W	
$\delta > 17$					$\delta > 26$				
$\varepsilon > 20$		tI4			$\varepsilon > 35$				
Cs 55 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} 5s^2 p^6 6s^1$	$V_{\text{at}} = 117.79 \text{ \AA}^3$				Ba 56 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} 5s^2 p^6 6s^2$	$V_{\text{at}} = 63.36 \text{ \AA}^3$			
$\alpha$		cI2	W		$\alpha$		cI2	W	
$\beta > 2.37$		cF4	Cu		$\beta > 5.33$		hP2	Mg	1.581
$\beta' > 4.22$		cF4	Cu		$\gamma > 7.5$				
$\gamma > 4.27$		tI4			$\delta > 12.6$				
$\delta > 10$									
$\varepsilon > 72$		cF4?							
Fr 87 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^2 p^6 7s^1$					Ra 88 $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^2 p^6 7s^2$	$V_{\text{at}} = 68.22 \text{ \AA}^3$			
					$\alpha$		cI2	W	

increasing number of inner electron shells, is shown by the example of Cs (fig. 13). With increasing pressure, the valence electrons change from s to d character, giving rise to a large number of pressure-induced phase transitions at ambient temperature (YOUNG [1991]):



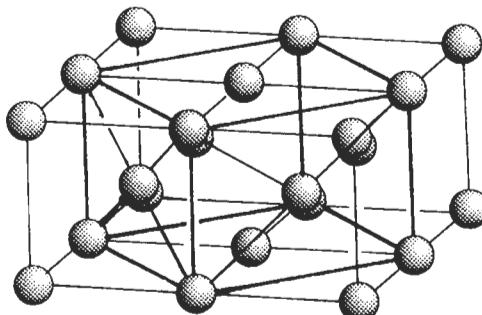


Fig. 11. Relationship between body-centered cubic (bcc)  $\alpha$ -Fe, cI2-W type, space group  $I\bar{m}\bar{3}m$ , No. 229, 1a: 0 0 0, and face-centered cubic (fcc)  $\gamma$ -Fe, cF4-Cu type, space group  $F\bar{m}\bar{3}m$ , No. 225, 4a: 0 0 0. The face-centered tetragonal unit cell drawn into an array of four bcc unit cells transforms by shrinking its faces to fcc.

 The alkaline earth metals behave quite similarly to the alkali metals. They crystallize under ambient conditions in one of the two closest-packed structures (ccp or hcp) or in the body-centered cubic (bcc) structure type and also show several allotropic forms (fig. 14). The large deviation  $c/a = 1.56$  from the ideal value of 1.633 for beryllium indicates covalent bonding contributions.

For alkali and alkaline earth metals, the pressure-induced phase transitions from cI2-W to cF4-Cu occur with increasing atomic number at decreasing pressures.

### 3.3. Groups 3 to 10, transition metals

 The elements of groups 3 to 10 are typical metals which have in common that their d-orbitals are partially occupied. These orbitals are only slightly screened by the outer s-electrons, leading to significantly different chemical properties of the transition elements going from left to right in the periodic system. The atomic volumes decrease rapidly with increasing number of electrons in bonding d-orbitals, because of cohesion, and increase as the anti-bonding d-orbitals become filled (fig. 15). The anomalous behavior of the 3d-transition metals, Mn, Fe and Co, may be explained by the existence of non-bonding d-electrons (PEARSON [1972]).

 Scandium, yttrium, lanthanum and actinium (table 6) are expected to behave quite

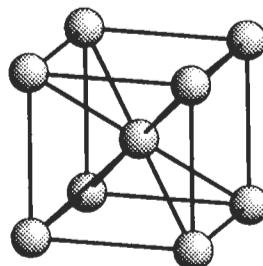


Fig. 12. Unit cell of the body-centered cubic structure type cI2-W, space group  $I\bar{m}\bar{3}m$ , No. 229, 1a: 0 0 0.

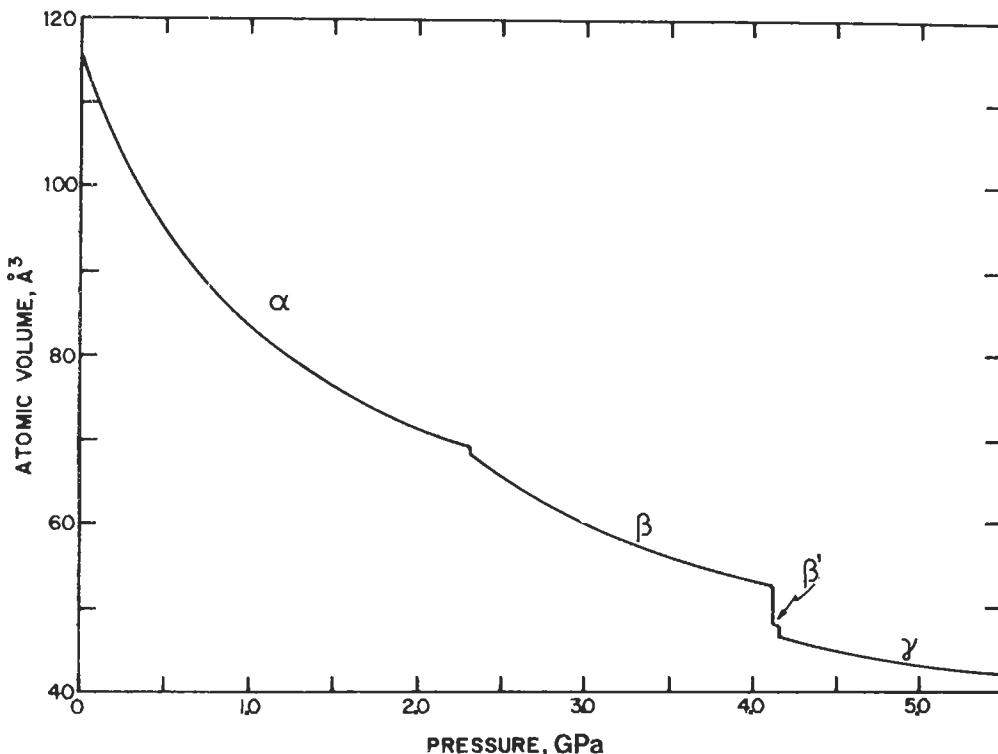


Fig. 13. The variation of the atomic volume of cesium with pressure (after DONOHUE [1974]).

similarly. Indeed they show similar phase sequences: the high-pressure phases of light elements occur as the ambient-pressure phases of the heavy homologues. The hP4 phase of lanthanum, with the sequence ..ACAB.., is one of the simpler closest-packed polytypic structures common for the lanthanides (fig. 16 and fig. 10). Another typical polytype for lanthanides is the hR3 phase of yttrium with stacking sequence ..ABABCBCAC.. (fig. 17 and fig. 10).

Titanium, zirconium and hafnium (table 6) crystallize in a slightly compressed hcp structure type and transform to bcc at higher temperatures. At higher pressures the  $\omega$ -Ti phase is obtained (fig. 18). The packing density of the hP3-Ti structure with ~0.57 is slightly larger than that of the simple cubic  $\alpha$ -Po structure (~0.52) but substantially lower than for bcc (~0.68) or ccp and hcp (~0.74) type structures. Calculations have shown that the  $\omega$ -Ti phase is stable owing to covalent bonding contributions from s-d electron transfer. At even higher pressures, zirconium and hafnium transform to the cI2-W type, while titanium remains in the hP3-Ti phase up to at least 87 GPa. By theoretical considerations it is also expected that titanium performs this transformation at sufficiently high pressures (AHUJA *et al.* [1993]). A general theoretical phase diagram for Ti, Zr and Hf is shown in fig. 19.

Vanadium, niobium, tantalum, molybdenum and tungsten have only simple bcc

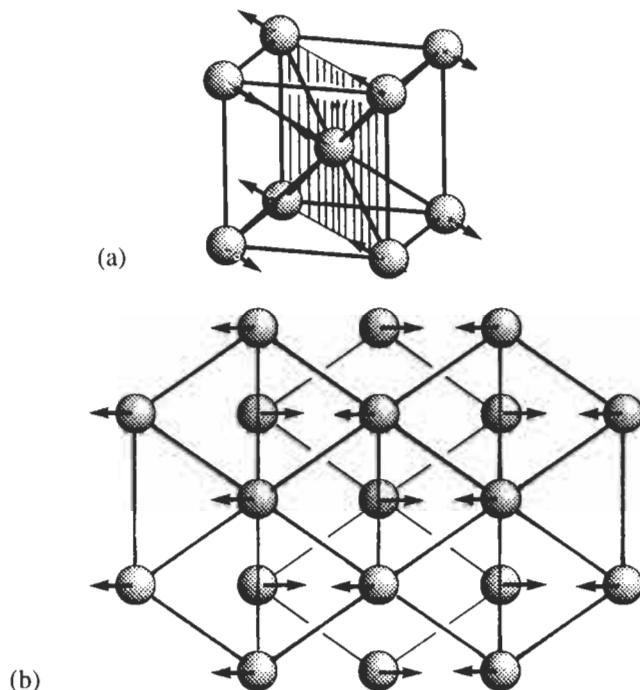


Fig. 14. Illustration of the bcc-to-hcp phase transition of Ba. (a) bcc unit cell with (110) plane marked. (b) Projection of the bcc structure upon the (110) plane. Atomic displacements necessary for the transformation are indicated by arrows.

structures (table 7). Up to pressures of 170 to 364 GPa no further allotropes could be found, in agreement with theoretical calculations. Chromium shows two antiferromagnetic phase transitions, which modify the structure only very slightly (YOUNG [1991]).

 The high-temperature phases of manganese (table 8),  $\gamma$ -Mn, cF4-Cu type, and  $\delta$ -Mn, cI2-W type, are typical metal structures, whereas  $\alpha$ -Mn and  $\beta$ -Mn form very complicated structures, possibly caused by their antiferromagnetism. Thus, the  $\alpha$ -Mn structure can be described as a  $3 \times 3 \times 3$  superstructure of bcc unit cells, with 20 atoms slightly shifted and 4 atoms added resulting in 58 atoms over all (fig. 20). The structure of  $\beta$ -Mn (fig. 21) is also governed by the valence electron concentration ("electron compound" or Hume-Rothery-type phase). The variation of the atomic volume of manganese with temperature is illustrated in fig. 22. For technetium, rhenium, ruthenium and osmium, only simple hcp structures are known.

 The technically most important element and the main constituent of the Earth's core, iron (table 8) shows five allotropic forms (fig. 23): ferromagnetic bcc  $\alpha$ -Fe transforms to paramagnetic isostructural  $\beta$ -Fe with a Curie temperature of 1043 K; at 1185 K fcc  $\gamma$ -Fe forms while at 1667 K a bcc phase, now called  $\delta$ -Fe, appears again. For the variation of

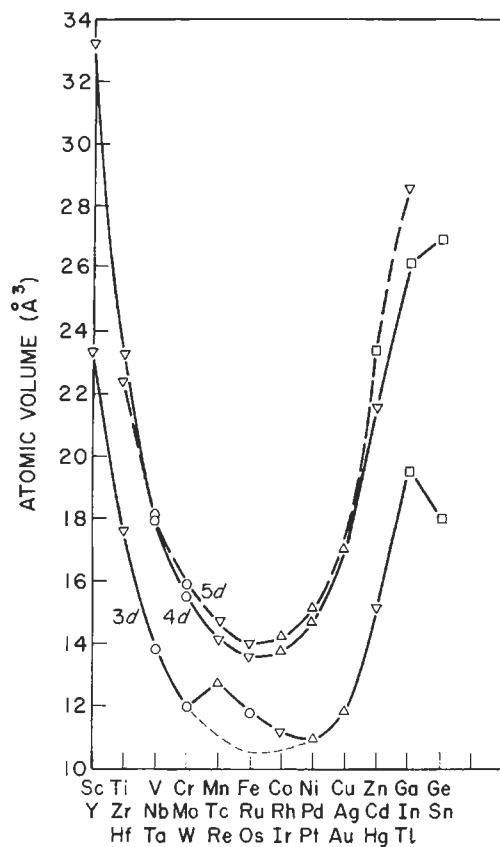


Fig. 15. Atomic volumes of the transition metals.  $\Delta$  means  $cF4-Cu$  type,  $\nabla$   $hP2-Mg$ ,  $\circ$   $cI2-W$ ,  $\square$  other types (after PEARSON [1972]).

the atomic volume with temperature see fig. 24. High-pressure nonmagnetic  $\varepsilon$ -Fe, existing above 13 GPa, has a slightly compressed hcp structure.

 Cobalt (table 9) is dimorphous, hcp at ambient conditions and ccp at higher temperatures. By annealing it in a special way, stacking disorder can be generated: the hcp sequence ..ABAB.. is statistically disturbed by a ccp sequence ..ABCABC.. like ..ABABABABCBCBCBC.. with a frequency of about one ..ABC.. among ten ..AB... Rhodium, iridium, nickel, palladium and platinum all crystallize in simple cubic closest-packed structures.

### 3.4. Groups 11 and 12, copper and zinc group metals

 The “mint metals”, copper, silver and gold (table 10) are typical metals with ccp structure type (fig. 25). Their single ns electron is less shielded by the filled d-orbitals than the ns electron of the alkali metals by the filled noble gas shell. The d-electrons also contribute to the metallic bond. These factors are responsible for the more noble

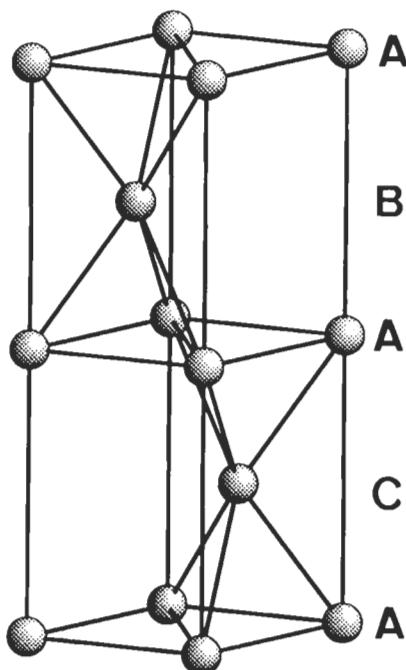


Fig. 16. One unit cell of the hP4-La structure type, space group  $P6_3/mmc$ , No. 194, 2a: 0 0 0, 2c:  $\frac{1}{3} \frac{2}{3} \frac{1}{4}$ .

character of these metals than of the alkali metals and that these elements sometimes are grouped to the transition elements.

 For zinc, cadmium and mercury (table 10) covalent bonding contributions (filled d-band) lead to deviations from hexagonal closest packing (hcp), with its ideal axial ratio  $c/a = 1.633$ , to values of 1.856 (Zn) and 1.886 (Cd), respectively. The bonds in the hcp layers are shorter and stronger, consequently, than between the layers. With increasing pressure,  $c/a$  approximates the ideal value 1.633: for Cd  $c/a = 1.68$  was observed at 30 GPa (DONOHUE [1974]), and for Hg,  $c/a = 1.76$  at 46.8 GPa (SCHULTE and HOLZAPFEL [1993]).

 The rhombohedral structure of  $\alpha$ -Hg may be derived from a ccp structure by compression along the threefold axis (fig. 26). In contrast to zinc and cadmium, the ratio  $c/a = 1.457$  for a hypothetical distorted hcp structure is smaller than the ideal value. There also exist several high-pressure allotropes (fig. 27).

### 3.5. Groups 13 to 16, metallic and semi-metallic elements

Only aluminum, thallium and lead crystallize in the closest-packed structures characteristic for typical metals (table 11). The s-d transfer effects, important for alkali- and alkaline-earth metals, do not appear for the heavier group 13 elements owing to their filled d-bands. Orthorhombic gallium forms a  $6^3$  network of distorted hexagons parallel to (100) at heights  $x=0$  and  $1/2$  (fig. 28). The bonds between the layers are considerably

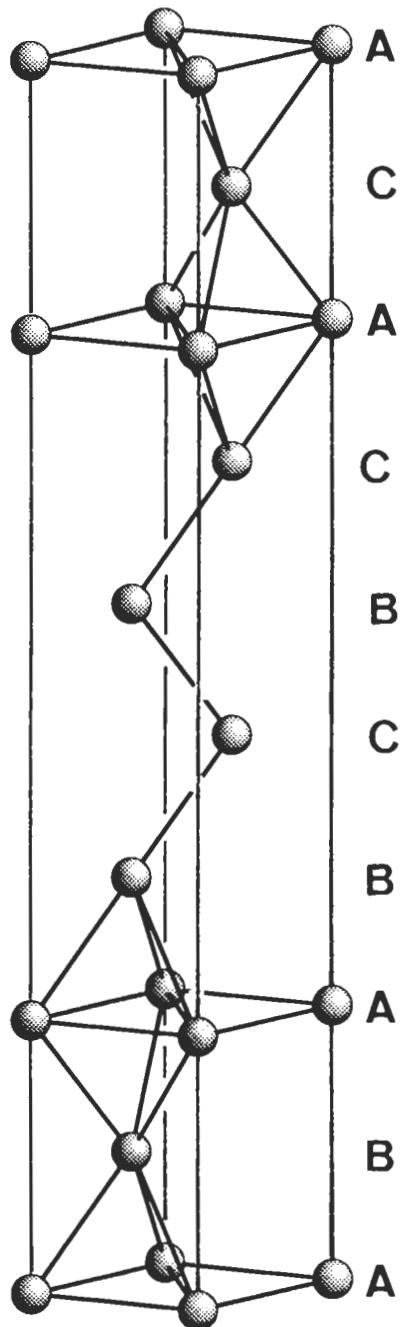


Fig. 17. One unit cell of the hR3-Sm structure type, space group  $\bar{R}\bar{3}m$ , No. 166, 3a: 0 0 0, 6c: 0 0 0.22.

*References: p. 45.*

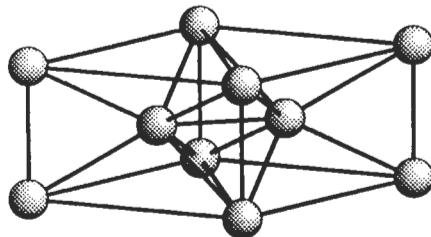


Fig. 18. The hP3–Ti structure type, space group P6/mmm, No. 191, 1a: 0 0 0, 2d:  $\frac{1}{3} \frac{2}{3} \frac{1}{2}$ .

weaker than within. At higher pressure gallium transforms to a bcc phase, cI12–Ga, and additionally increasing the temperature leads to the tetragonal indium structure type tI2–In (fig. 29). In an alternative description based on a face-centered tetragonal unit cell with  $a' = \sqrt{2} a$ , the resemblance to a slightly distorted cubic close-packed structure with  $c/a = 1.08$  becomes clear.

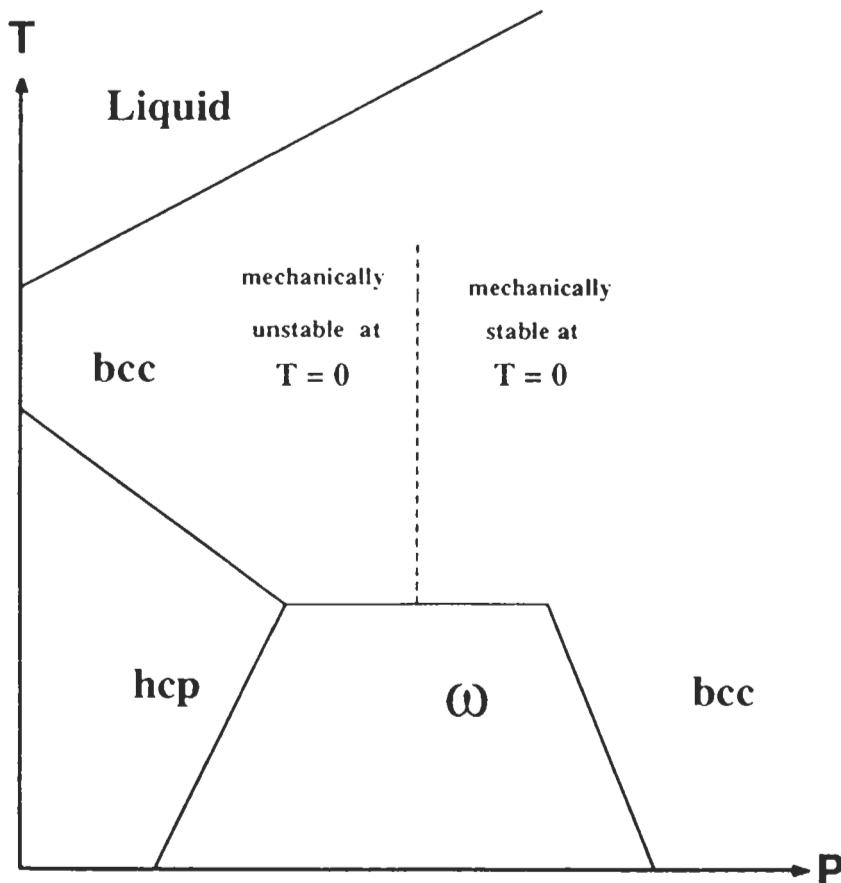


Fig. 19. Schematic calculated phase diagram for Ti, Zr and Hf (from AHUJA *et al.* [1993]).

Table 6

Structure information for the elements of groups 3 and 4. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

	T[K]	P[GPa]	PS	PT	$c/a$		T[K]	P[GPa]	PS	PT	$c/a$
<b>Sc</b>	21	$V_{\text{at}}=24.97 \text{ \AA}^3$				<b>Ti</b>	22	$V_{\text{at}}=17.65 \text{ \AA}^3$			
		$1s^2 2s^2 p^6 3s^2 p^6 d^1 4s^2$					$1s^2 2s^2 p^6 3s^2 p^6 d^2 4s^2$				
$\alpha$			hP2	Mg	1.592	$\alpha$			hP2	Mg	1.587
$\beta$	> 1610		cI2	W		$\beta$	> 1155		cI2	W	
$\gamma$	> 19		tP4?			$\omega$	> 2		hP3	$\omega$ -Ti	
<b>Y</b>	39	$V_{\text{at}}=33.01 \text{ \AA}^3$				<b>Zr</b>	40	$V_{\text{at}}=23.28 \text{ \AA}^3$			
		$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^1 5s^2$					$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^2 5s^2$				
$\alpha$			hP2	Mg	1.571	$\alpha$			hP2	Mg	1.593
$\beta$	> 1751		cI2	W		$\beta$	> 1136		cI2	W	
$\gamma$	> 10		hR3	Sm		$\omega$	> 2		hP3	$\omega$ -Ti	
$\delta$	> 26		hP4?			$\omega'$	> 30		cI2	W	
$\varepsilon$	> 39		cF4	Cu							
<b>La</b>	57	$V_{\text{at}}=37.17 \text{ \AA}^3$				<b>Hf</b>	72	$V_{\text{at}}=22.31 \text{ \AA}^3$			
		$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} 5s^2 p^6 d^1 6s^2$					$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^2 6s^2$				
$\alpha$			hP4	$\alpha$ -La	2×1.613	$\alpha$			hP2	Mg	1.581
$\beta$	> 583 or > 2.3		cF4	Cu		$\beta$	> 2016		cI2	W	
$\gamma$	> 1138		cI2	W		$\omega$	> 38		hP3	$\omega$ -Ti	
$\delta$	> 7.0		hP6			$\omega'$	> 71		cI2	W	
<b>Ac</b>	89	$V_{\text{at}}=37.45 \text{ \AA}^3$ at 293 K $\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^2 p^6 d^{17} 7s^2$				<b>Ku</b>	104				
$\alpha$			cF4	Cu			$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{14} 6s^2 p^6 d^{27} 7s^2$				

Silicon and germanium (table 11) under ambient conditions crystallize in the diamond structure, owing to strong covalent bonding. At higher pressures they transform to the metallic white-tin ( $\text{tI4-Sn}$ ) structure. This structure type consists of a body-centered tetragonal lattice which can be regarded as being intermediate between the diamond structure of semiconducting  $\alpha$ -Sn and ccp lead (fig. 30). For an ideal ratio of  $c/a=0.528$  one atom is sixfold coordinated. The high-pressure phase hP1-BiIn has a quasi-eightfold coordination, the ideal ratio for CN=8 would be  $c/a=1$ . At higher pressures, closest-packed structures with twelvefold coordinations are obtained. Thus with increasing pressure silicon runs through phases with coordination numbers 4, 6, 8 and 12.

The effective radius of tin in  $\beta$ -Sn and of lead in  $\alpha$ -Pb is large compared with that of other typical metals with large atomic number due to uncomplete ionization of the single ns electron. This means that in  $\alpha$ -Sn, for instance, the electron configuration is ... $5s^1 5p^3$ , allowing  $sp^3$ -hybridization and covalent tetrahedrally coordinated bonding, whereas in  $\beta$ -Sn with ... $5s^2 5p^2$  only two p-orbitals are available for covalent and one further p-orbital for metallic bonding.

The structure of arsenic, antimony and bismuth (isotypic under ambient conditions)

Table 7

Structure information for the elements of groups 5 and 6. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$
<b>V</b> 23 $V_{\text{at}} = 13.82 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>3</sup> 4s <sup>2</sup>					<b>Cr</b> 24 $V_{\text{at}} = 12.00 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>5</sup> 4s <sup>1</sup>				
		cl2	W				cl2	W	
<b>Nb</b> 41 $V_{\text{at}} = 17.98 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>5</sup> s <sup>1</sup>					<b>Mo</b> 42 $V_{\text{at}} = 15.58 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>5</sup> s <sup>1</sup>				
		cl2	W				cl2	W	
<b>Ta</b> 73 $V_{\text{at}} = 18.02 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>3</sup> 6s <sup>2</sup>					<b>W</b> 74 $V_{\text{at}} = 15.85 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>4</sup> 6s <sup>2</sup>				
		cl2	W				cl2	W	

(table 12) consists of puckered layers of covalently bonded atoms stacked along the hexagonal axis (fig. 31). The structure can be regarded as a distorted primitive cubic structure ( $\alpha$ -Po) in which the atomic distance  $d_1$  in the layer equals that between the layers  $d_2$ . The metallic character of these elements increases for  $d_2/d_1$  approximating to 1 (table 13).

The helical structures of isotropic  $\alpha$ -Se and  $\alpha$ -Te may also be derived from the

Table 8

Structure information for the elements of groups 7 and 8. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$
<b>Mn</b> 25 $V_{\text{at}} = 12.21 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>5</sup> 4s <sup>2</sup>					<b>Fe</b> 26 $V_{\text{at}} = 11.78 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>6</sup> 4s <sup>2</sup>				
$\alpha$		cl58	$\alpha$ -Mn		$\alpha$		cl2	W	
$\beta$ > 1000		cP20	$\beta$ -Mn		$\gamma$ > 1185		cF4	Cu	
$\gamma$ > 1373		cF4	Cu		$\delta$ > 1667		cl2	W	
$\delta$ > 1411		cl2	W		$\varepsilon$ > 13		hP2	Mg	1.603
<b>Tc</b> 43 $V_{\text{at}} = 14.26 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>6</sup> 5s <sup>1</sup>					<b>Ru</b> 44 $V_{\text{at}} = 13.57 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>7</sup> 5s <sup>1</sup>				
		hP2	Mg	1.604			hP2	Mg	1.582
<b>Re</b> 75 $V_{\text{at}} = 14.71 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>5</sup> 6s <sup>2</sup>					<b>Os</b> 76 $V_{\text{at}} = 13.99 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>6</sup> 6s <sup>2</sup>				
		hP2	Mg	1.615			hP2	Mg	1.580

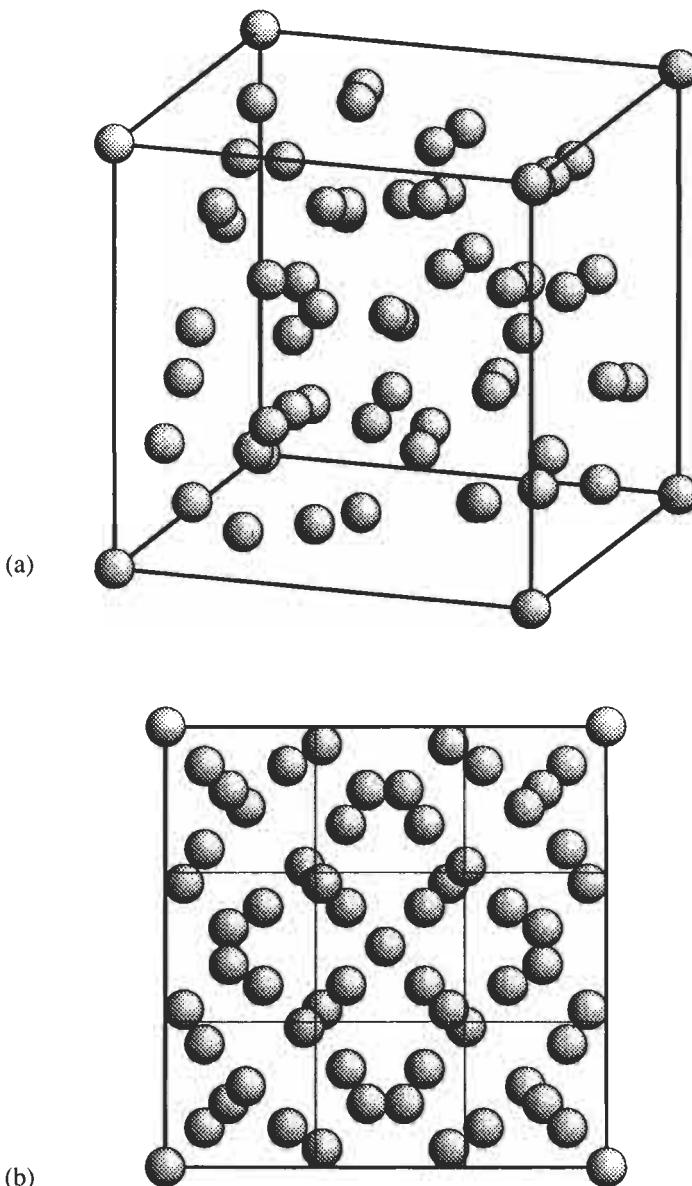


Fig. 20. One unit cell of cI58–Mn, space group  $I\bar{4}3m$ , No. 217, with four different types of Mn atoms in 2a: 0 0 0, 8c: 0.316 0.316 0.316, 24g: 0.356 0.356 0.034, 24g: 0.089 0.089 0.282, shown (a) in perspective view and (b) in projection. Two types of Mn atoms are coordinated by CN 16 Friauf polyhedra, one by a CN 14 Frank-Kasper polyhedron and one by an icosahedron.

primitive cubic  $\alpha$ -Po structure (fig. 32). The infinite helices run along the trigonal axes, and have three atoms per turn. The interhelix bonding distance  $d_2$  plays a comparable

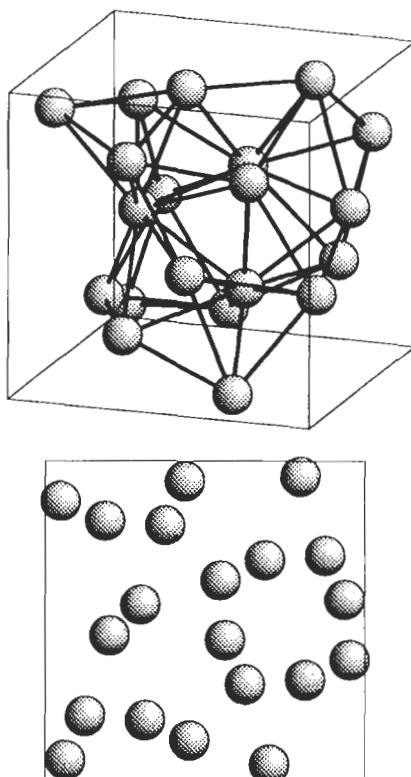


Fig. 21. One unit cell of cP20–Mn, space group  $P4_32$ , No 213, with two types of Mn atoms: 8c: 0.063 0.063 0.063, 12d: 0.125 0.202 0.452, shown (a) in perspective view and (b) in projection. The atoms in 8c are coordinated by 12 atoms in a distorted icosahedron, the Mn atoms in 12d by 14 atoms in a distorted Frank-Kasper CN 14 type polyhedron.

role for the metallic character of these elements as does the interlayer distance in the case of the group 15 elements. With increasing pressure, the transition to the metallic  $\beta$ -Te phase takes place.

### 3.6. Lanthanides and actinides

Lanthanides and actinides (table 14) are characterized by the fact that their valence electrons occupying the f-orbitals are shielded by filled outer s- and p-orbitals. The chemical properties of the lanthanides are rather uniform since the 4f-orbitals are largely screened by the 5s- and 5p-electrons. The chemical behavior of the actinides, however, is somewhat in between that of the 3d transition metals and the lanthanides since the 5f-orbitals are screened to a much smaller amount by the 6s- and 6p-electrons. With the exception of Sm and Eu, all lanthanides under ambient conditions show either a simple hcp structure with the standard stacking sequence ..AB.. or a twofold superstructure with a stacking sequence ..ACAB... Samarium has, with ..ABABCBCAC.., an even more

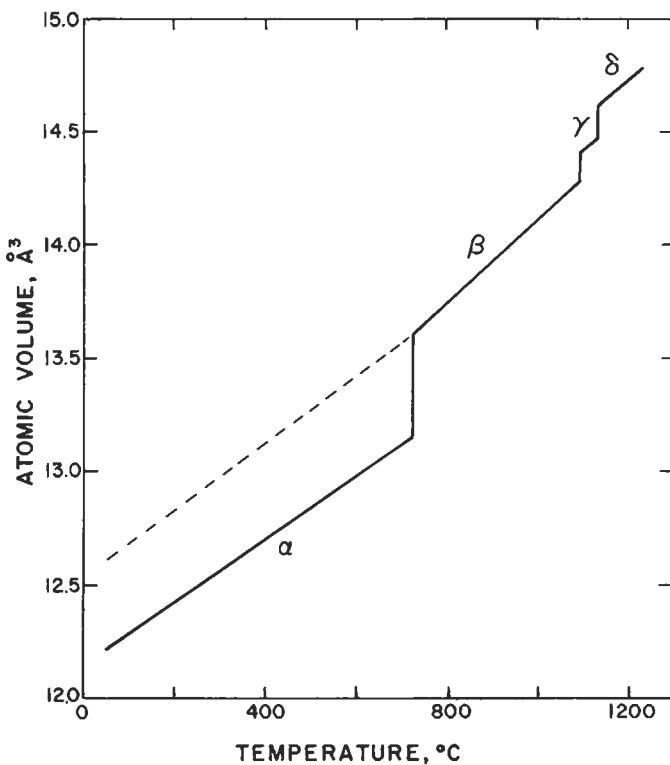


Fig. 22. The variation of the atomic volume of manganese with temperature (from DONOHUE [1974]).

Table 9

Structure information for the elements of groups 9 and 10. In the first line of each box the chemical symbol, atomic number  $Z$ , and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature  $T[\text{K}]$  and pressure  $P[\text{GPa}]$ , Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	c/a	T[K]	P[GPa]	PS	PT	c/a
Co 27	$V_{\text{at}} = 11.08 \text{\AA}^3$				Ni 28	$V_{\text{at}} = 10.94 \text{\AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^7 4s^2$					$1s^2 2s^2 p^6 3s^2 p^6 d^8 4s^2$			
$\epsilon$		hP2	Mg	1.623			cF4	Cu	
$\alpha$	> 695	cF4	Cu						
Rh 45	$V_{\text{at}} = 13.75 \text{\AA}^3$				Pd 46	$V_{\text{at}} = 14.72 \text{\AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^8 5s^1$					$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10}$			
		cF4	Cu				cF4	Cu	
Ir 77	$V_{\text{at}} = 14.15 \text{\AA}^3$				Pt 78	$V_{\text{at}} = 15.10 \text{\AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^7 6s^2$					$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^9 6s^1$			
		cF4	Cu				cF4	Cu	

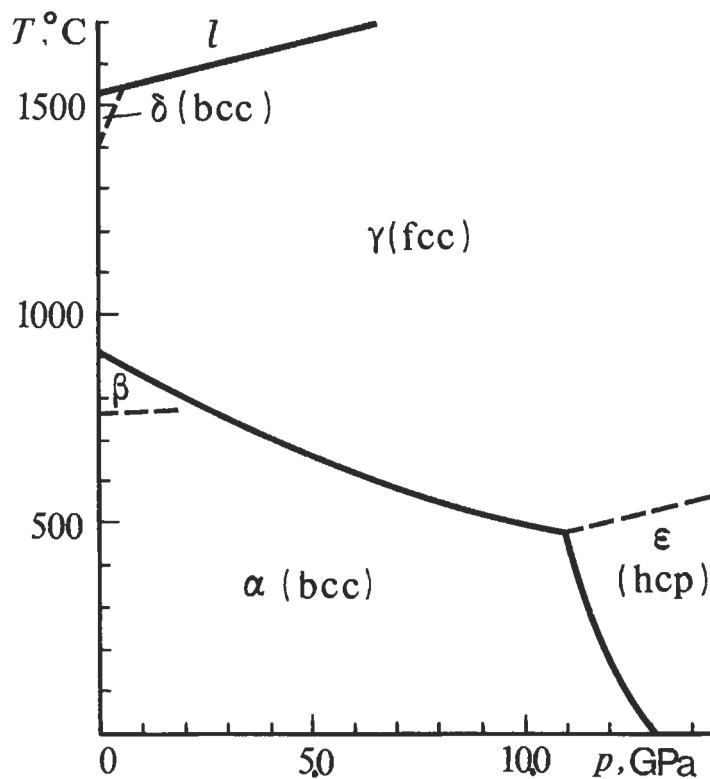
Fig. 23. Phase diagram of iron (from VAINSHTEIN *et al.* [1982]).

Table 10

Structure information for the elements of groups 11 and 12. In the first line of each box the chemical symbol, atomic number  $Z$ , and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature  $T[\text{K}]$  and pressure  $P[\text{GPa}]$ , Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

$T[\text{K}]$	$P[\text{GPa}]$	PS	PT	$c/a$	$T[\text{K}]$	$P[\text{GPa}]$	PS	PT	$c/a$
<b>Cu</b> 29 $V_{\text{at}} = 11.81 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^1$		cF4	Cu		<b>Zn</b> 30 $V_{\text{at}} = 15.20 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2$		hP2	Mg	1.856
<b>Ag</b> 47 $V_{\text{at}} = 17.05 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} 5s^1$		cF4	Cu		<b>Cd</b> 48 $V_{\text{at}} = 21.60 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} 5s^2$		hP2	Mg	1.886
<b>Au</b> 79 $V_{\text{at}} = 16.96 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^1$		cF4	Cu		<b>Hg</b> 80 $V_{\text{at}} = 23.13 \text{ \AA}^3$ at 80 K $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^2$		hR1	$\alpha$ -Hg	
					$\alpha$ < 234.3		tI2	$\alpha$ -Pa	
					$\beta$ > 3.7		oP4		
					$\gamma$ > 12				
					$\delta$ > 37		hP2	Mg	1.76

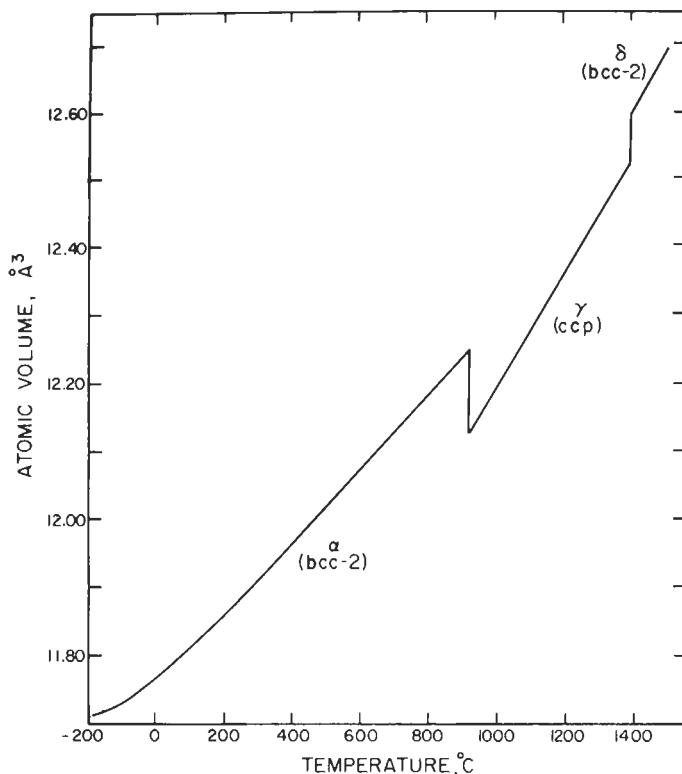


Fig. 24. The variation of atomic volume of iron with temperature (from DONOHUE [1974]).

complicated stacking order with 4.5-fold superperiod. For all lanthanides the ratio  $c/a$  is near the ideal value of  $n \times 1.633$ . It is interesting that with increasing pressure and decreasing atomic number the sequence of closest-packed phases hP2–Mg (..AB..)  $\Rightarrow$  hR3–Sm (..ABABCBCAC..)  $\Rightarrow$  hP4–La (..ACAB..)  $\Rightarrow$  cF4–Cu (..ABC..)  $\Rightarrow$  hP6–Pr appears (cf. figs. 10, 17 and 33).

Cerium undergoes a transformation from the  $\gamma$  to the  $\alpha$ -phase at pressures  $> 0.7$  GPa:

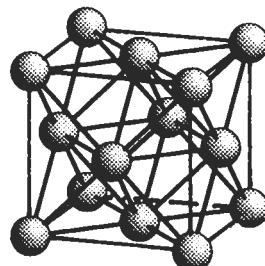


Fig. 25. The structure of cF4–Cu, space group  $Fm\bar{3}m$ , No. 225, 4a 0 0 0.

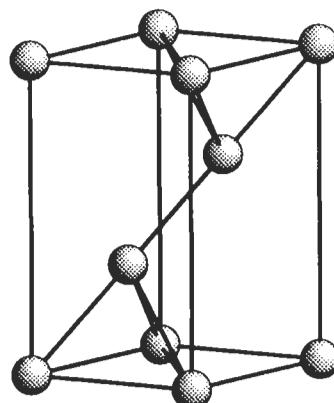


Fig. 26. The structure of hR1-Hg, space group  $R\bar{3}m$ , No. 166, 3a 0 0 0.

the CCP structure is preserved but the lattice constant decreases drastically from 5.14 to 4.84 Å owing to a transition of one 4f-electron to the 5d-level (fig. 34). This isostructural transition is terminated in a critical point near 550 K and 1.75 GPa (YOUNG [1991]). Further compression gives the transformation at 5.1 GPa to the  $\alpha'$ -phase, and finally at 12.2 GPa to the  $\varepsilon$ -phase. Europium shows a completely different behavior, as do the other lanthanides, owing to the stability of its half filled 4f-orbitals. Thus, it has more similarities to the alkaline earth metals; its phase diagram is comparable to that of barium

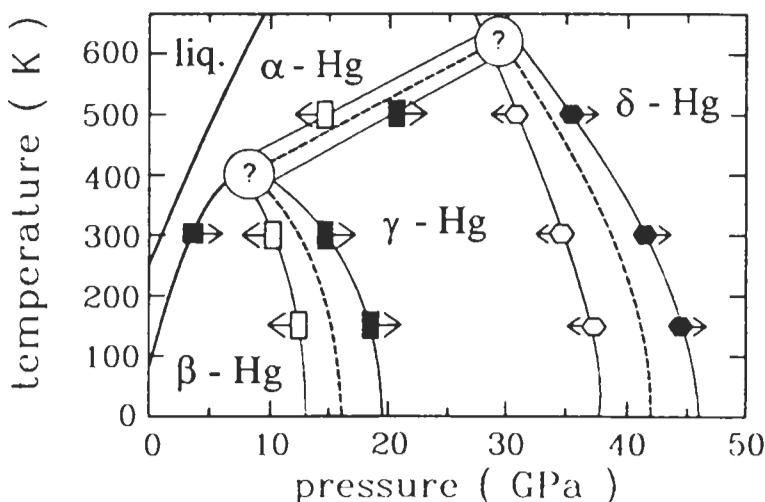


Fig. 27. Schematical phase diagram of mercury (from SCHULTE and HOLZAPFEL [1993]).

Table 11

Structure information for the elements of groups 13 and 14. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{at}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$
<b>Al</b> 13 $V_{at}=16.60 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>1</sup>					<b>Si</b> 14 $V_{at}=20.02 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>2</sup>				
		cF4	Cu		$\alpha$		cF8	Cd	
					$\beta$	> 12	tI4	$\beta$ -Sn	0.552
					$\gamma$	> 13.2	hP1	BiIn	0.92
					$\delta$	> 36		$\sigma$ ?	
					$\varepsilon$	> 43	hP2	Mg	1.699
					$\zeta$	> 78	cF4	Cu	
<b>Ga</b> 31 $V_{at}=19.58 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>1</sup>		oC8	$\alpha$ -Ga		<b>Ge</b> 32 $V_{at}=22.63 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>2</sup>		cF8	C	
$\alpha$					$\alpha$		cF8		
$\beta$ < 330 > 1.2		cI12			$\beta$	> 11	tI4	$\beta$ -Sn	0.551
$\gamma$ > 330 > 3.0		tI2	In	1.588	$\gamma$	> 75	hP1	BiIn	0.92
					$\delta$	> 106	hP4		
<b>In</b> 49 $V_{at}=26.16 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 5s <sup>2</sup> p <sup>1</sup>		tI2	In	1.521	<b>Sn</b> 50 $V_{at}=34.16 \text{ \AA}^3$ at 285 K 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 5s <sup>2</sup> p <sup>2</sup>		cF8	C	
					$\alpha$ < 291		cF8		
					$\beta$ > 291		tI4	$\beta$ -Sn	0.546
					$\gamma$	> 9.2	tI2	Pa	0.91
					$\delta$	> 40	cI2	W	
<b>Tl</b> 81 $V_{at}=28.59 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 6s <sup>2</sup> p <sup>1</sup>					<b>Pb</b> 82 $V_{at}=30.32 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 6s <sup>2</sup> p <sup>2</sup>		cF4	Cu	
$\alpha$			hP2	Mg	$\alpha$		cF4		
$\beta$ > 503			cI2	W	$\beta$	> 13.7	hP2	Mg	1.650
$\gamma$ > 3.7		cF4	Cu		$\gamma$	> 109	cI2	W	

rather than to the other lanthanides. A similar behavior is observed for ytterbium which is divalent owing to the stability of the completely filled 4f-orbitals; its phase diagram resembles that of strontium.

The  $c$ -lattice parameter of gadolinium exhibits an anomalous expansion when cooled below 298 K (fig. 35) due to a change in the magnetic properties of the metal. Several other lanthanides show a similar behavior.

According to their electronic properties, the actinides (table 14) can be divided into two subgroups: the elements from thorium to plutonium have itinerant 5f-electrons contributing to the metallic bond, whereas the elements from americium onwards have more localized 5f-electrons. This situation leads to superconductivity for thorium, protactinium and uranium, for instance, and to magnetic ordering for curium, berkelium and californium (DABOS-SEIGNON *et al.* [1993]). The contribution of 5f-electrons to

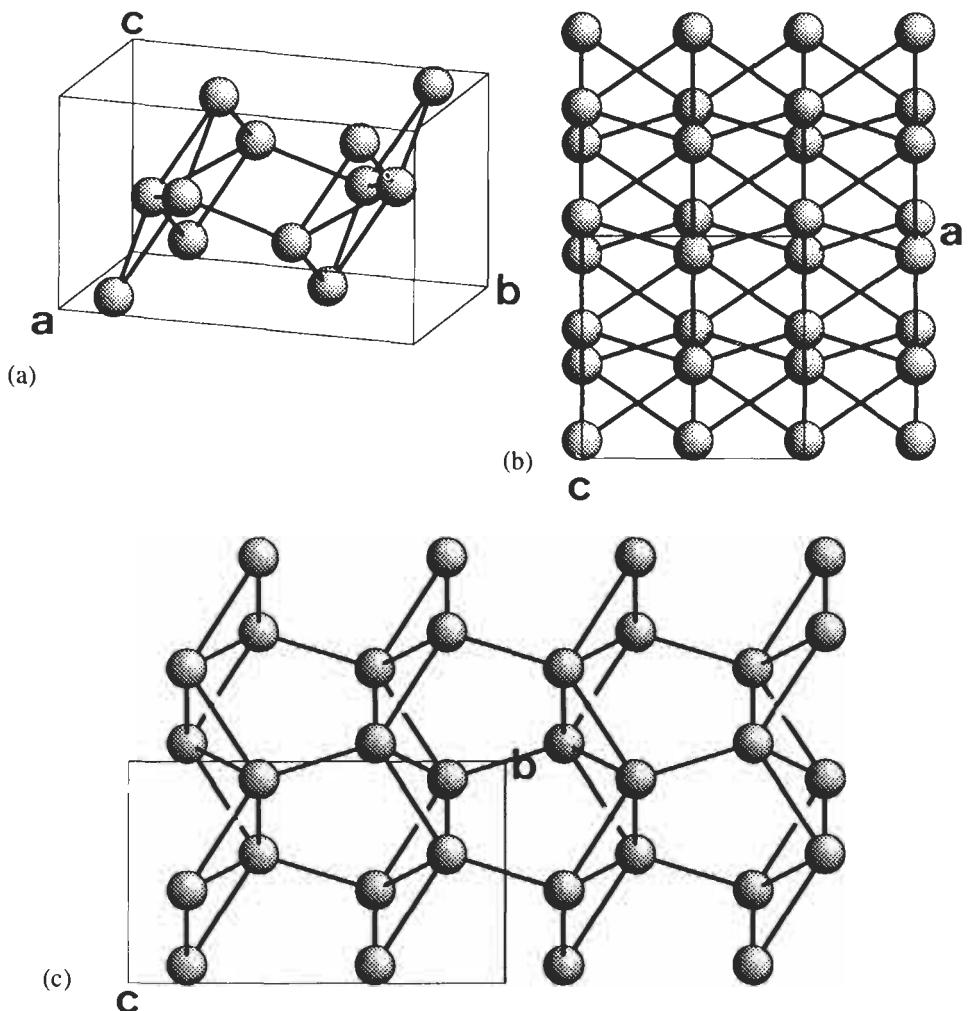


Fig. 28. The structure of oC8–Ga, Cmca, No. 64, 8f 0 0.155 0.081, (a) in a perspective view and projected upon (b) (010) and (c) (100), showing the distorted hexagonal layers.

bonding leads to low symmetry, small atomic volumes and high density in the case of the light actinides while the heavier actinides crystallize at ambient conditions in the hcp structure type. The position of plutonium at the border of itinerant and localized 5f-states causes its unusually complex phase diagram, with structures typical for both cases. Thus, monoclinic  $\alpha$ -Pu can be considered as a distorted hcp-structure with about 20% higher packing density than cF4-Pu owing to covalent bonding contributions from 5f-electrons (fig. 36) (EK *et al.* [1993]). This ratio is quite similar to the above-mentioned one of  $\alpha$ -Ce and  $\gamma$ -Ce, which are both ccp. The phase diagram of americium is very similar to

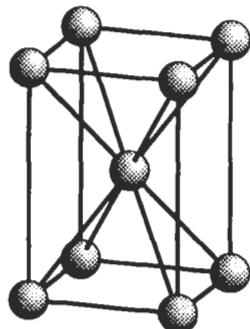


Fig. 29. The structure of tI<sub>2</sub>-In, space group I4/mmm, No. 139, 2a 0 0 0.

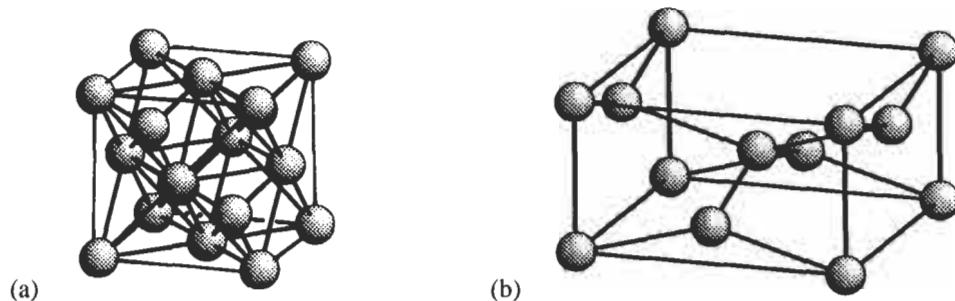


Fig. 30. Relationships between the structures of the two tin allotropes: (a) grey  $\alpha$ -Sn, cF8-C type, space group Fd<sub>3</sub>m, No. 227, 8a: 0 0 0,  $\frac{1}{4}$   $\frac{1}{4}$   $\frac{1}{4}$ , and (b) white  $\beta$ -Sn, tI<sub>4</sub>- $\beta$ -Sn type, space group I4<sub>1</sub>/amd, No. 141, 4a: 0 0 0. Note the large difference in the minimum distances:  $d_{\min}^{\alpha\text{-Sn}} = 1.54 \text{ \AA}$  and  $d_{\min}^{\beta\text{-Sn}} = 3.02 \text{ \AA}$ .

those of lanthanum, proseodymium and neodymium. Owing to the localization of 5f-electrons it is the first lanthanide-like actinide element.

Both lanthanides and actinides crystallize in a great variety of polymorphic modifications (fig. 37).

Table 12

Structure information for the more metallic elements of groups 15, pnictides, and of group 16, chalcogenides. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{\text{at}}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$	
<b>As</b> 33 $V_{\text{at}} = 21.52 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>3</sup>					<b>Se</b> 34 $V_{\text{at}} = 27.27 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>4</sup>					
$\alpha$		hR2	$\alpha$ -As	2.805	$\alpha$		hP3	$\alpha$ -Se	1.135	
$\beta$	> 25.0	cP1	$\alpha$ -Po		$\beta$	> 14	mP3			
					$\gamma$	> 28	tP4			
					$\delta$	> 41	hR2			
<b>Sb</b> 51 $V_{\text{at}} = 30.21 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 5s <sup>2</sup> p <sup>3</sup>					<b>Te</b> 52 $V_{\text{at}} = 33.98 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 5s <sup>2</sup> p <sup>4</sup>					
$\alpha$		hR2	$\alpha$ -As	2.617	$\alpha$		hP3	$\alpha$ -Se	1.330	
$\beta$	> 8	mP4	$\beta$ -Sb		$\beta$	> 4.0	mP4	$\beta$ -Te		
$\gamma$	> 28	cI2	W		$\gamma$	> 6.6	oP4			
					$\delta$	> 10.6	hR1	$\beta$ -Po		
					$\varepsilon$	> 27	cI2	W		
<b>Bi</b> 83 $V_{\text{at}} = 35.39 \text{ \AA}^3$ 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 6s <sup>2</sup> p <sup>3</sup>					<b>Po</b> 84 $V_{\text{at}} = 38.14 \text{ \AA}^3$ at 311 K 1s <sup>2</sup> 2s <sup>2</sup> p <sup>6</sup> 3s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 4s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> f <sup>14</sup> 5s <sup>2</sup> p <sup>6</sup> d <sup>10</sup> 6s <sup>2</sup> p <sup>4</sup>					
$\alpha$		hR2	$\alpha$ -As	2.609	$\alpha$		cP1	$\alpha$ -Po		
$\beta$	> 2.6	mC4	$\beta$ -Bi		$\beta$	> 327	hR1	$\beta$ -Po		
$\gamma$	> 3.0	mP4	$\beta$ -Sb							
$\delta$	> 4.3									
$\varepsilon$	> 9.0	cI2	W							

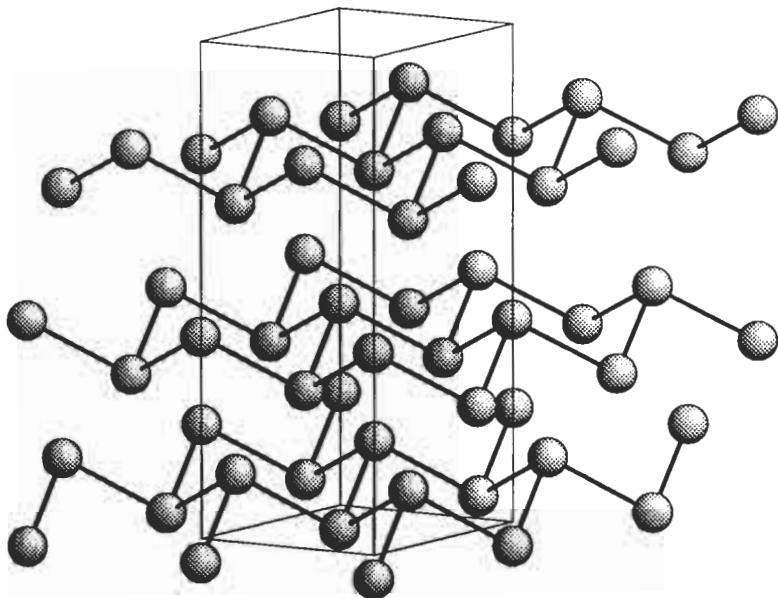


Fig. 31. The structure of hR2-As, space group  $\bar{R}\bar{3}m$ , No. 166, 6c 0 0 0.277.

Table 13

Intralayer ( $d_1$ ) and interlayer ( $d_2$ ) distances in  $\alpha$ -As-type layer structures,  $\gamma$ -Se-type helix structures and primitive cubic  $\alpha$ -Po (PEARSON[1972]).

Element	Distance $d_1$	Distance $d_2$	$d_2/d_1$
$\alpha$ -As	2.51 Å	3.15 Å	1.25
$\alpha$ -Sb	2.87 Å	3.37 Å	1.17
$\alpha$ -Bi	3.10 Å	3.47 Å	1.12
$\gamma$ -Se	2.32 Å	3.46 Å	1.49
$\gamma$ -Te	2.86 Å	3.46 Å	1.31
$\alpha$ -Po	3.37 Å	3.37 Å	1.00

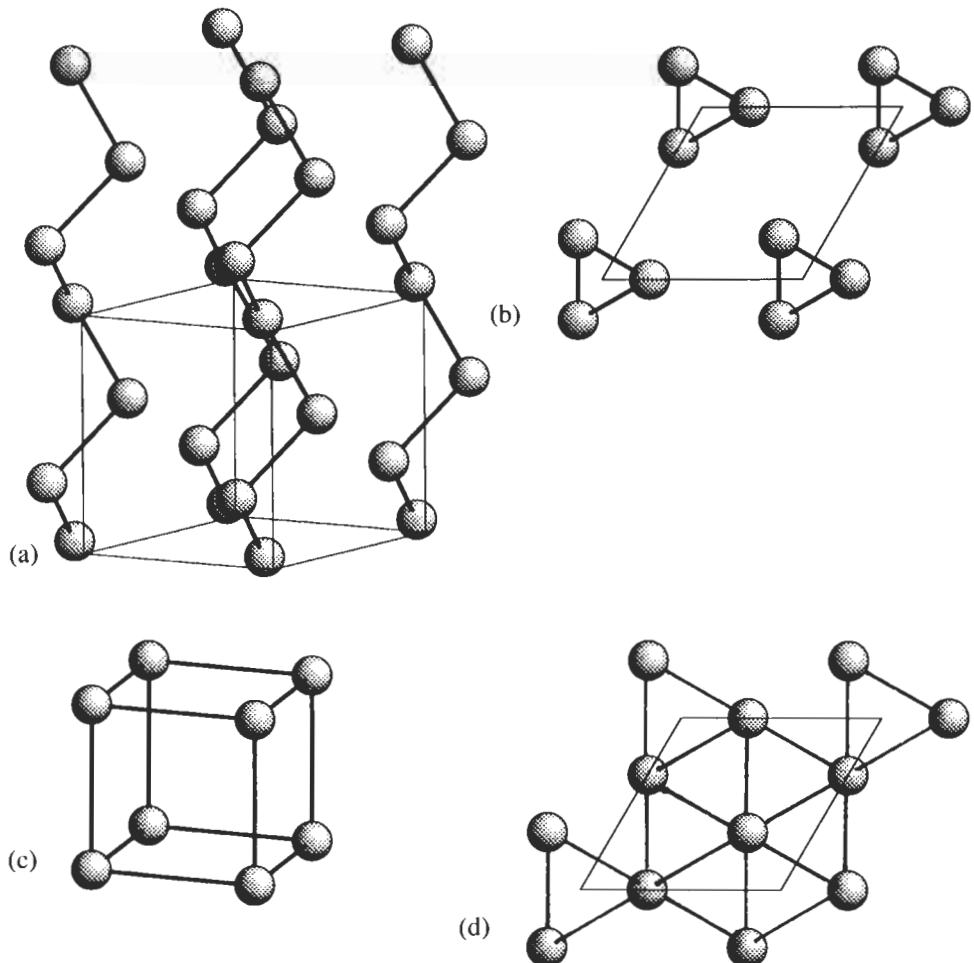


Fig. 32. (a) The structure of hP3–Se, space group  $P\bar{3}_121$ , No. 152,  $a = 0.237\text{ }\text{\AA}$ , and (b) its projection upon (001) compared with (c) one unit cell of cP1–Po, space group  $Pm\bar{3}m$ , No. 221,  $a = 0.0\text{ }\text{\AA}$ , and (d) its projection along [111]. The hexagonal outline of the projected cubic unit cell is drawn in.

Table 14

Structure information for the lanthanides and actinides. In the first line of each box the chemical symbol, atomic number Z, and the atomic volume  $V_{at}$  under ambient conditions is listed. In the second line the electronic ground state configuration is given. For each phase there is tabulated: limiting temperature T[K] and pressure P[GPa], Pearson symbol PS, prototype structure PT, and, if applicable, the lattice parameter ratio  $c/a$ .

T[K]	P[GPa]	PS	PT	$c/a$	T[K]	P[GPa]	PS	PT	$c/a$
<b>Ce</b> 58 $V_{at}=34.72 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^2 5s^2 p^6 6s^2$					<b>Th</b> 90 $V_{at}=32.87 \text{ \AA}^3$ $... 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} 6s^2 p^6 d^2 7s^2$				
$\alpha$ < 96		cF4	Cu		$\alpha$		cF4	Cu	
$\beta$		hP4	$\alpha$ -La	2×1.611	$\beta$	> 1633	cl2	W	
$\gamma$ > 326		cF4	Cu						
$\delta$ > 999		cl2	W						
$\alpha'$	> 5.1	oC4	$\alpha$ -U?						
$\varepsilon$	> 12.2	tI2	In						
<b>Pr</b> 59 $V_{at}=35.08 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^3 5s^2 p^6 6s^2$					<b>Pa</b> 91 $V_{at}=25.21 \text{ \AA}^3$ $... 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^2 6s^2 p^6 d^1 7s^2$				
$\alpha$		hP4	$\alpha$ -La	2×1.611	$\alpha$		tI2	$\alpha$ -Pa	0.825
$\beta$ > 1068		cl2	W		$\beta$	> 1443	cl2	W	
$\gamma$	> 3.8	cF4	Cu						
$\delta$	> 6.2	hp6	Pr	3×1.622					
$\varepsilon$	> 20	oC4	$\alpha$ -U						
<b>Nd</b> 60 $V_{at}=34.17 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^4 5s^2 p^6 6s^2$					<b>U</b> 92 $V_{at}=20.75 \text{ \AA}^3$ $... 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^3 6s^2 p^6 d^1 7s^2$				
$\alpha$		hP4	$\alpha$ -La	2×1.612	$\alpha$		oC4	$\alpha$ -U	
$\beta$ > 1136		cl2	W		$\beta$	> 941	tP30	$\beta$ -U	
$\gamma$	> 5.8	cF4	Cu		$\gamma$	> 1049	cl2	W	
$\delta$	> 18	hp6	Pr	3×1.611					
$\varepsilon$	> 38	mC4	?						
<b>Pm</b> 61 $V_{at}=33.60 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^5 5s^2 p^6 6s^2$					<b>Np</b> 93 $V_{at}=19.21 \text{ \AA}^3$ $... 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^5 6s^2 p^6 7s^2$				
$\alpha$		hP4	$\alpha$ -La	2×1.60	$\alpha$		oP8	$\alpha$ -Np	
$\beta$ > 1163		cl2	W		$\beta$	> 553	tP4	$\beta$ -Np	0.694
$\gamma$	> 10	cF4	Cu		$\gamma$	> 849	cl2	W	
$\delta$	> 18	hp6	Pr						
$\varepsilon$	> 40	?							

Continued on next page

Table 14—Continued

T[K]	P[GPa]	PS	PT	c/a	T[K]	P[GPa]	PS	PT	c/a
<b>Sm</b> 62	$V_{at}=33.17 \text{ \AA}^3$				<b>Pu</b> 94	$V_{at}=19.88 \text{ \AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^6 5s^2 p^6 6s^2$					$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^6 6s^2 p^6 7s^2$			
$\alpha$		hR3	$\alpha\text{-Sm}$	$4.5 \times 1.605$	$\alpha$		mP16	$\alpha\text{-Pu}$	
$\beta$	> 1007	hP2	Mg	1.596	$\beta$	> 388	mC34	$\beta\text{-Pu}$	
$\gamma$	> 1195	cI2	W		$\gamma$	> 488	oF8	$\gamma\text{-Pu}$	
$\delta$	> 4.5	hP4	$\alpha\text{-La}$	$2 \times 1.611$	$\delta$	> 583	cF4	Cu	
$\varepsilon$	> 14	cF4	Cu		$\delta'$	> 725	tI2	In	1.342
$\zeta$	> 19	hp6	Pr	$3 \times 1.611$	$\varepsilon$	> 756	cI2	W	
$\theta$	> 33	mC4	?		$\zeta$	> 40.0	hP8		1.657/2
<b>Eu</b> 63	$V_{at}=48.10 \text{ \AA}^3$				<b>Am</b> 95	$V_{at}=29.27 \text{ \AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^7 5s^2 p^6 6s^2$					$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^7 6s^2 p^6 7s^2$			
$\alpha$		cI2	W		$\alpha$		hP4	$\alpha\text{-La}$	$2 \times 1.621$
$\beta$	> 12.5	hP2	Mg	1.553	$\beta$	> 1042 or > 5	cF4	Cu	
$\gamma$	> 18	?			$\gamma$	> 1350	cI2	W	
<b>Gd</b> 64	$V_{at}=33.04 \text{ \AA}^3$				$\delta$	> 12.5	mP4	$\delta\text{-Am}$	
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^7 5s^2 p^6 5d^1 6s^2$				$\varepsilon$	> 15	oC4	$\alpha\text{-U}$	
$\alpha$		hP2	Mg	1.591	<b>Cm</b> 96	$V_{at}=29.98 \text{ \AA}^3$			
$\beta$	> 1508	cI2	W			$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^7 6s^2 p^6 d^1 7s^2$			
$\gamma$	> 2.0	hR3	$\alpha\text{-Sm}$	$4.5 \times 1.61$	$\alpha$		hP4	$\alpha\text{-La}$	$2 \times 1.621$
$\delta$	> 5	hP4	$\alpha\text{-La}$	$2 \times 1.624$	$\beta$	> 1550 or > 23	cF4	Cu	
$\varepsilon$	> 25	cF4	Cu		$\gamma$	> 43	oC4	$\alpha\text{-U}$	
$\zeta$	> 36	hp6	Pr		<b>Tb</b> 65	$V_{at}=32.04 \text{ \AA}^3$			
	$1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^9 5s^2 p^6 6s^2$					$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^8 6s^2 p^6 d^1 7s^2$			
$\alpha$	< 220	oC4	$\alpha'\text{-Dy}$		<b>Bk</b> 97	$V_{at}=27.96 \text{ \AA}^3$			
$\alpha'$		hP2	Mg	1.580		$\dots 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^8 6s^2 p^6 d^1 7s^2$			
$\beta$	> 1562	cI2	W		$\alpha$		hP4	$\alpha\text{-La}$	$2 \times 1.620$
$\gamma$	> 3.0	hR3	$\alpha\text{-Sm}$	$4.5 \times 1.60$	$\beta$	> 1250 or > 8	cF4	Cu	
$\delta$	> 6.0	hP4	$\alpha\text{-La}$		$\gamma$	> 25	oC4	$\alpha\text{-U}$	
$\varepsilon$	> 29	cF4	Cu						
$\zeta$	> 32	hp6	Pr	$3 \times 1.616$					

Continued on next page

Table 14—Continued

T[K]	P[GPa]	PS	PT	c/a	T[K]	P[GPa]	PS	PT	c/a
<b>Dy</b> 66	$V_{at}=31.57 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{10} 5s^2 p^6 6s^2$				<b>Cf</b> 98	$V_{at}=27.41 \text{ \AA}^3$ ... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{10} 6s^2 p^6 7s^2$			
$\alpha'$ < 86		oC4	$\alpha'$ -Dy		$\alpha$		hP4	$\alpha$ -La	$2 \times 1.625$
$\alpha$		hP2	Mg	1.573	$\beta$ > 863 or > 17		cF4	Cu	
$\beta$ > 1654		cl2	W		$\gamma$ > 30		aP4	$\gamma$ -Cf	
$\gamma$ > 5.0		hR3	$\alpha$ -Sm	4.5×1.606	$\delta$ > 41		oC4	$\alpha$ -U	
$\delta$ > 9.0		hP4	$\alpha$ -La						
$\varepsilon$ > 38		cF4	Cu						
<b>Ho</b> 67	$V_{at}=31.12 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{11} 5s^2 p^6 6s^2$				<b>Es</b> 99				
$\alpha$		hP2	Mg	1.570	... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{11} 6s^2 p^6 7s^2$				
$\beta$ > 1660		cl2	W		$\alpha$	hP4	$\alpha$ -La		
$\gamma$ > 7.0		hR3	$\alpha$ -Sm	4.5×1.63	$\beta$ ?	cF4	Cu		
$\delta$ > 13		hP4	$\alpha$ -La						
<b>Er</b> 68	$V_{at}=30.65 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{12} 5s^2 p^6 6s^2$				<b>Fm</b> 100				
$\alpha$		hP2	Mg	1.569	... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{12} 6s^2 p^6 7s^2$				
$\beta$ > 7.0		hR3	$\alpha$ -Sm						
$\gamma$ > 13		hP4	$\alpha$ -La						
<b>Tm</b> 69	$V_{at}=30.10 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{13} 5s^2 p^6 6s^2$				<b>Md</b> 101				
$\alpha$		hP2	Mg	1.570	... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{13} 6s^2 p^6 7s^2$				
$\beta$ > 1800		cl2	W						
$\gamma$ > 9		hR3	$\alpha$ -Sm						
$\delta$ > 13		hP4	$\alpha$ -La	4.5×1.57					
<b>Yb</b> 70	$V_{at}=41.24 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 6s^2$				<b>No</b> 102				
$\alpha$ < 270 or > 34		hP2	Mg	1.646	... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{14} 6s^2 p^6 7s^2$				
$\beta$		cF4	Cu						
$\gamma$ > 1047 or > 3.5		cl2	W						
<b>Lu</b> 71	$V_{at}=29.52 \text{ \AA}^3$ $1s^2 2s^2 p^6 3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^1 6s^2$				<b>Lr</b> 103				
		hP2	Mg	1.583	... $3s^2 p^6 d^{10} 4s^2 p^6 d^{10} f^{14} 5s^2 p^6 d^{10} f^{14} 6s^2 p^6 d^1 7s^2$				
$\beta$ > 18		hR3	$\alpha$ -Sm	4.5×1.52					
$\gamma$ > 35		hP4	$\alpha$ -La						

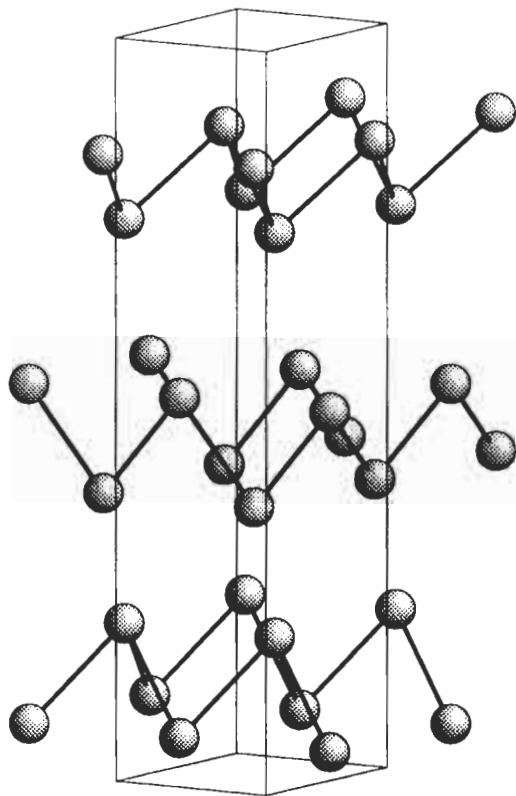


Fig. 33. The structure of hP6-Pr, space group  $P\bar{3}_121$ , No. 152, 6c 0.28 0.28 0.772.

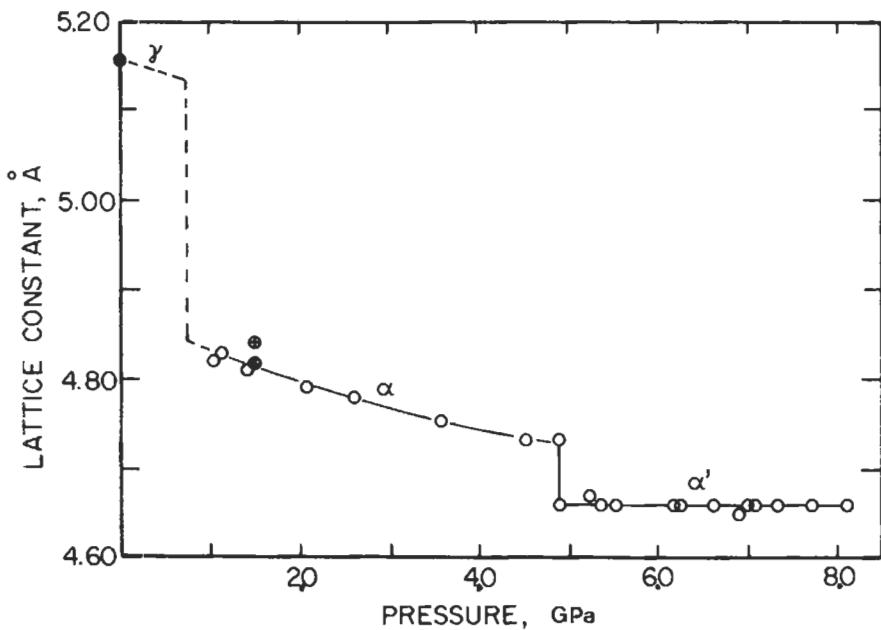


Fig. 34. Pressure dependence of the atomic volume of cerium (from DONOHUE [1974]).

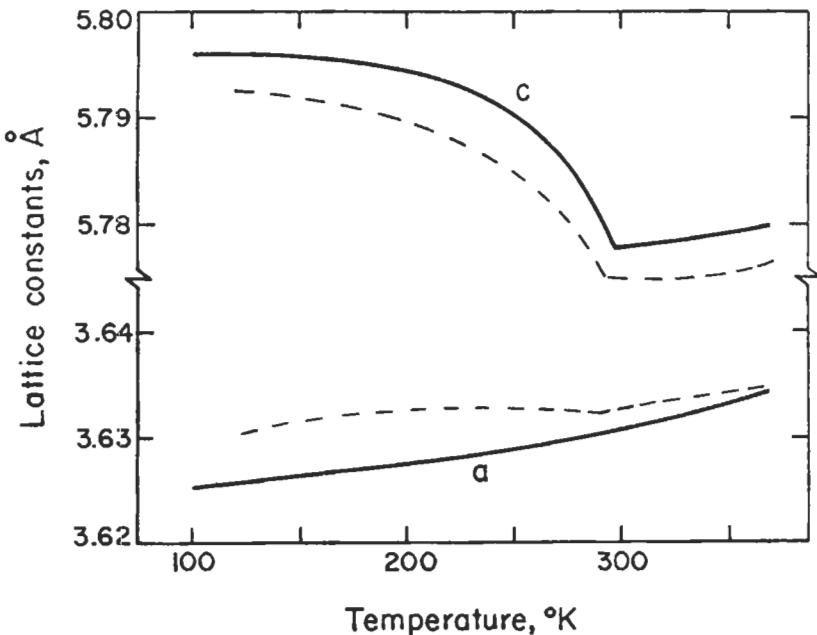


Fig. 35. Variation of the lattice parameters of gadolinium with temperature. There are no structural changes in this temperature range (from DONOHUE [1974]).

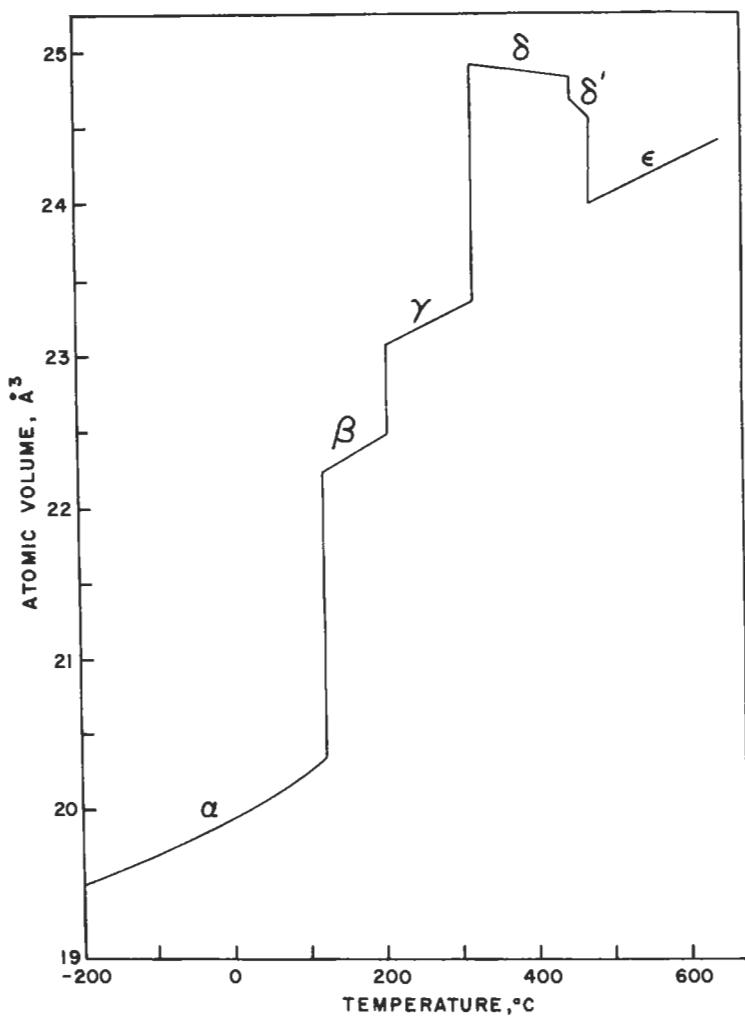


Fig. 36. The variation of the atomic volume of the various allotropes of plutonium with temperature (from DONOHUE [1974]).